Name: $\qquad$

Entry number: $\qquad$
There are 3 questions for a total of 10 points.

1. (3 points) Let the matrix representation of gates $U_{1}$ and $U_{2}$ be $U_{1}=\left[\begin{array}{ll}p & q \\ r & s\end{array}\right]$ and $U_{2}=\left[\begin{array}{ll}a & b \\ c & d\end{array}\right]$. Give the states $\left|\psi_{1}\right\rangle,\left|\psi_{2}\right\rangle,\left|\psi_{3}\right\rangle,\left|\psi_{4}\right\rangle$ in the circuits below.

2. (2 points) What is the input-output behaviour of the following circuit. ( $U^{*}$ denotes conjugate transpose.)


| Input | Output |
| :---: | :---: |
| $\|00\rangle\|\psi\rangle$ |  |
| $\|01\rangle\|\psi\rangle$ |  |
| $\|10\rangle\|\psi\rangle$ |  |
| $\|11\rangle\|\psi\rangle$ |  |

3. (5 points) Give the the intermediate states $\left|\psi_{0}\right\rangle,\left|\psi_{1}\right\rangle,\left|\psi_{2}\right\rangle,\left|\psi_{3}\right\rangle$ of the 3-qubit circuit given below. Show your calculations.

