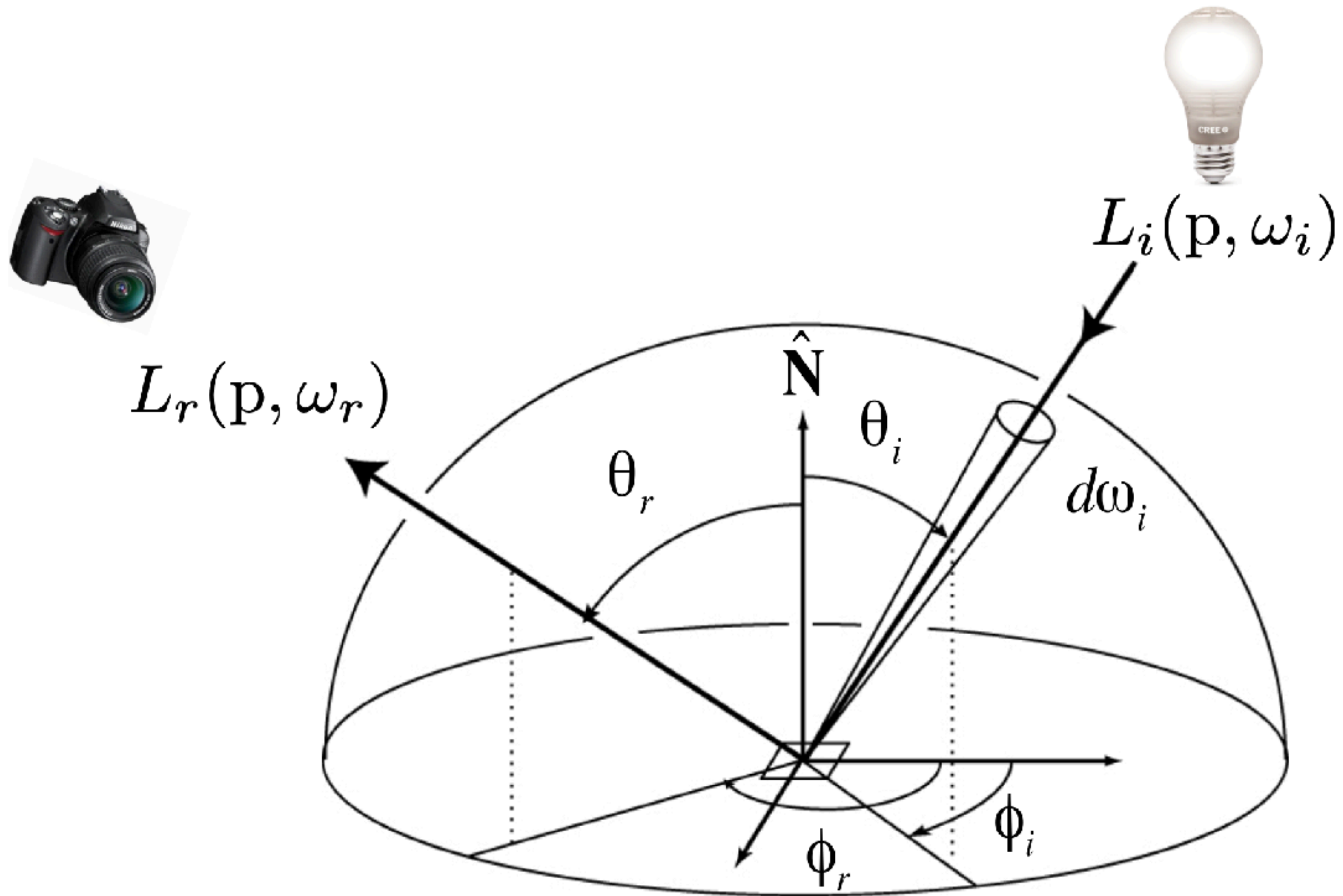


COL781: Computer Graphics

# 37. Real-Time Rendering



$$L_o(\mathbf{x}, \boldsymbol{\omega}_r) = L_e(\mathbf{p}, \boldsymbol{\omega}_o) + \int_{H^2} f_r(\boldsymbol{\omega}_i \rightarrow \boldsymbol{\omega}_r) L_i(\mathbf{x}, \boldsymbol{\omega}_i) \cos(\theta_i) d\boldsymbol{\omega}_i$$

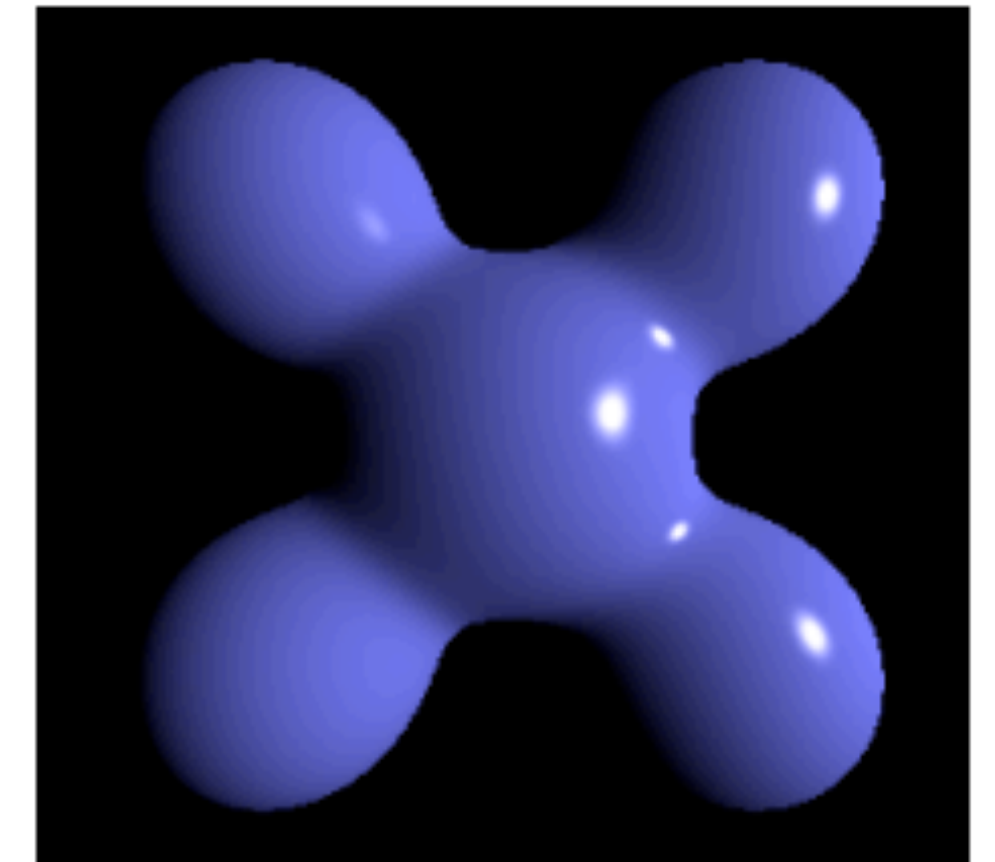
How to do **realistic** rendering in rasterization?

~~$$L_o = k_a I_a + k_d I \max(0, \mathbf{n} \cdot \mathbf{l}) + k_s I \max(0, \mathbf{n} \cdot \mathbf{h})^p$$~~

$$L_o(\mathbf{p}, \omega_o) = L_e(\mathbf{p}, \omega_o) + \int_{H^2} f_r(\mathbf{p}, \omega_i \rightarrow \omega_o) L_i(\mathbf{p}, \omega_i) \cos(\theta_i) d\omega_i$$

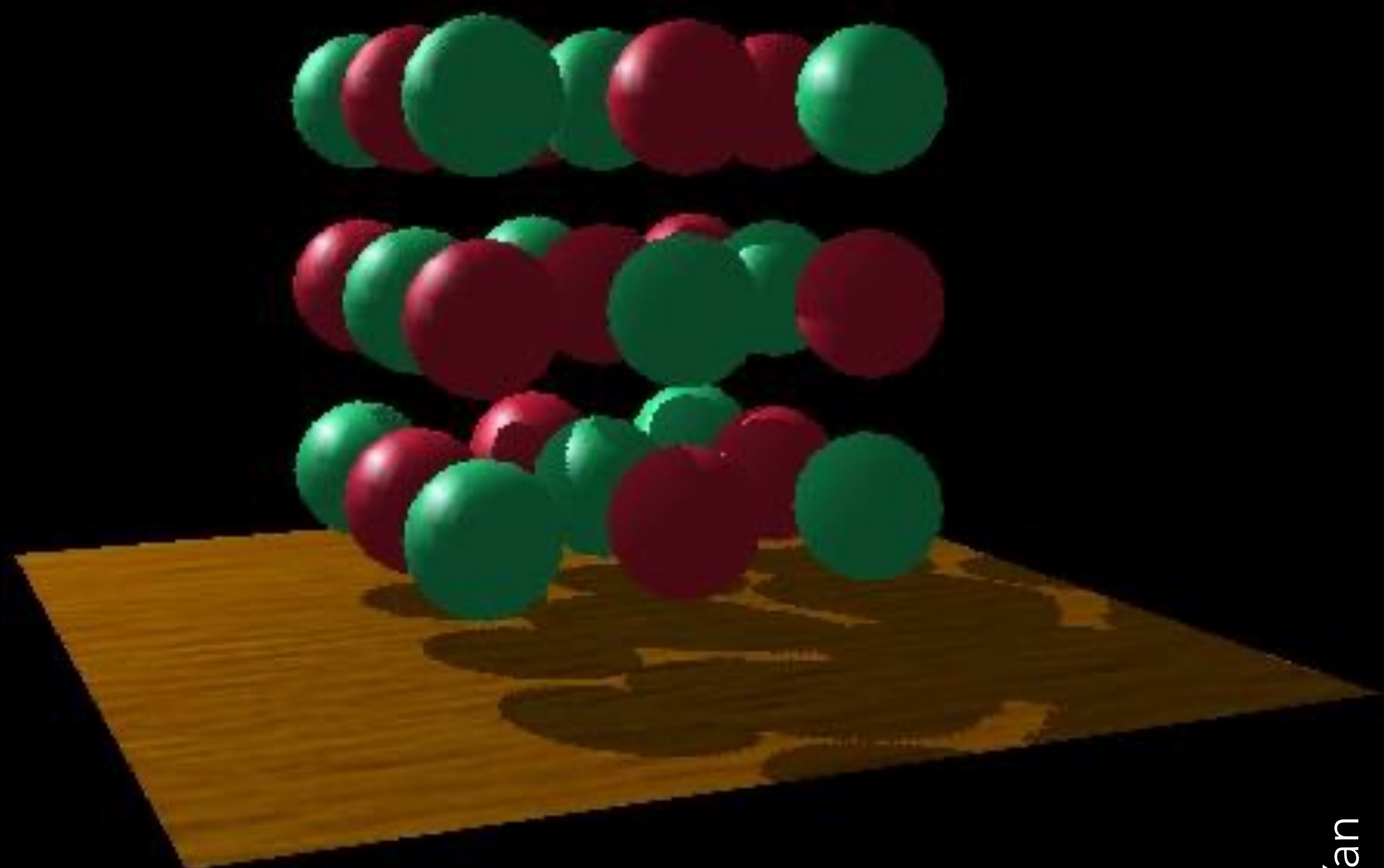
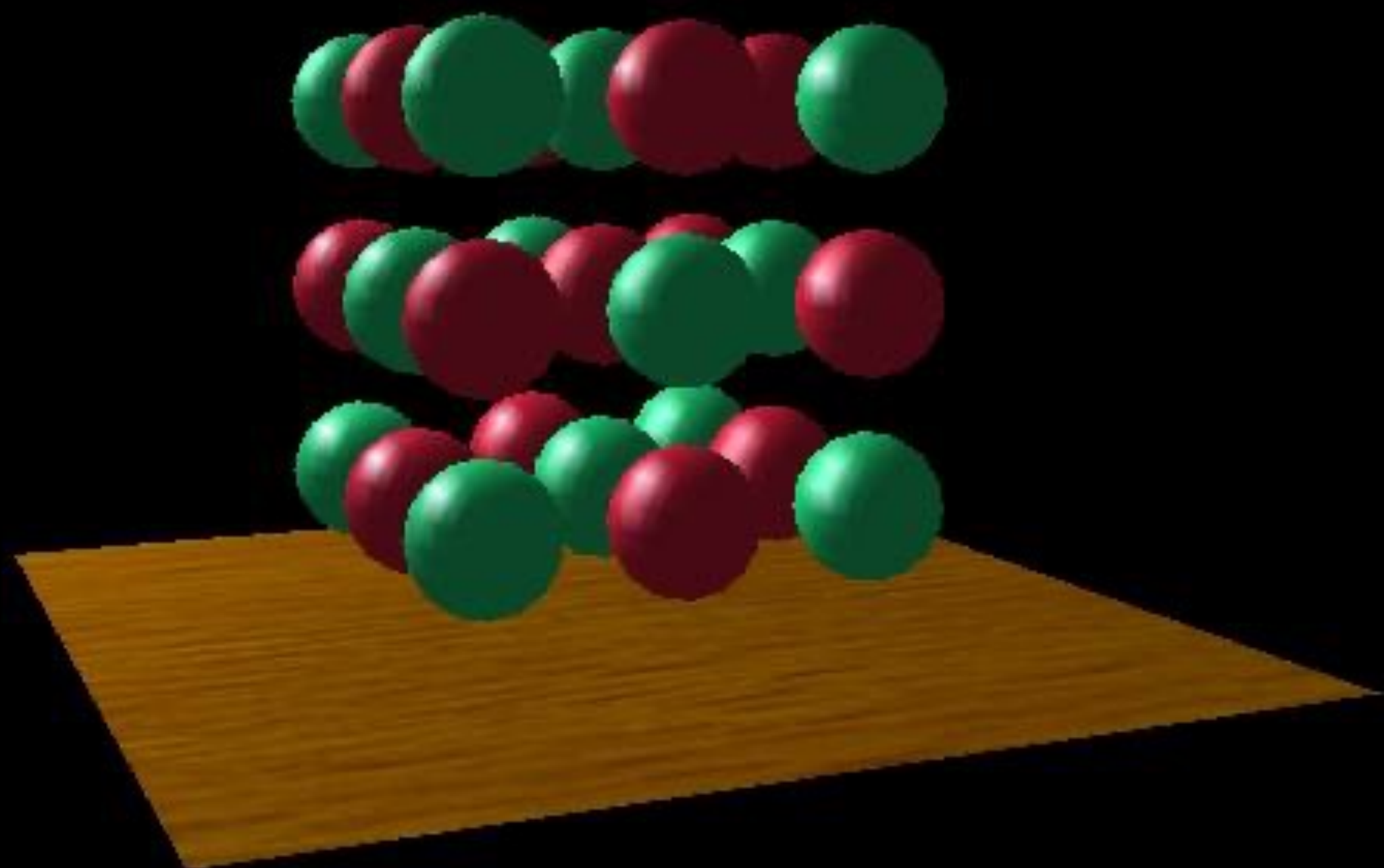
approximate

approximate





# Shadows

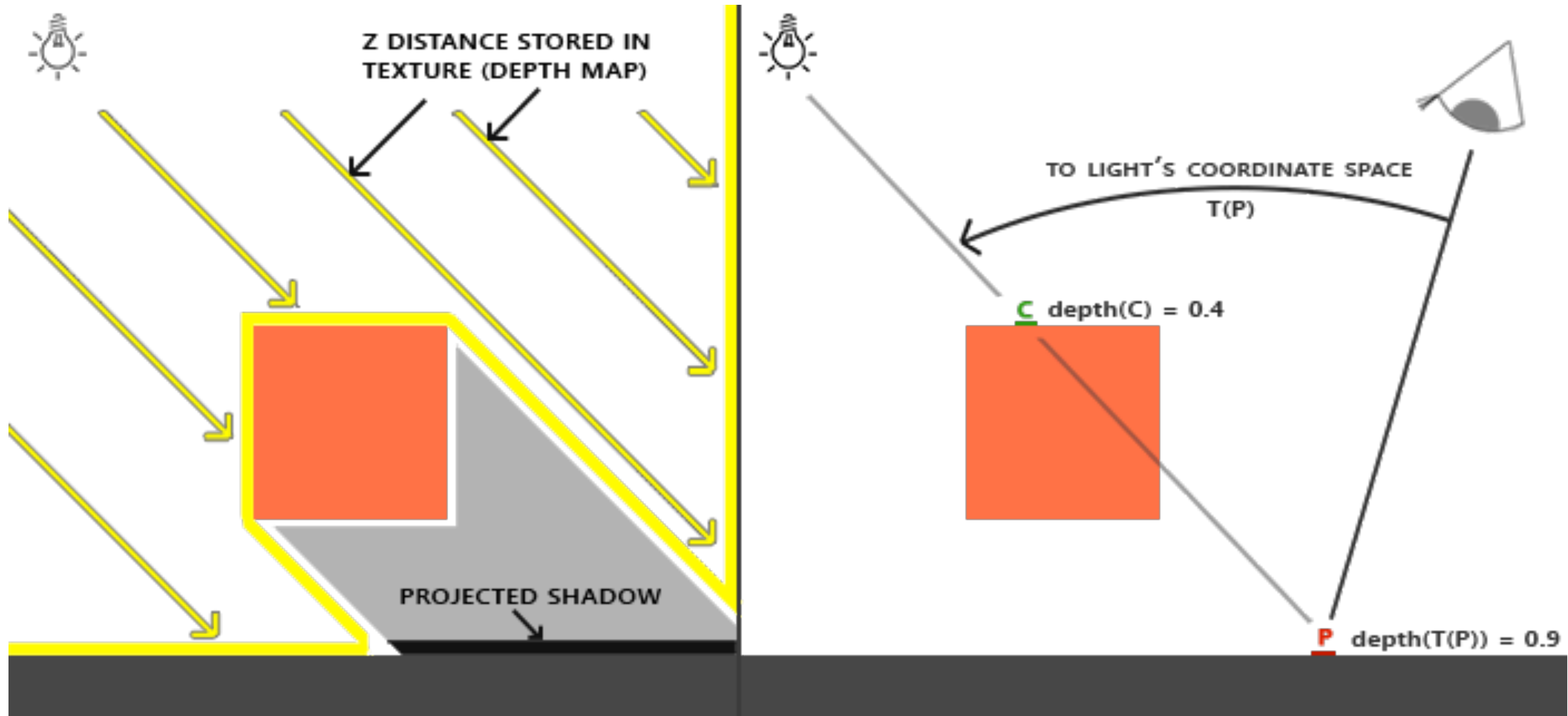


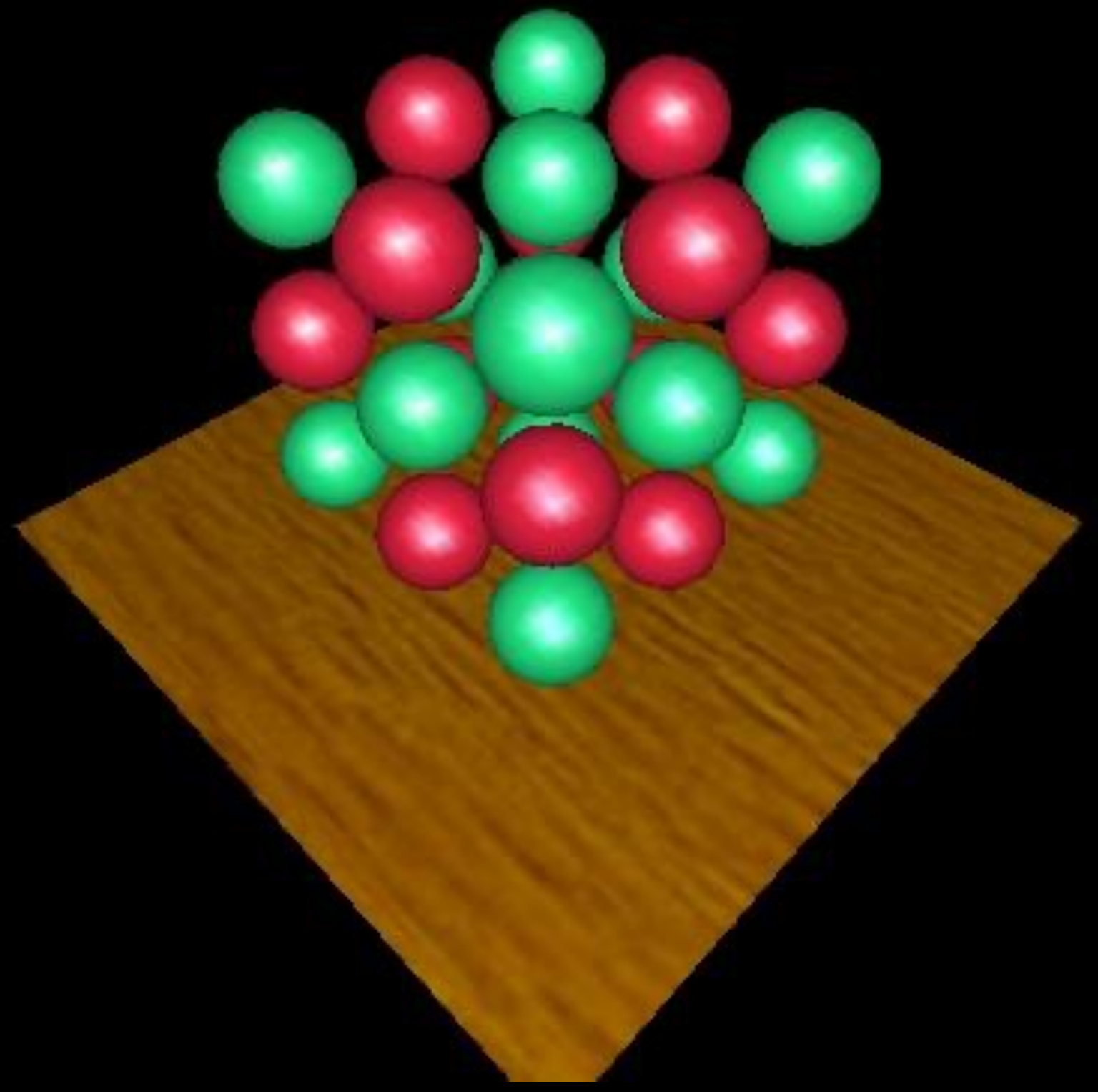
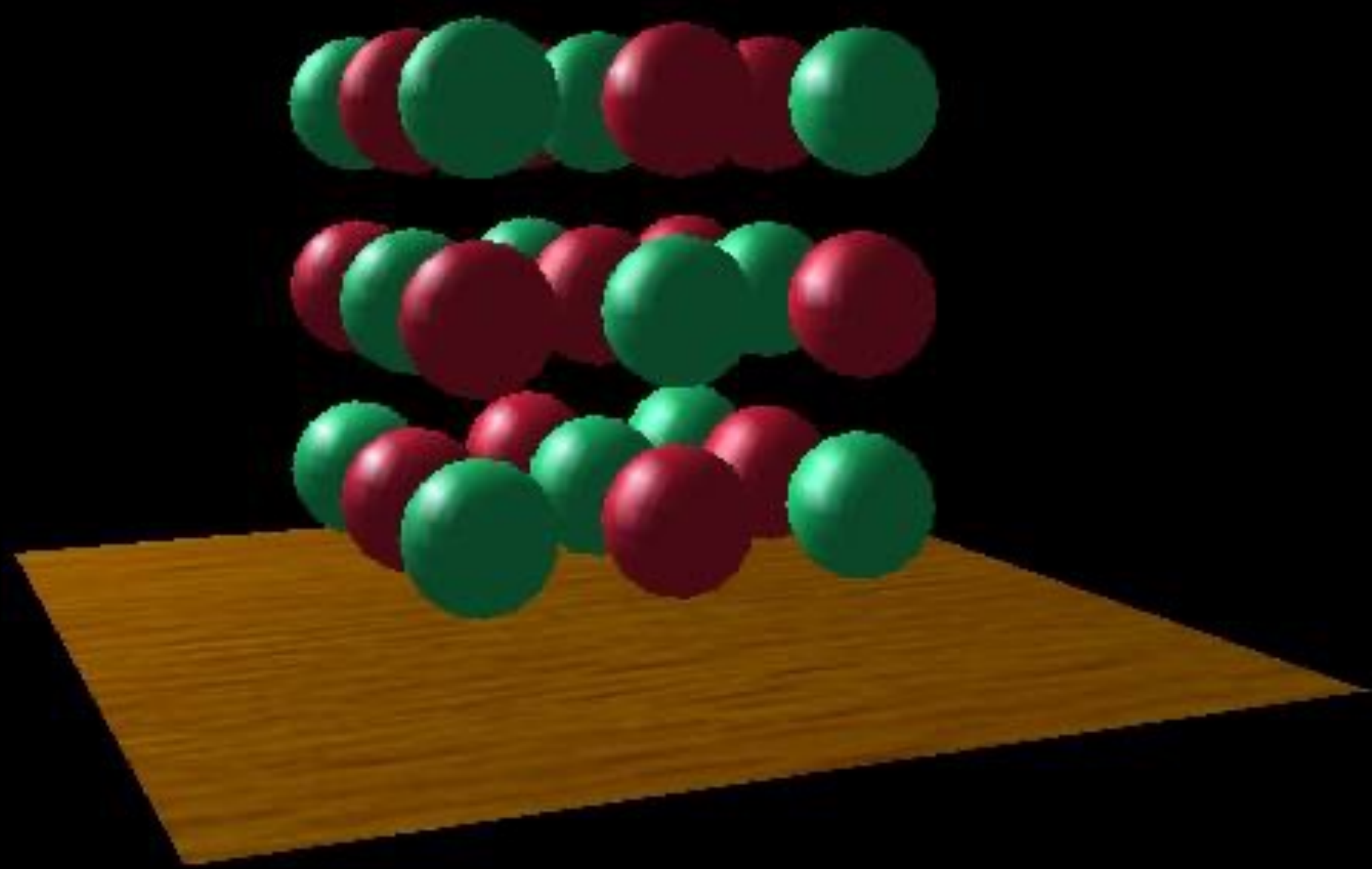


Assume only direct illumination from a point light  $\mathbf{p}'$ .

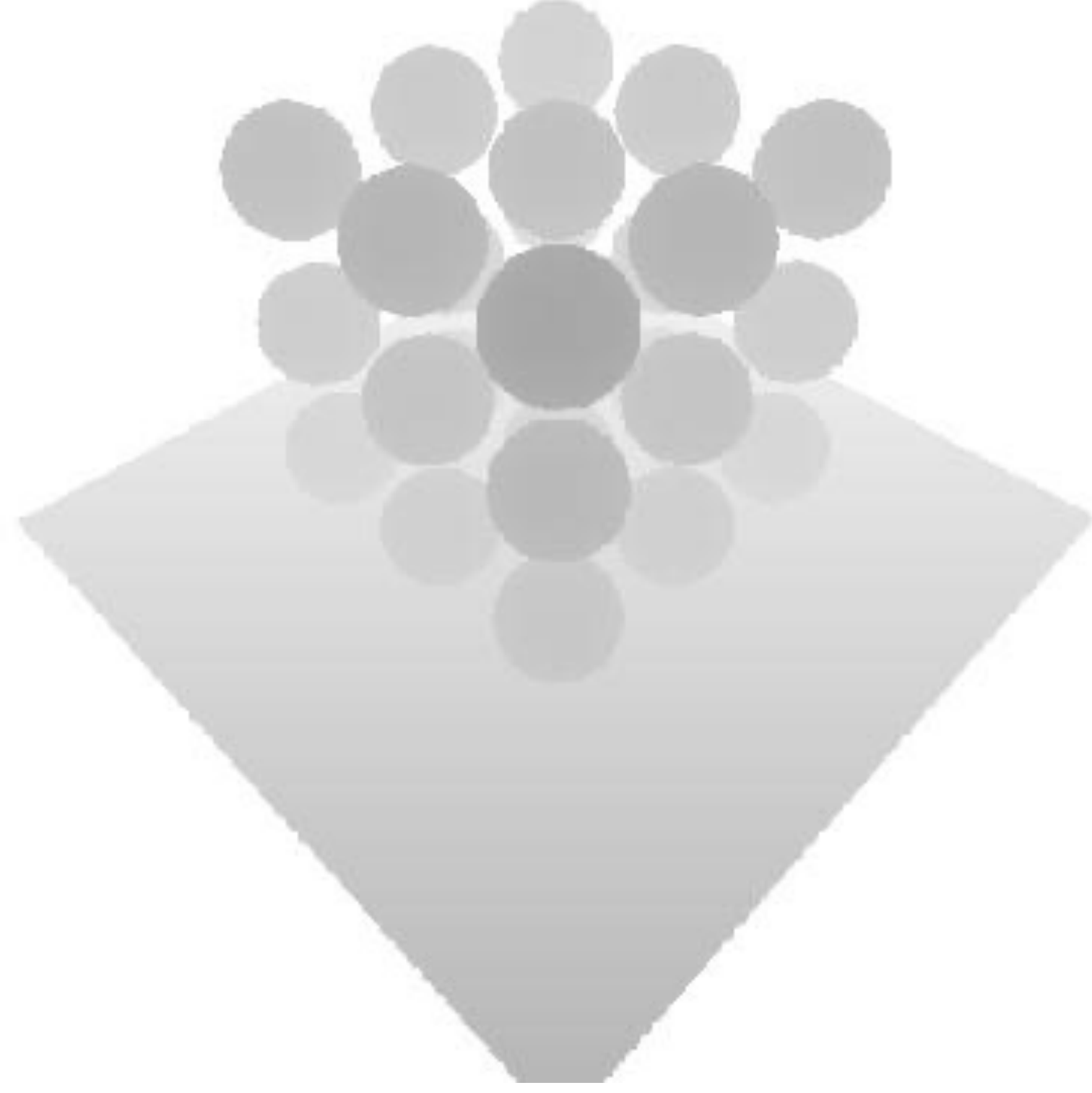
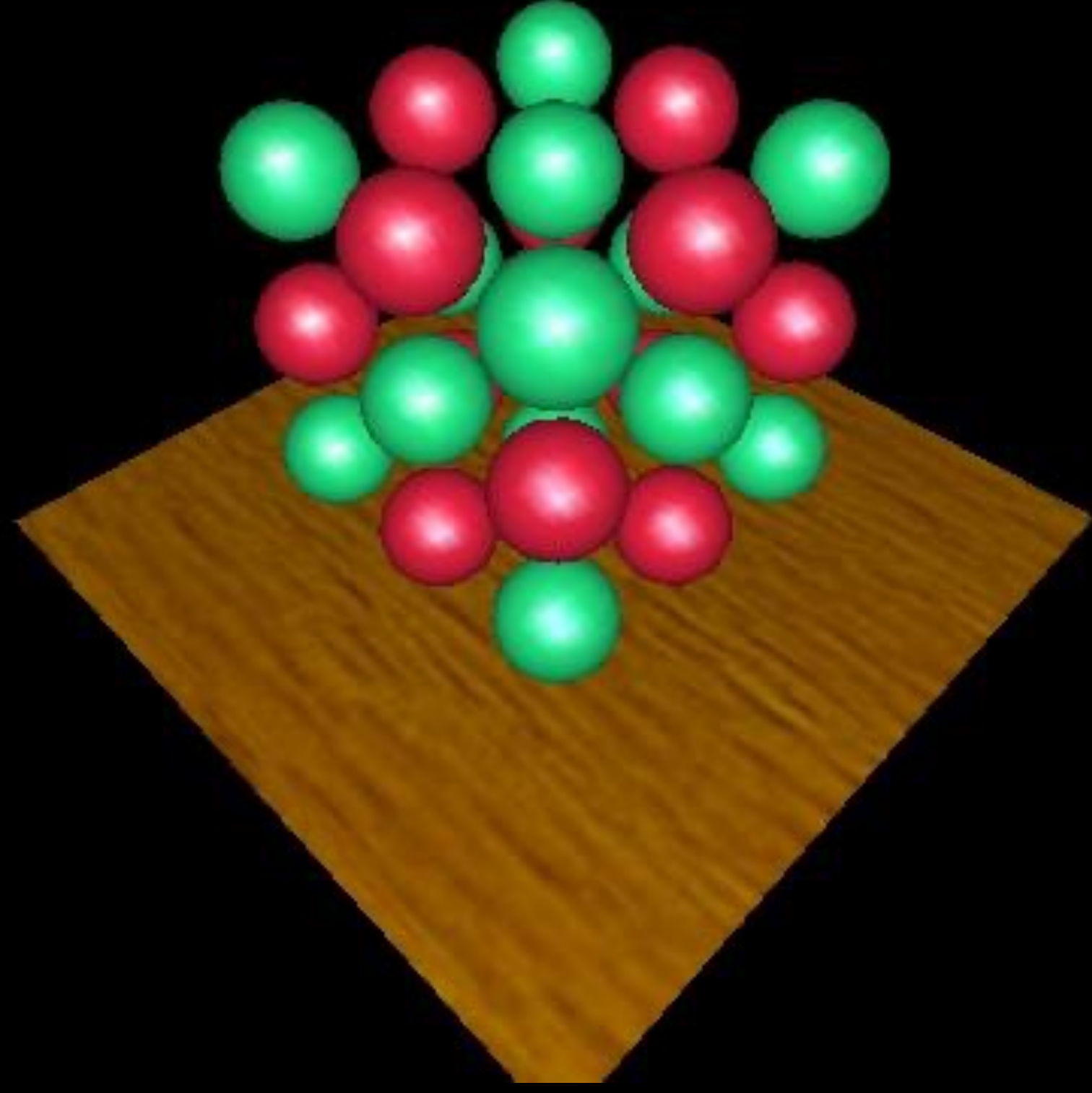
$$L_o(\mathbf{p}, \boldsymbol{\omega}_o) = f_r(\mathbf{p}, \boldsymbol{\omega}_i \rightarrow \boldsymbol{\omega}_o) l_o(\mathbf{p}', \boldsymbol{\omega}') V(\mathbf{p}, \mathbf{p}')$$

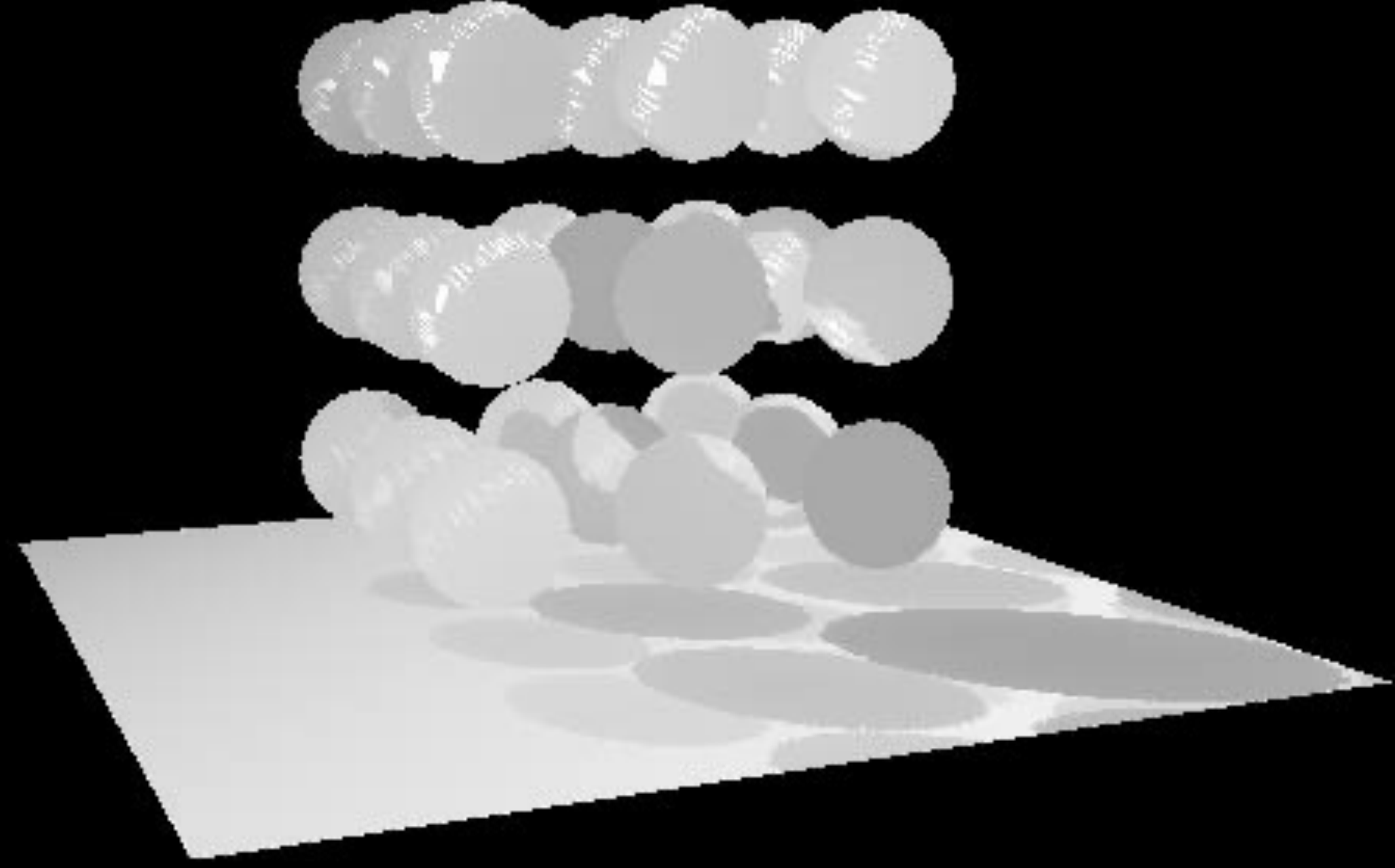
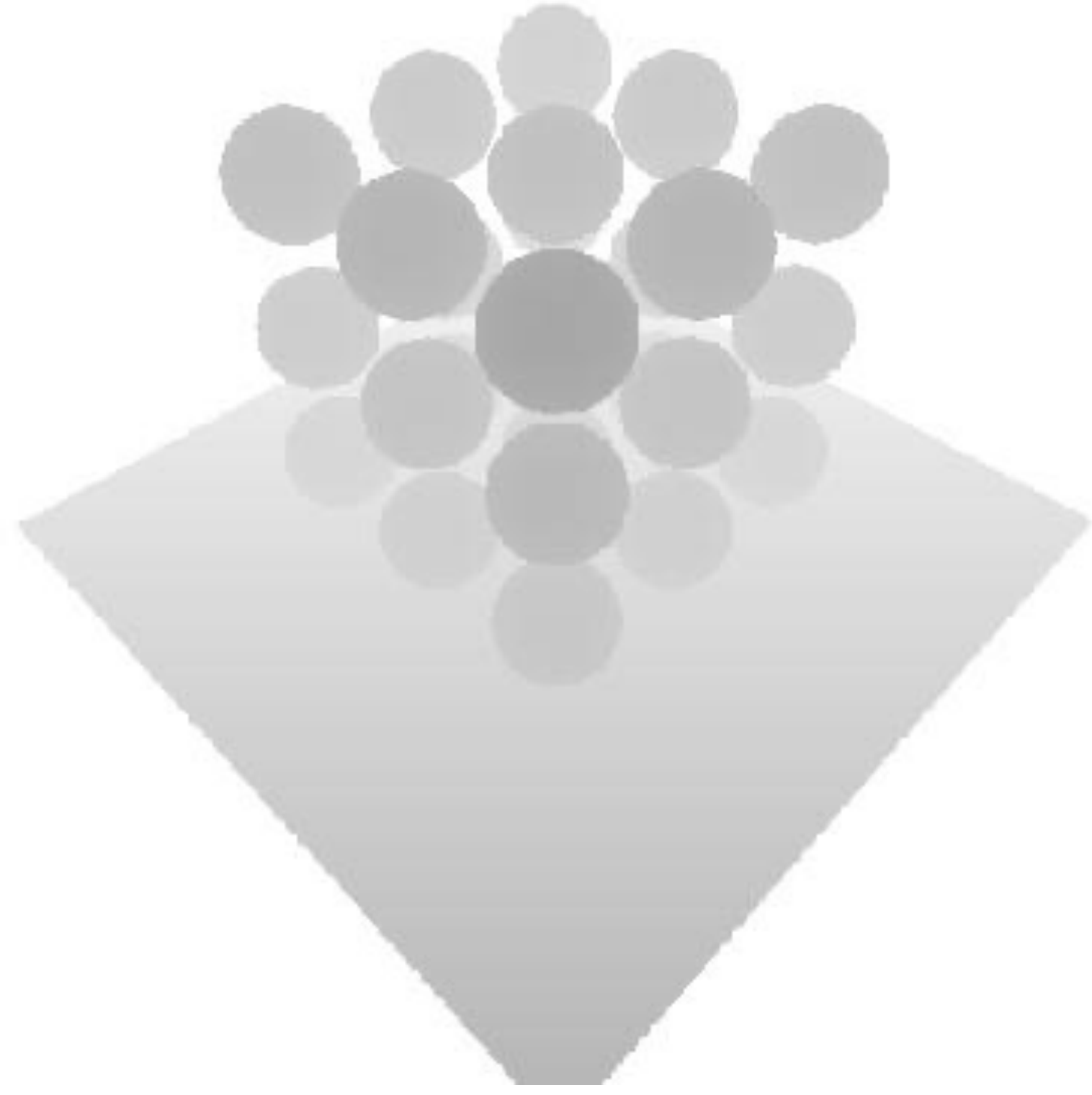
# Shadow maps

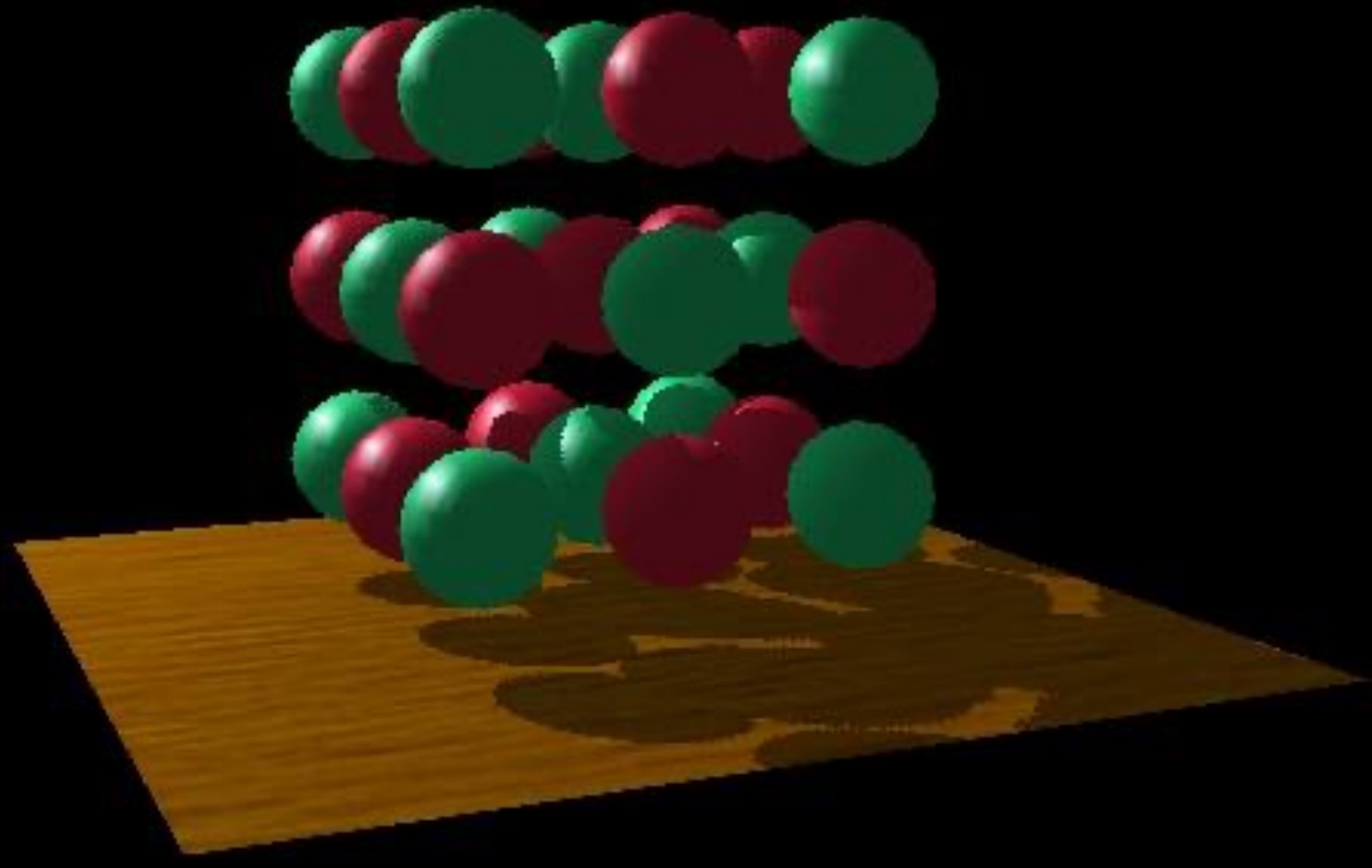
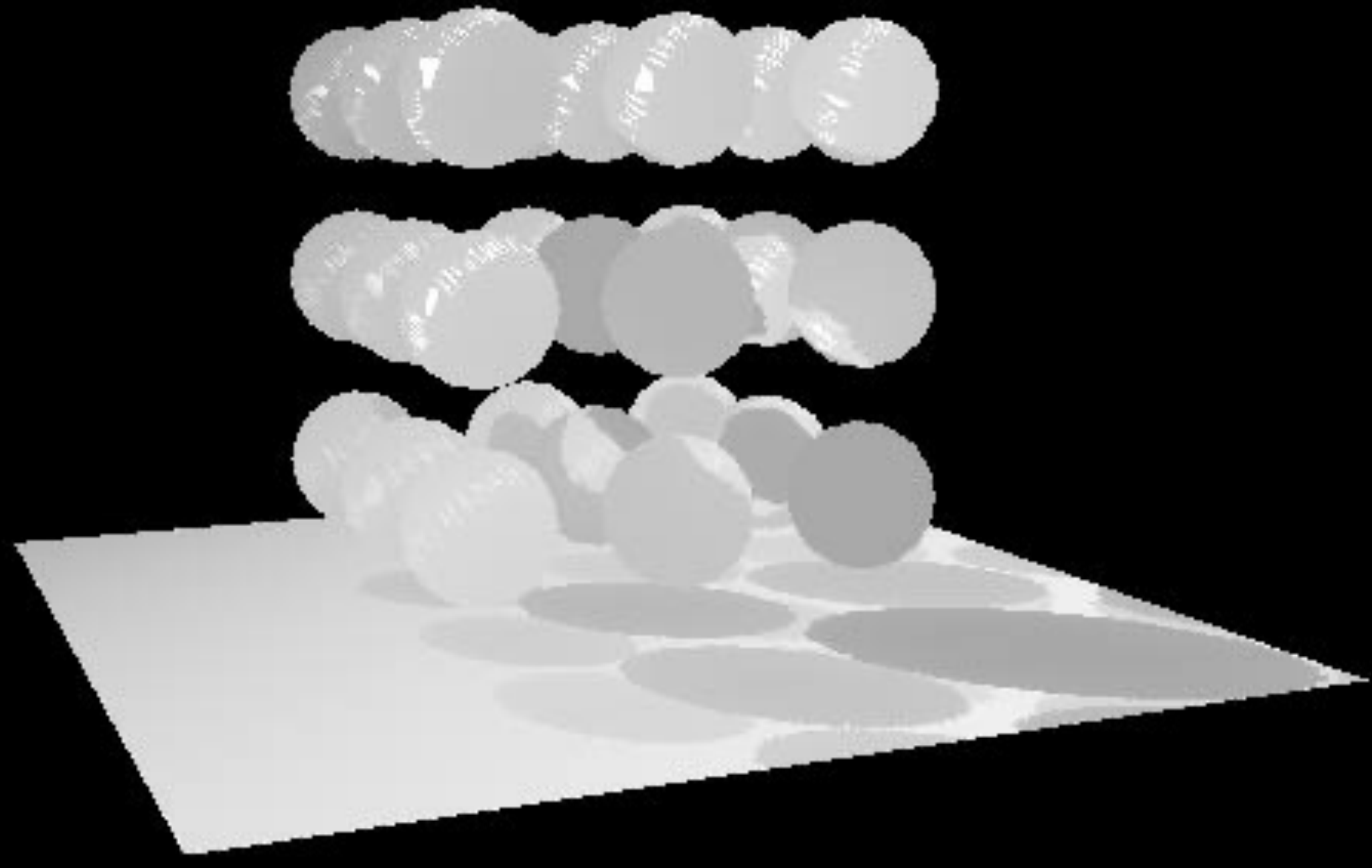




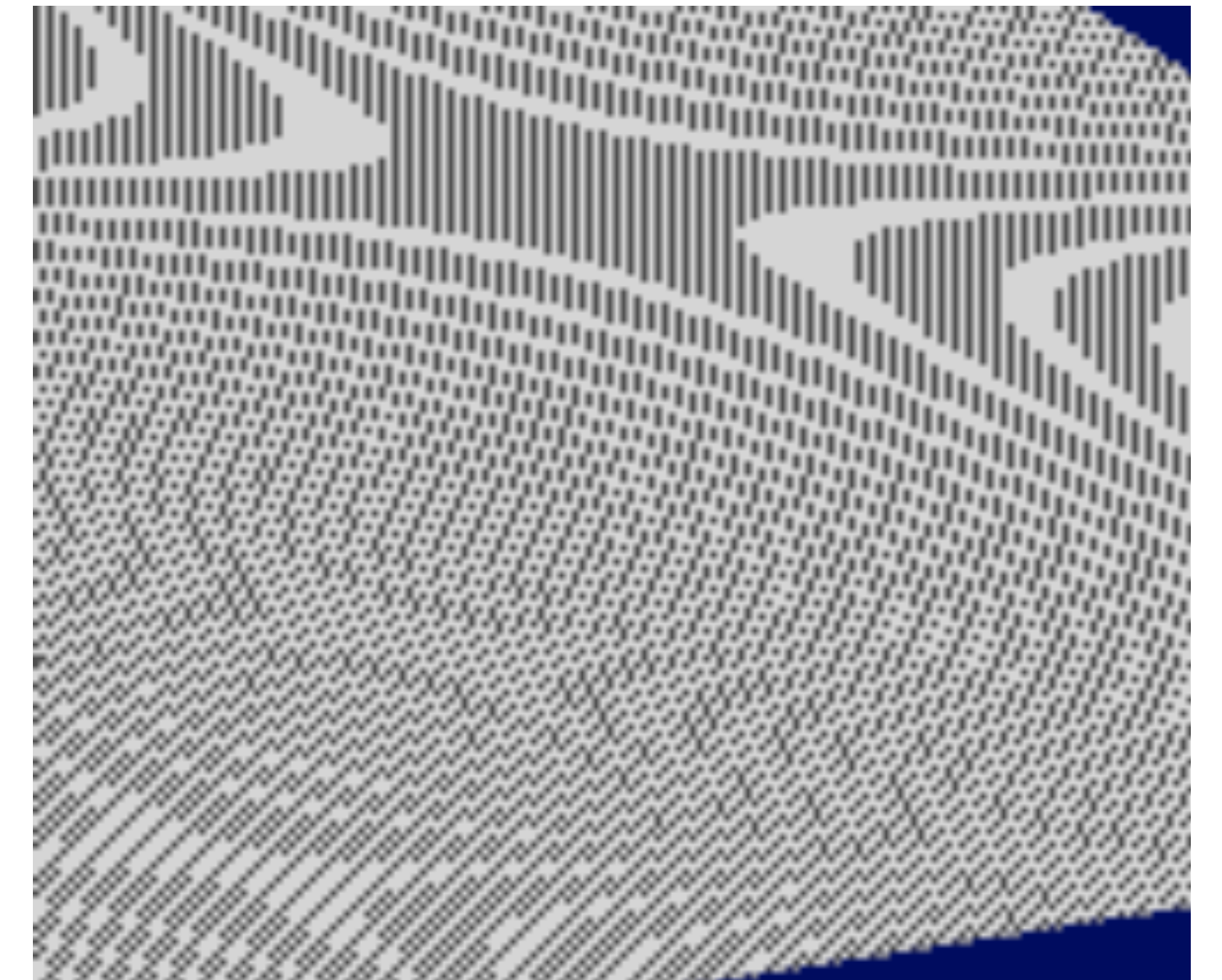
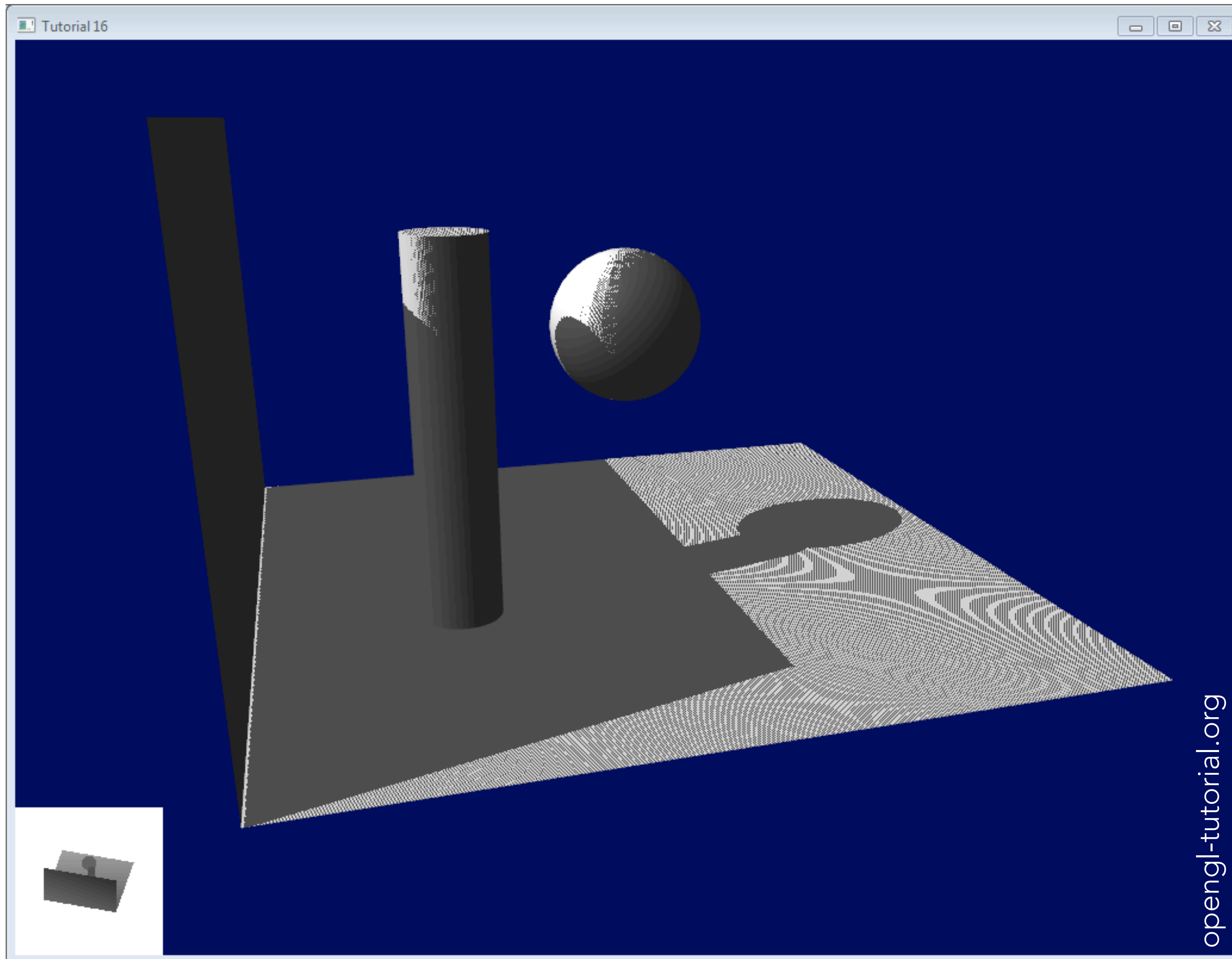




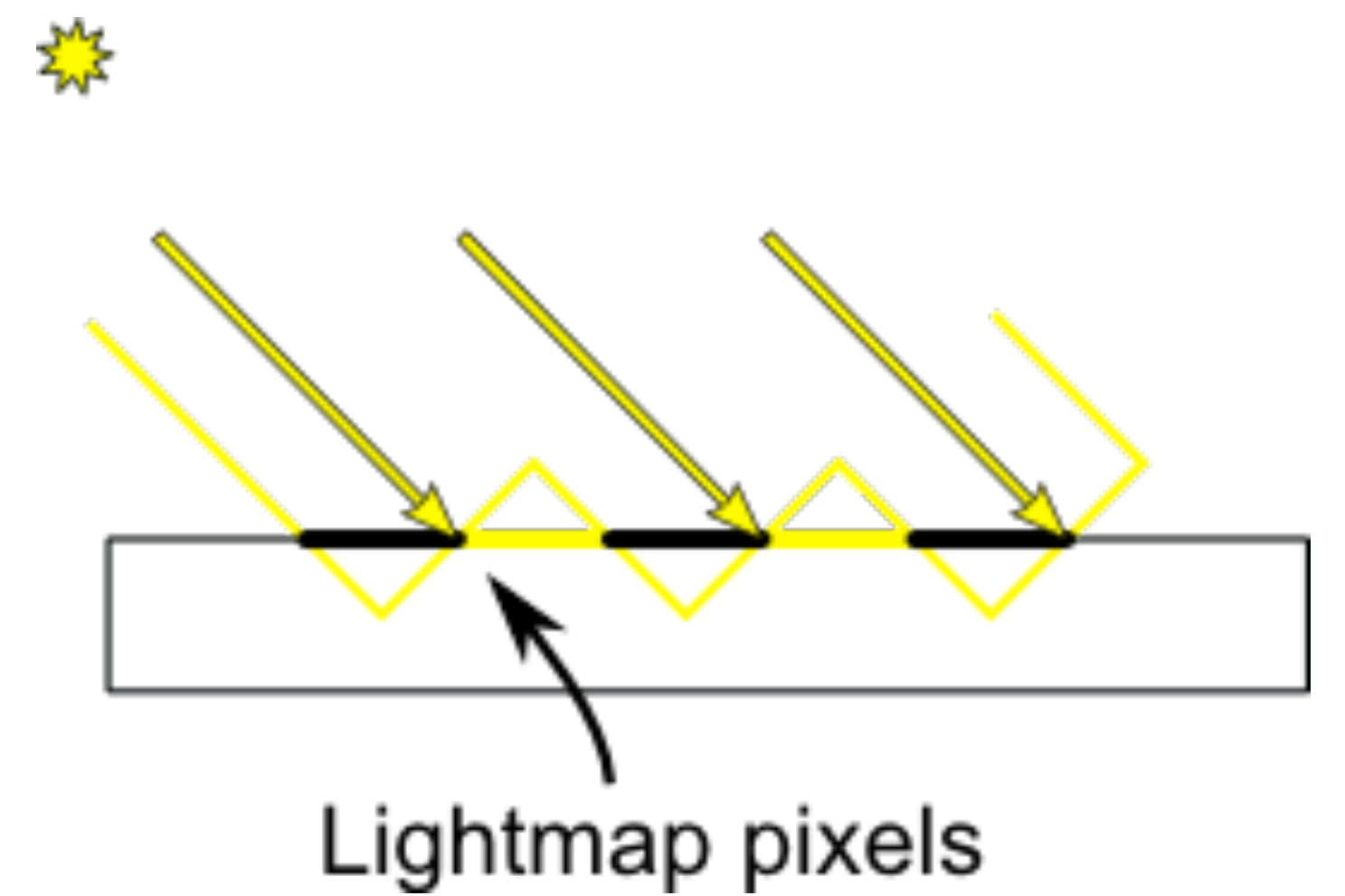




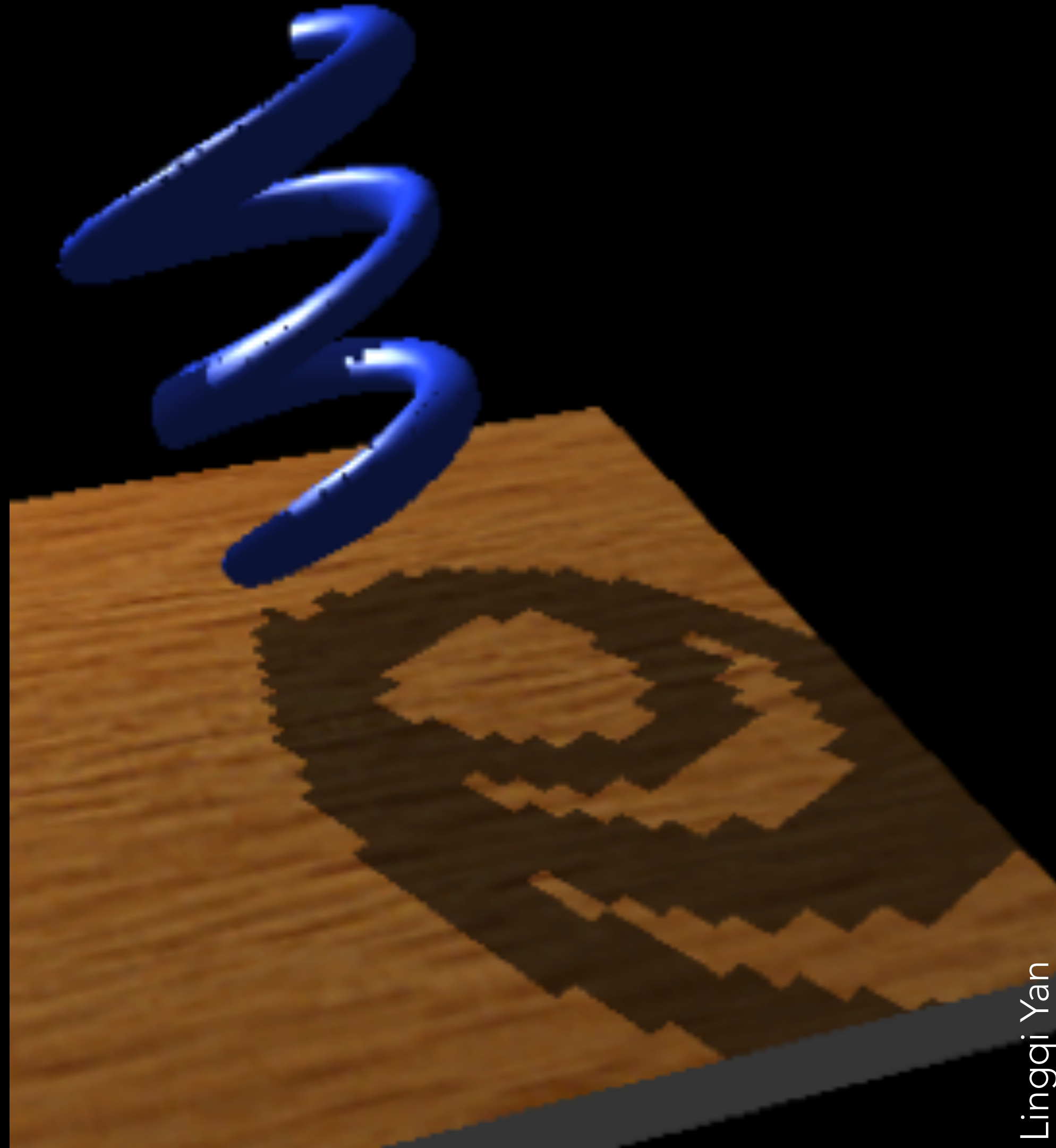




"Shadow acne"



# Aliasing



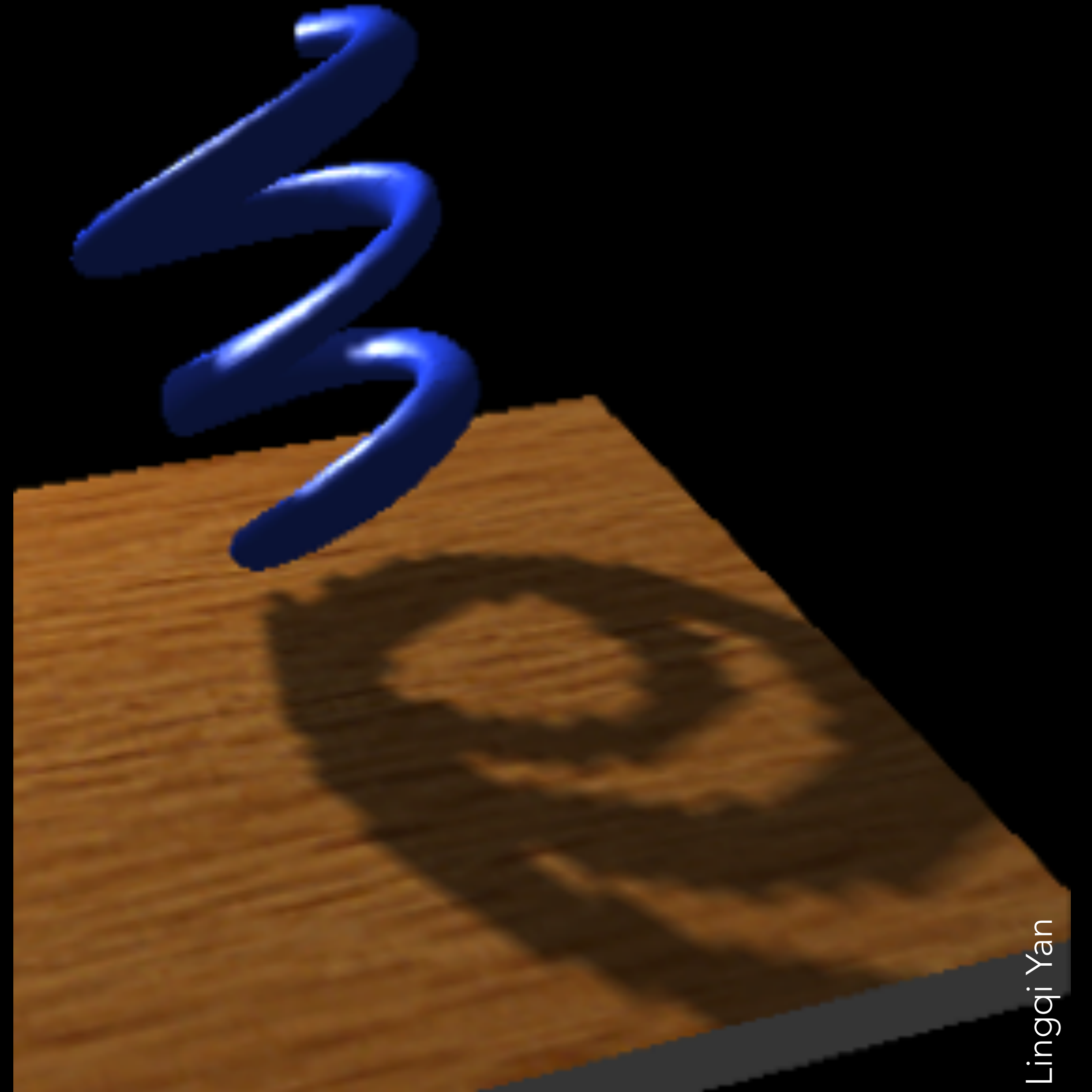
Lingqi Yan



# Percentage closer filtering (PCF)

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	1	1	1
0	0	0	0	0	1	1	1	1
0	0	0	0	0	1	1	1	1
0	0	0	0	1	1	1	1	1
0	0	0	0	1	1	1	1	1
1	1	1	1	1	1	1	1	1

0	0	0	1
0	0	1	1
1	1	1	1
1	1	1	1





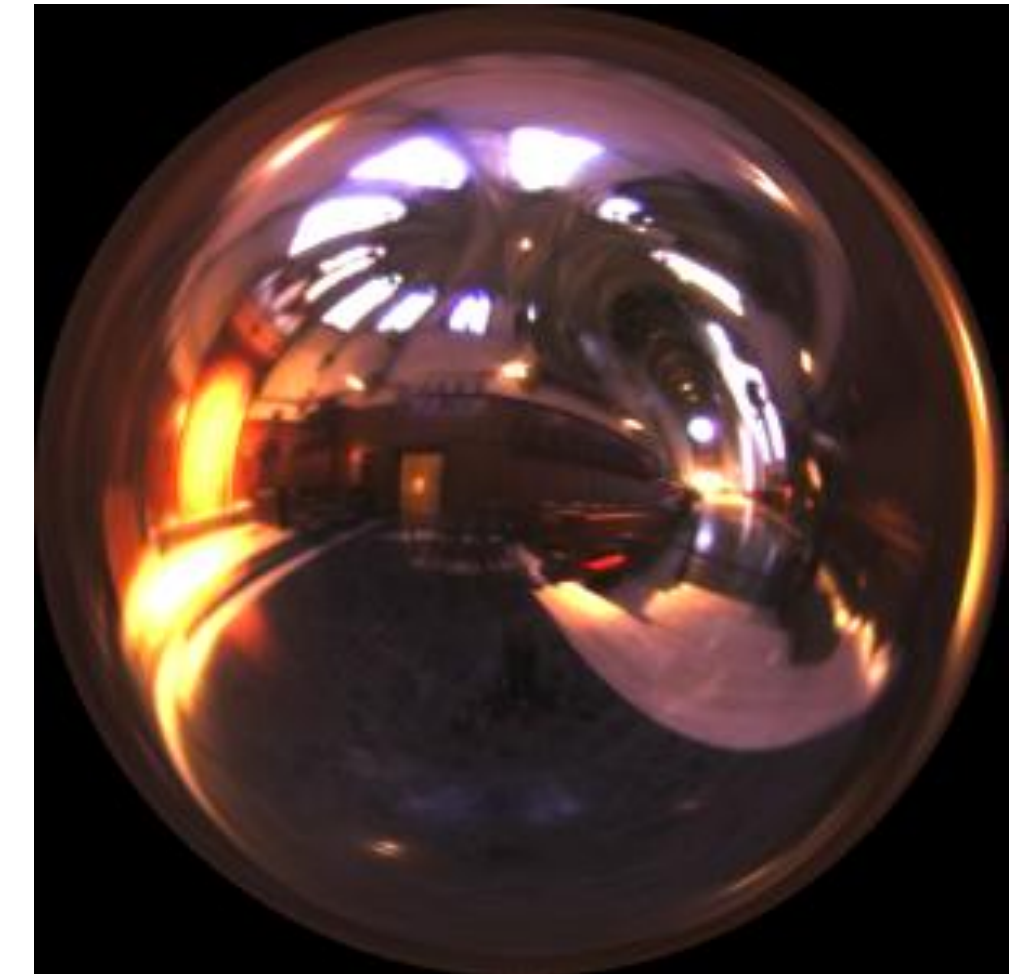
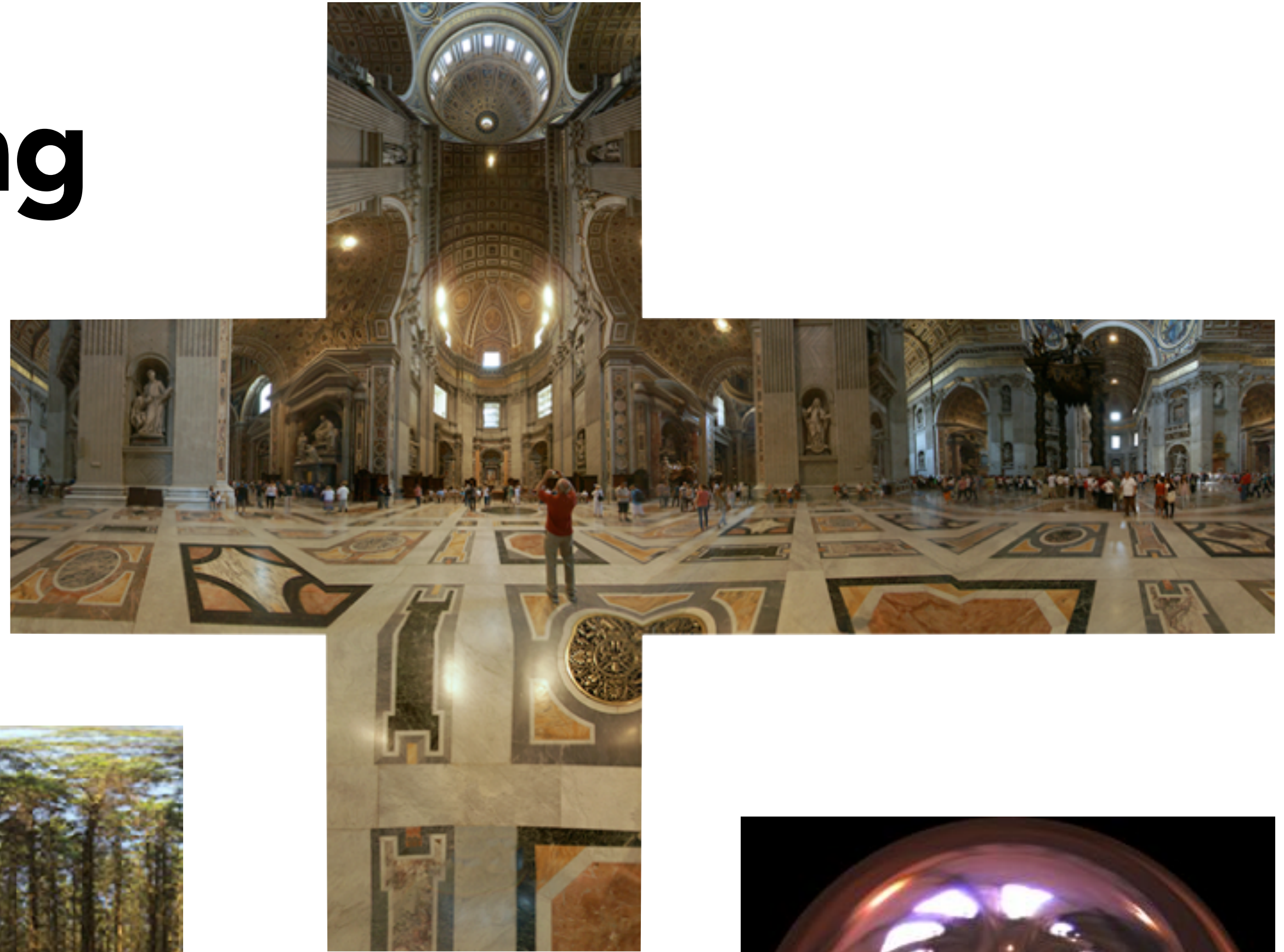
Moral(s) of the story:

1. **Precompute as much as possible!**
2. **Render the scene from the right viewpoint** to replace geometric queries with image lookups



# Environment mapping

A.K.A. image-based lighting





Assume all incident light is from environment map (i.e. ignore all other objects in the scene!)

$$L_o(\mathbf{p}, \boldsymbol{\omega}_o) = \int_{H^2} f_r(\mathbf{p}, \boldsymbol{\omega}_i \rightarrow \boldsymbol{\omega}_o) L_i(\boldsymbol{\omega}_i) \cos(\theta_i) d\boldsymbol{\omega}_i$$



Easy case: perfect specular reflection





Another easy case: **diffuse surface**

$$\begin{aligned} L_o(\mathbf{p}, \boldsymbol{\omega}_o) &= f_r \int_{H^2} L_i(\boldsymbol{\omega}_i) \cos(\theta_i) d\boldsymbol{\omega}_i \\ &= f_r l_i(\mathbf{n}) \end{aligned}$$

Precompute  $l_i(\mathbf{n})$ : **irradiance environment map**







Ramamoorthi and Hanrahan 2001

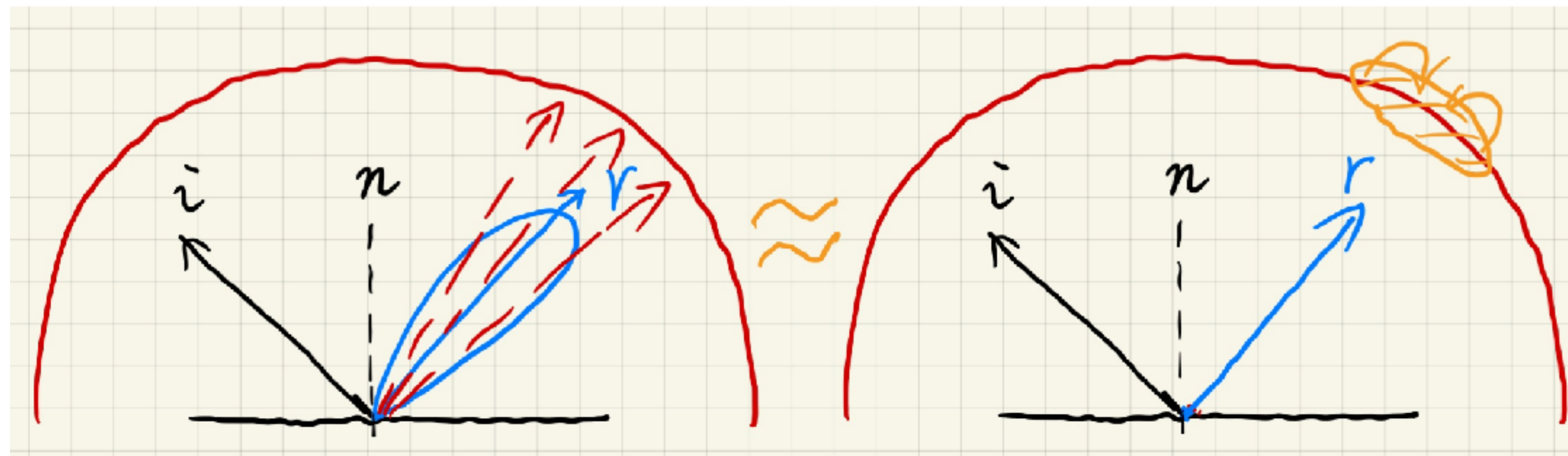


What about glossy surfaces? "Split sum approximation"

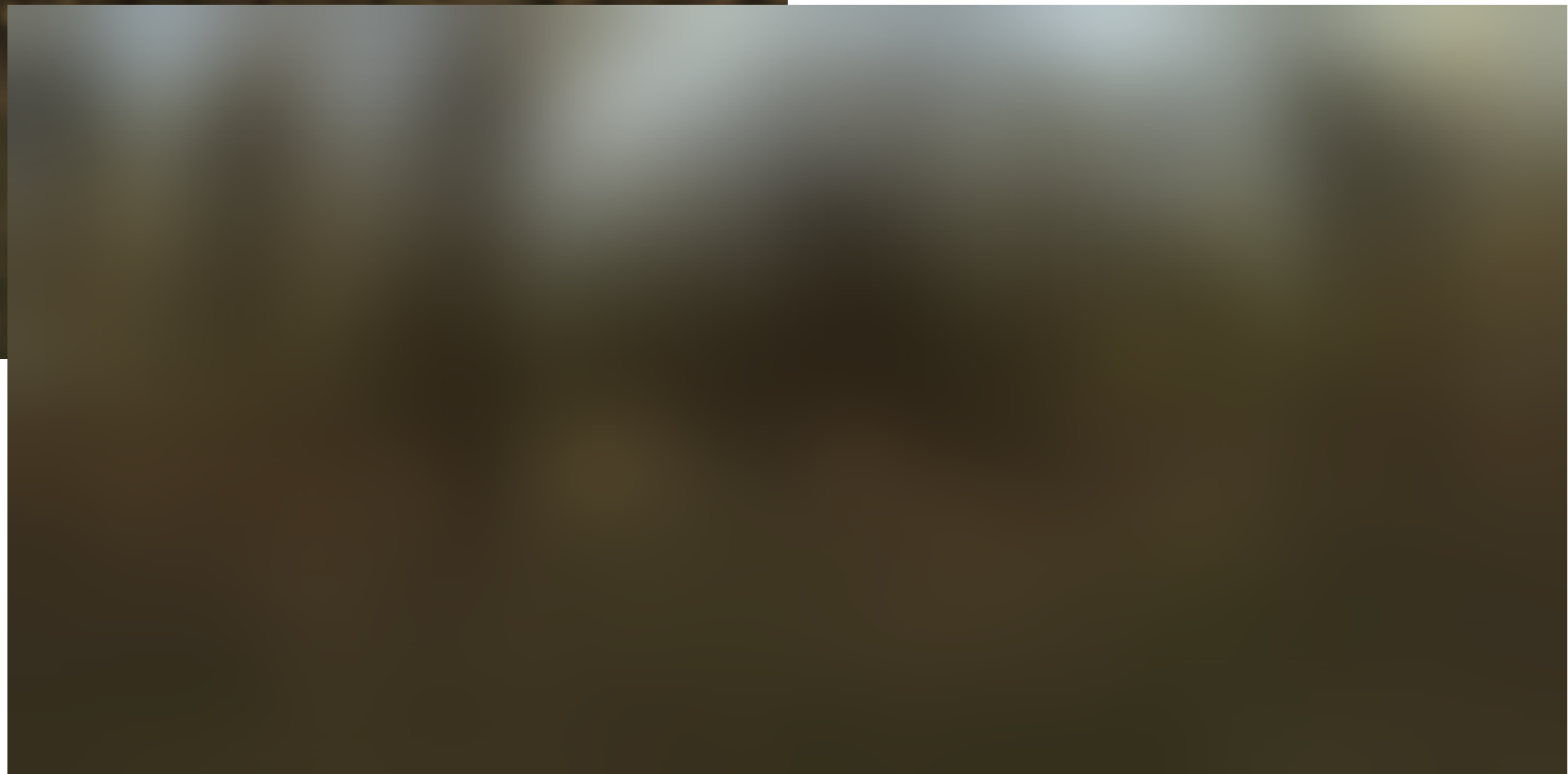
$$\int f(x)g(x) dx = \left( \frac{\int f(x)g(x) dx}{\int f(x) dx} \right) \cdot \int f(x) dx$$

$$L_o(\mathbf{p}, \boldsymbol{\omega}_o) = \int_{H^2} f_r(\mathbf{p}, \boldsymbol{\omega}_i \rightarrow \boldsymbol{\omega}_o) L_i(\mathbf{p}, \boldsymbol{\omega}_i) \cos(\theta_i) d\boldsymbol{\omega}_i$$

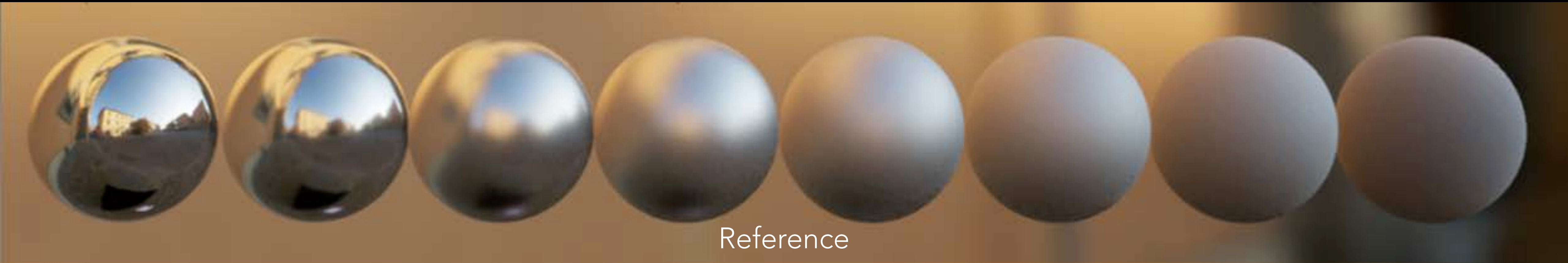
$$= [\text{weighted average of } L_i] \cdot \int_{H^2} f_r(\mathbf{p}, \boldsymbol{\omega}_i \rightarrow \boldsymbol{\omega}_o) \cos(\theta_i) d\boldsymbol{\omega}_i$$



Lingqi Yan



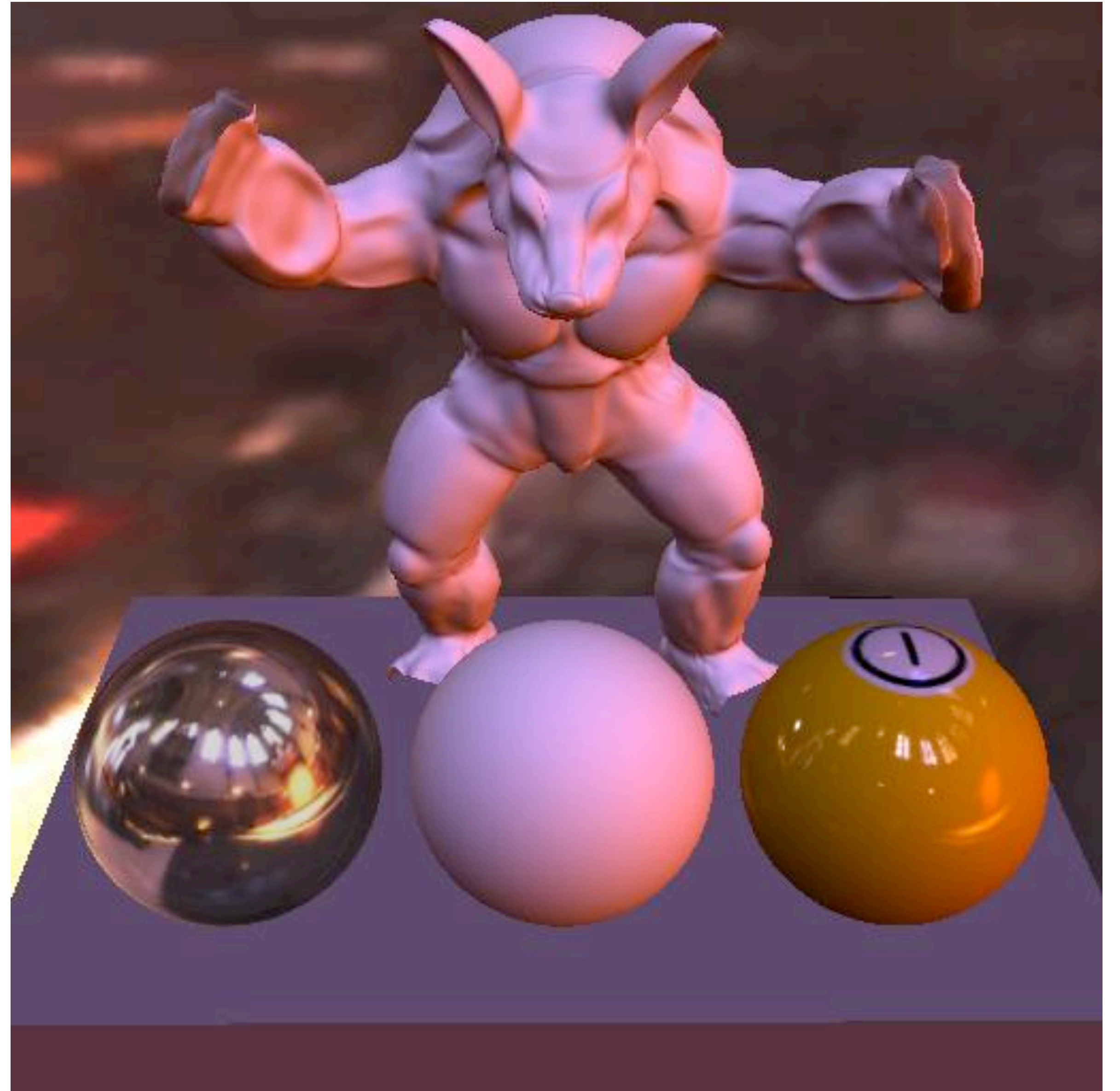




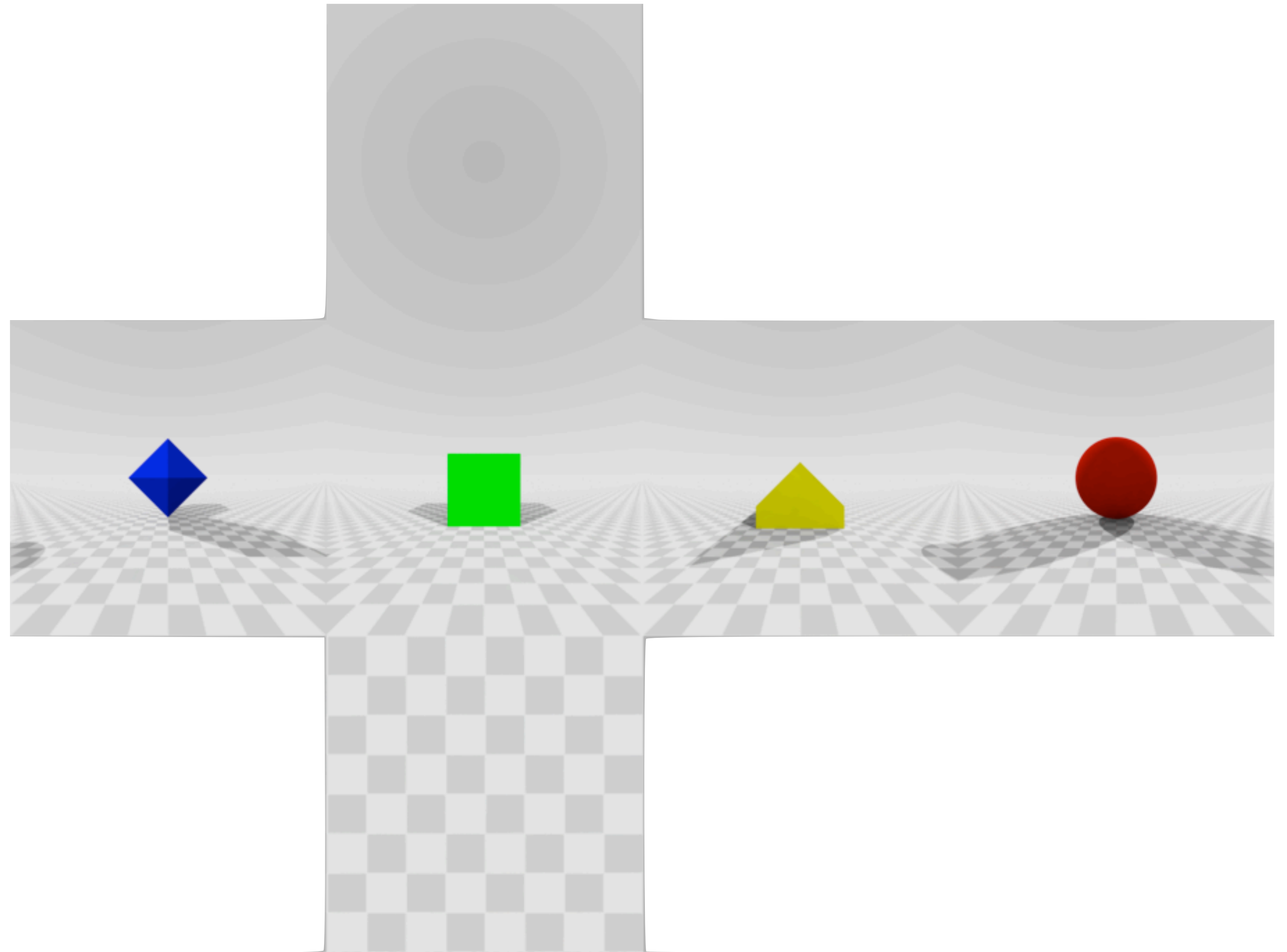
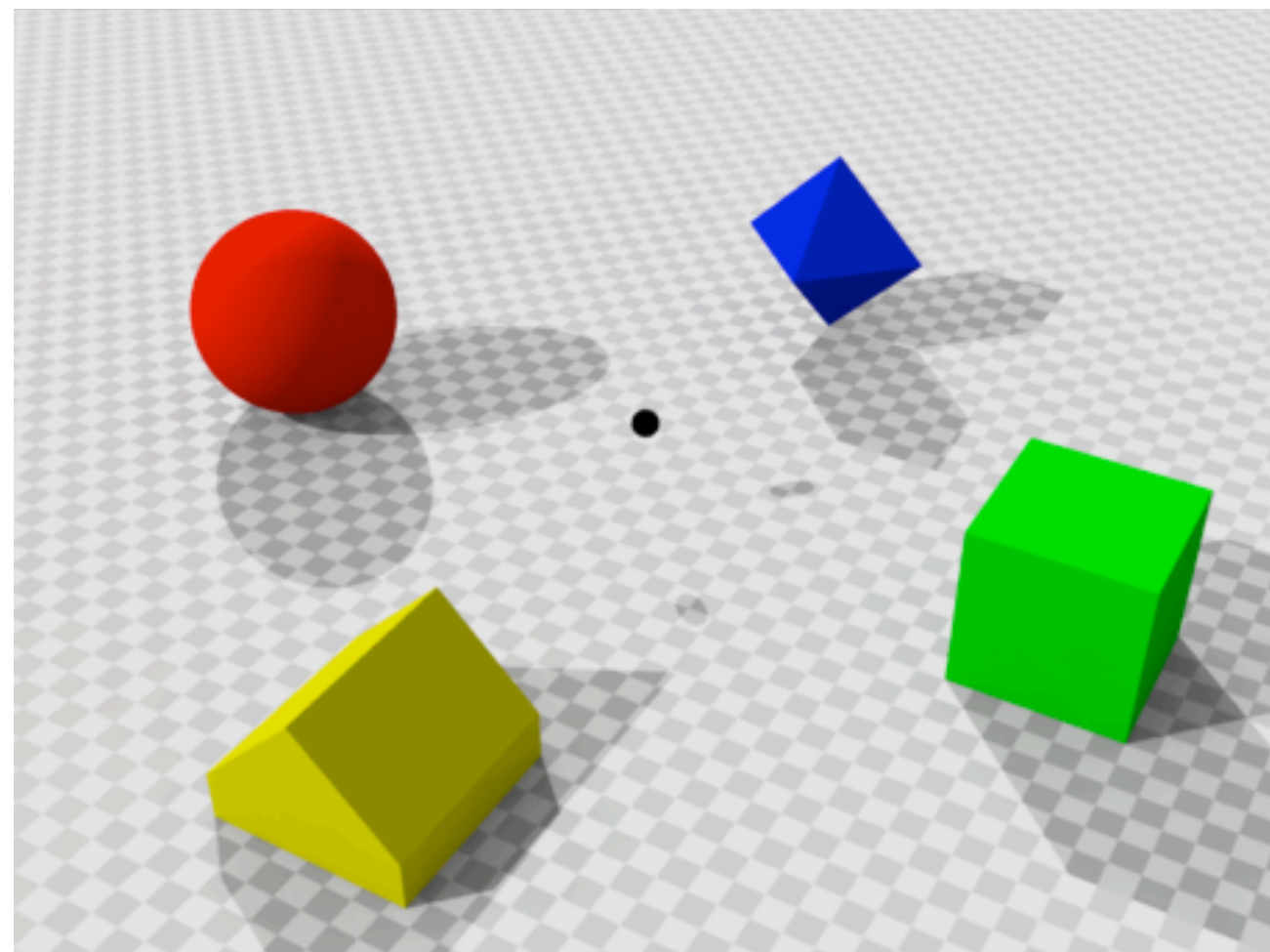


Problems with basic environment maps:

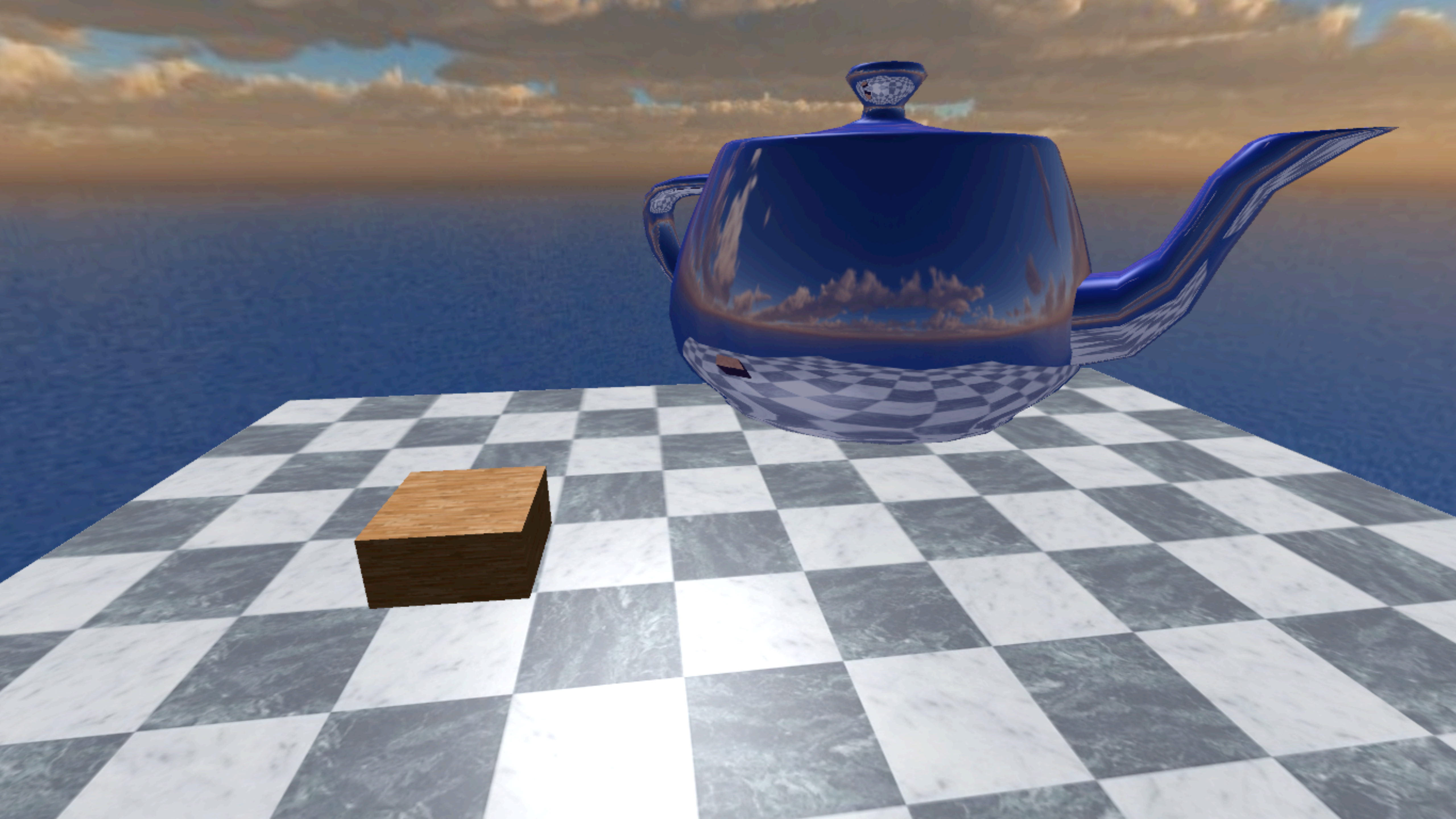
- No reflections of other objects
- No shadows



# Light probes









Reflection probes assume incident light is coming from infinitely far away...

