

Soft Rasterizer: A Differentiable Renderer for Image-based 3D Reasoning

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Introduction

- We're addressing the problem of getting 3D definitions from 2D images
- Problem in the pipeline is Rasterization and Z-buffering are non-differentiable
- Thus, we can't pass the gradients back to variables

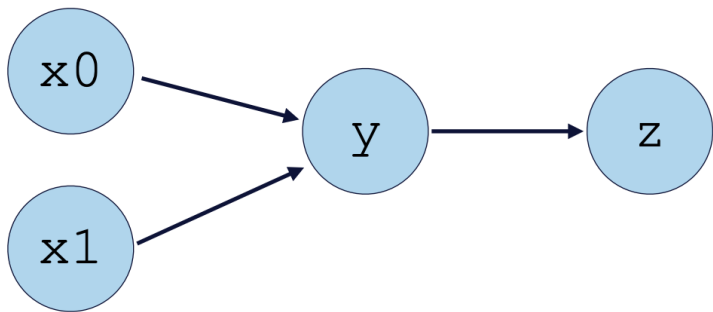
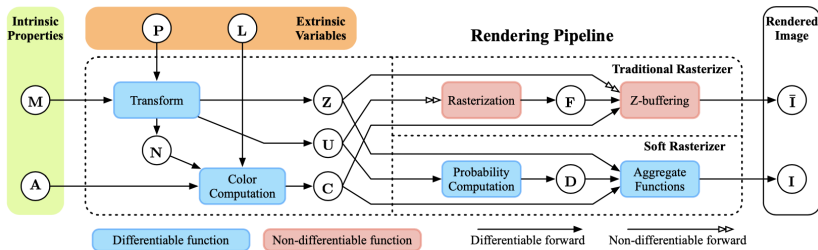


Figure: $\frac{dz}{dx_0} = \frac{dz}{dy} * \frac{dy}{dx_0}$

Proposed Idea : Change the rendering pipeline



- Variables : Mesh (M), Appearance (A), Camera (P), Light (L)
- Normals (N), Depths (Z), Image-space (U), Vertex colours (C)

Rasterization (XY discontinuity) and Z-buffering (Z discontinuity) aren't differentiable functions, hence we replace them with equivalent with differentiable functions "Probability Computation" and "Aggregation function"

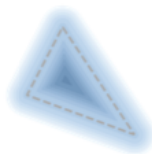
Probability Map

Define, probability map D_j for every triangle f_j and get the influence triangle f_j onto pixel p_i i.e every triangle has some influence on every pixel

D_j at pixel p_i is defined as follows :

$$D_j^i = \text{sigmoid}\left(\delta_j^i \cdot \frac{d^2(i, j)}{\sigma}\right)$$

where, $\text{sigmoid}(x) = \frac{1}{1+e^{-x}}$, $\delta_j^i = +1$ if $p_i \in f_j$ else -1
 $d(i, j)$ is closest distance from p_i to f_j 's edges, $\sigma > 0$ sharpness scalar



(a) ground truth (b) $\sigma = 0.003$ (c) $\sigma = 0.01$ (d) $\sigma = 0.03$

Aggregate Function

Color map C_j for every pixel p_i is defined using weighted average of barycentric coordinates for triangle f_j if inside else 0.

Aggregate function is a function of $\{D_j\}$, $\{C_j\}$ and depth $\{z_j\}$, function output at pixel i is given by,

$$I^i = A(\{D_j\}, \{C_j\}, \{z_j\}) = (\sum_j w_j^i C_j^i) + w_b^i C_b$$

where, $w_b^i + \sum_j w_j^i = 1$ and w_j^i is defined as

$$w_j^i = \frac{D_j^i * \exp^{-z_j^i/\gamma}}{\exp^{\epsilon/\gamma} + \sum_k D_k^i * \exp^{-z_k^i/\gamma}}$$

Higher weights are assigned to closer triangles, as γ is sharpness constant and ϵ is background color dependent constant

Every triangle is contributing to the color of all pixels

Rendered example



Standard rendering



Rendered
w/ larger γ



Rendered
w/ larger γ and σ

Comparison

- We can pass gradients from pixels to triangles now as shown in figure below - (Z-discontinuity solved)
- Screen space gradients now exists because of probability map of triangles - (XY-discontinuity solved)

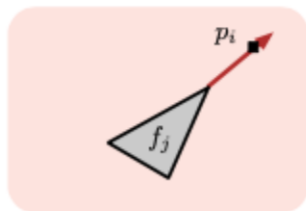
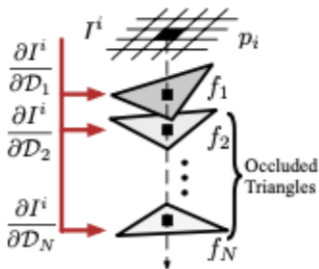
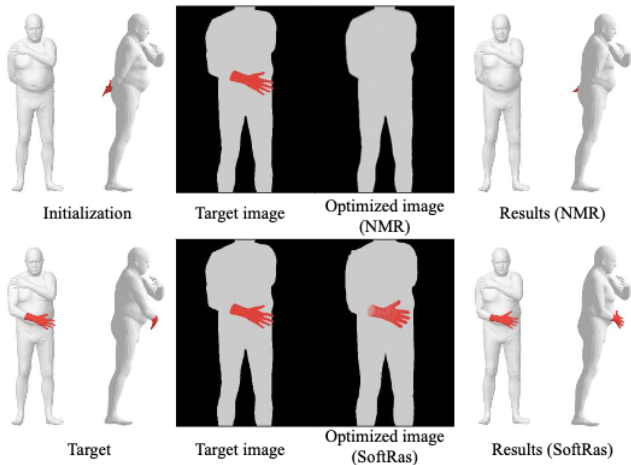


Image based shape fitting

- Occlusion Awareness : Gradients must pass through



Mesh Reconstruction

Minimise $L = L_s + \lambda L_c + \mu L_g$ where

- L_s is silhouette loss, $1 - \frac{\|I_s \otimes \hat{I}_s\|_1}{\|I_s \oplus \hat{I}_s - I_s \otimes \hat{I}_s\|_1}$, silhouette is binary image
- L_c is coloured loss, $\|I_c - \hat{I}_c\|_1$
- L_g is geomteric loss (Laplacian of shape and colour)

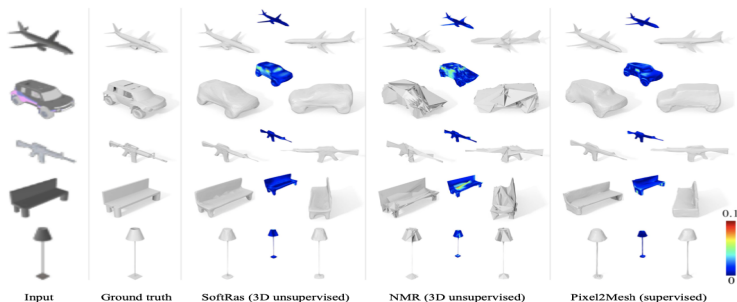


Figure: 64 input images, $\lambda = 1$, $\mu = 10^{-3}$

- ① Change of rendering pipeline by replacing rasterization and z-buffering with probability maps and Aggregator function to form **Soft Rasterizer**
- ② This makes the functions differentiable thus differentiable rendering is possible
- ③ Performance-comparison of new pipeline with other differentiable rendering algorithms with applications in
 - Shape fitting
 - Mesh reconstruction

More details can be found in : *Soft Rasterizer: A Differentiable Renderer for Image-based 3D Reasoning*

Thank You !!!