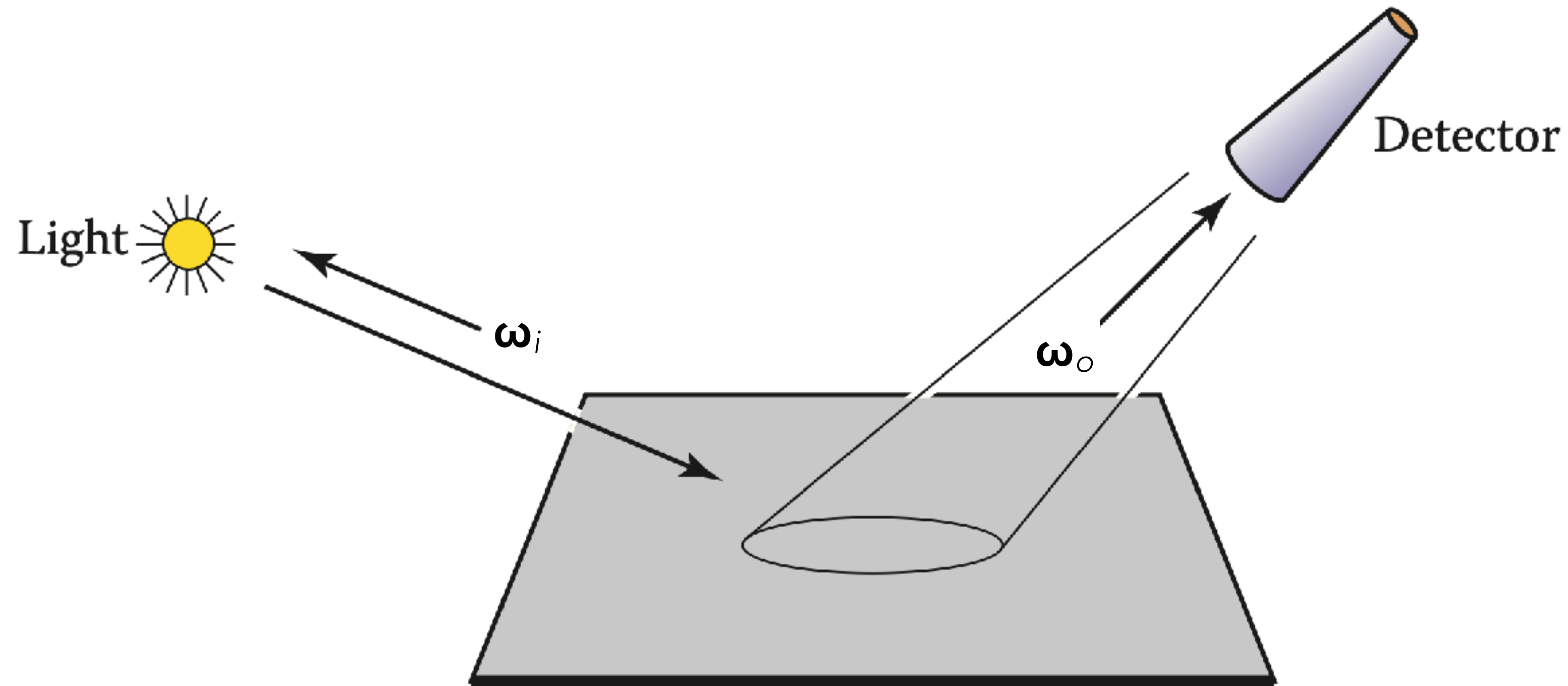


A 3D rendered birthday cake with pink frosting, green ice cream scoops, and pink candles. The cake is decorated with pink frosting, green ice cream scoops, and pink candles. The background is a plain grey color.

COL781: Computer Graphics

21. Material Appearance

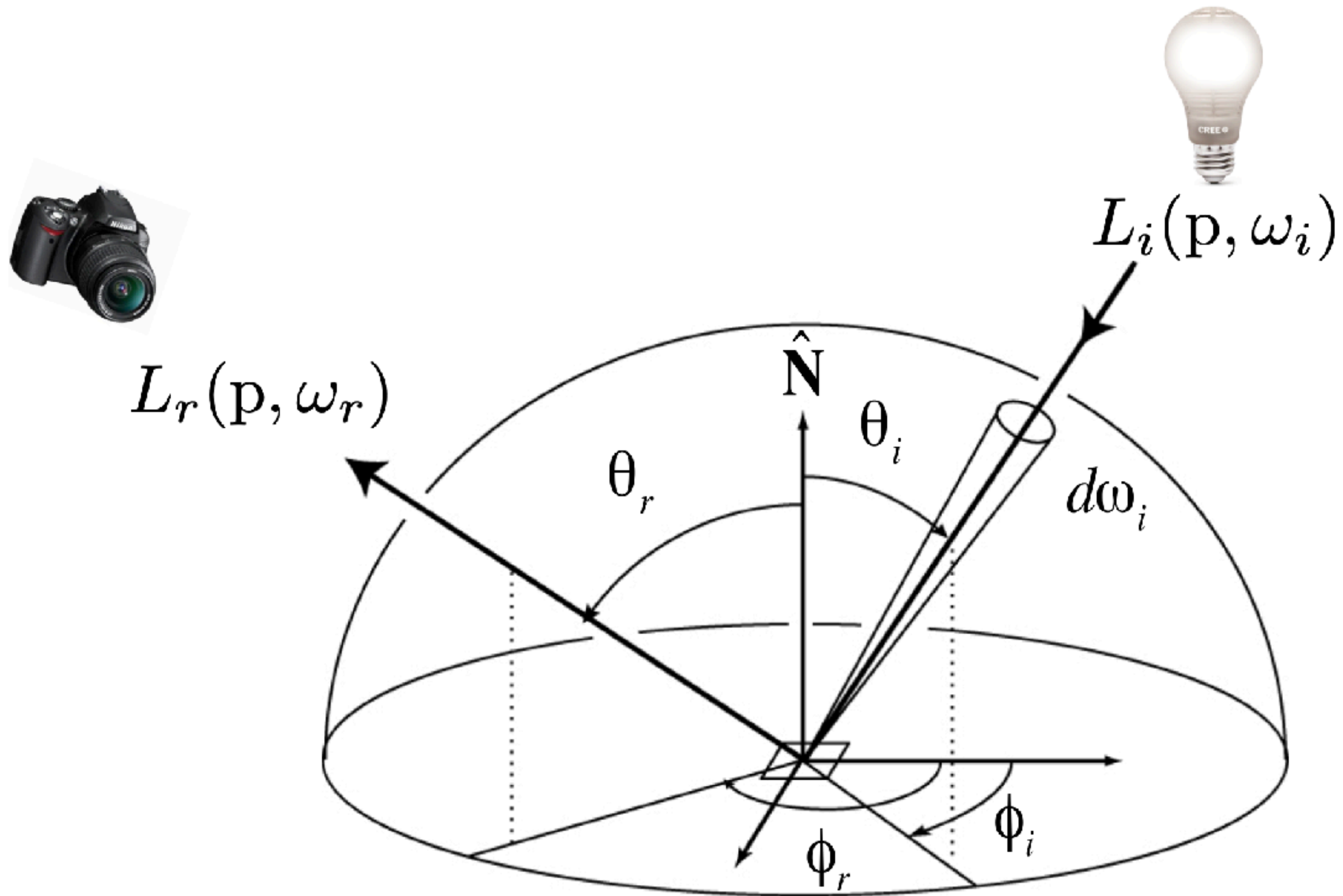
Recap: the BRDF



Bidirectional
Reflectance
Distribution
Function

Fundamentals of
Computer Graphics

$$f_r(\omega_i \rightarrow \omega_o) = L_o(\mathbf{x}, \omega_o) / E(\mathbf{x})$$



$$L_r(\mathbf{x}, \omega_r) = \int_{H^2} f_r(\omega_i \rightarrow \omega_r) L_i(\mathbf{x}, \omega_i) \cos(\theta_i) d\omega_i$$



Diffuse



Plastic



Red semi-gloss paint



Ford "Mystic Lacquer" paint



Mirror



Gold

Lambertian (diffuse) material

Simplest possible model: BRDF is a constant!

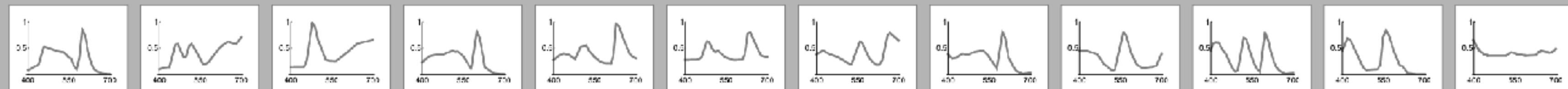
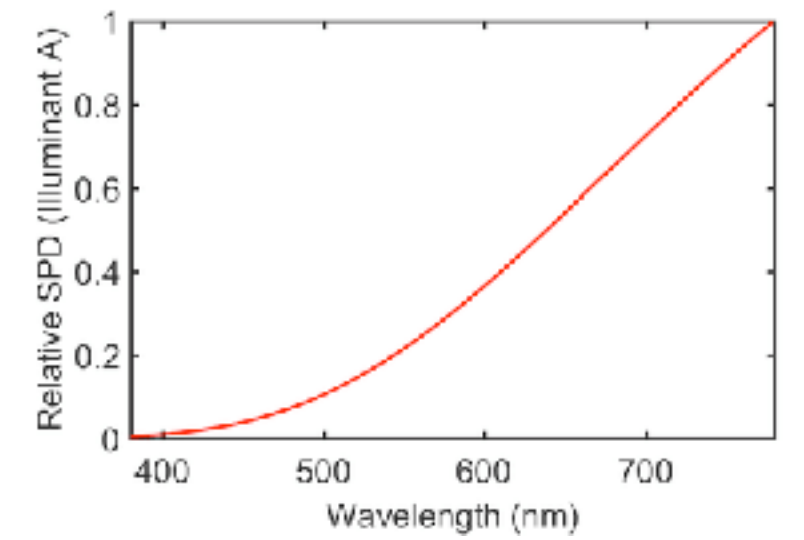
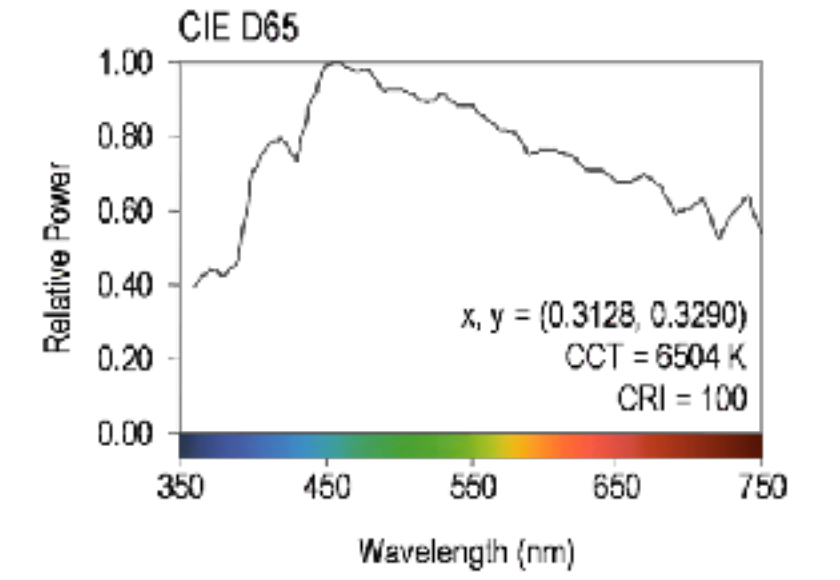
$$\begin{aligned} L_o(\omega_o) &= \int_{H^2} f_r L_i(\omega_i) \cos(\theta_i) d\omega_i \\ &= f_r E_i \end{aligned}$$

To conserve energy, $f_r = \rho/\pi$ where **albedo** ρ is ≤ 1

Why? For constant radiance L , total flux density = $L \pi$

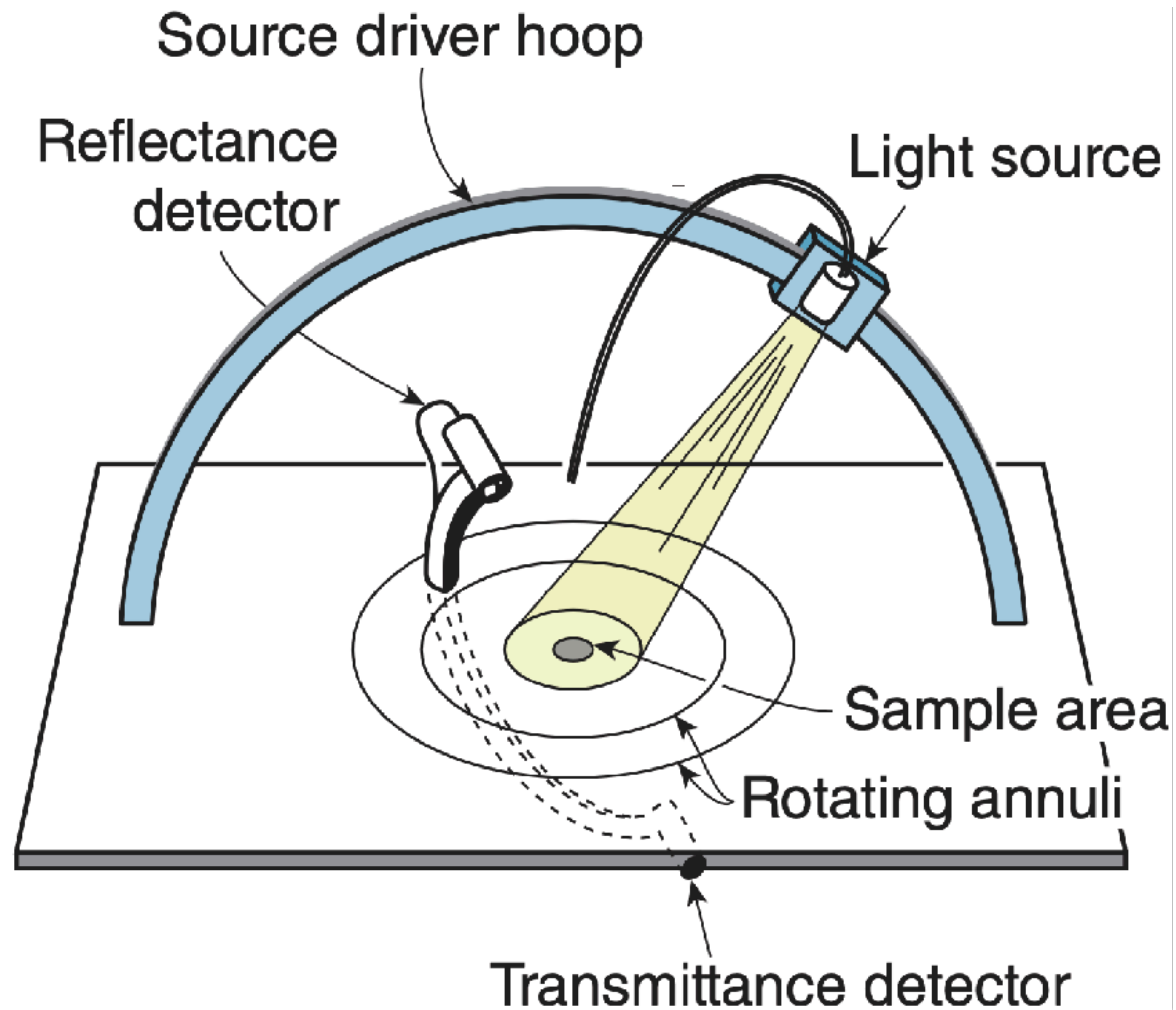


In principle, we should specify the **spectral** albedo...



Andrea Weidlich

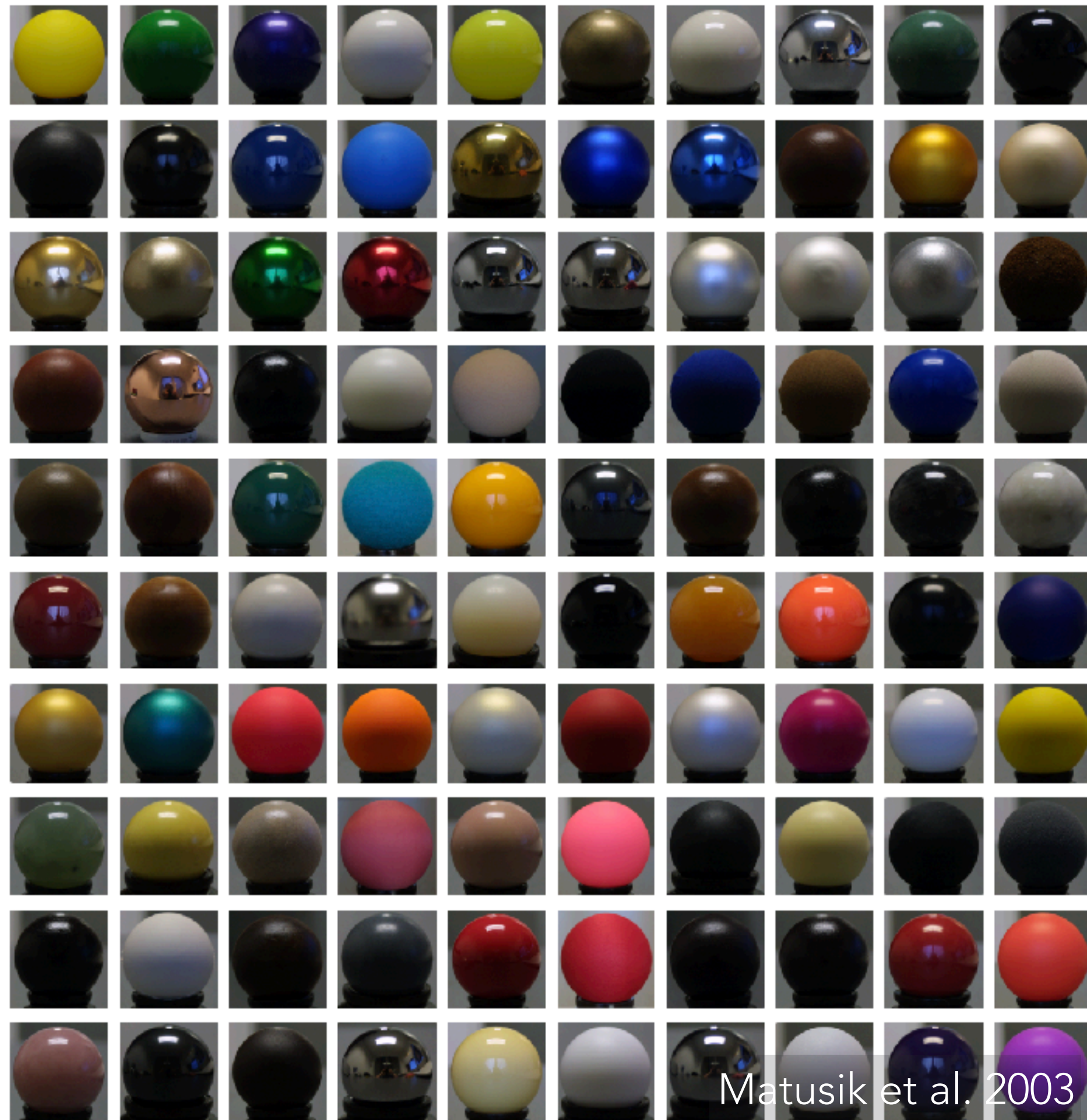
BRDF acquisition: Gonioreflectometer



Matusik et al.'s acquisition setup for isotropic BRDFs



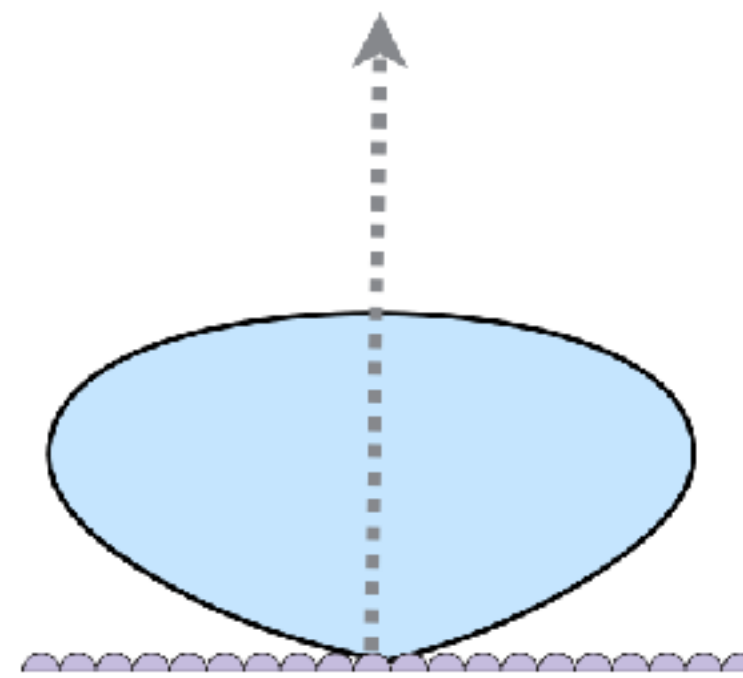
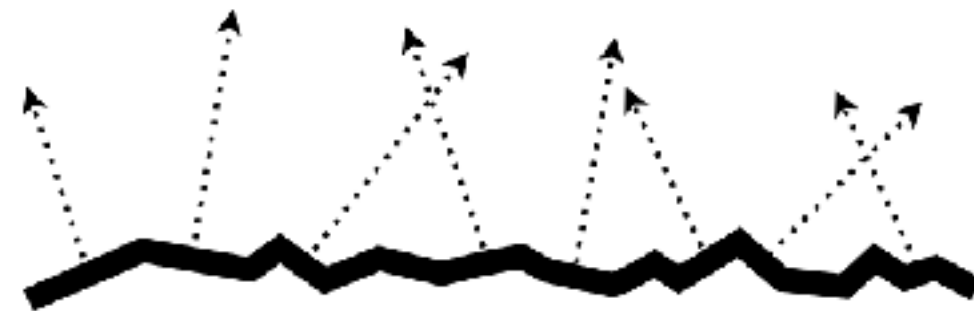
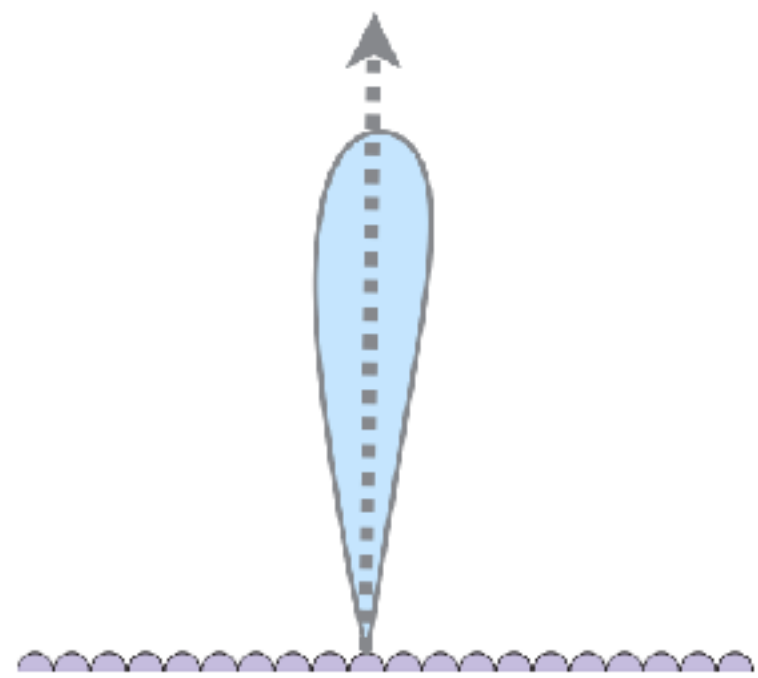
MERL BRDF database

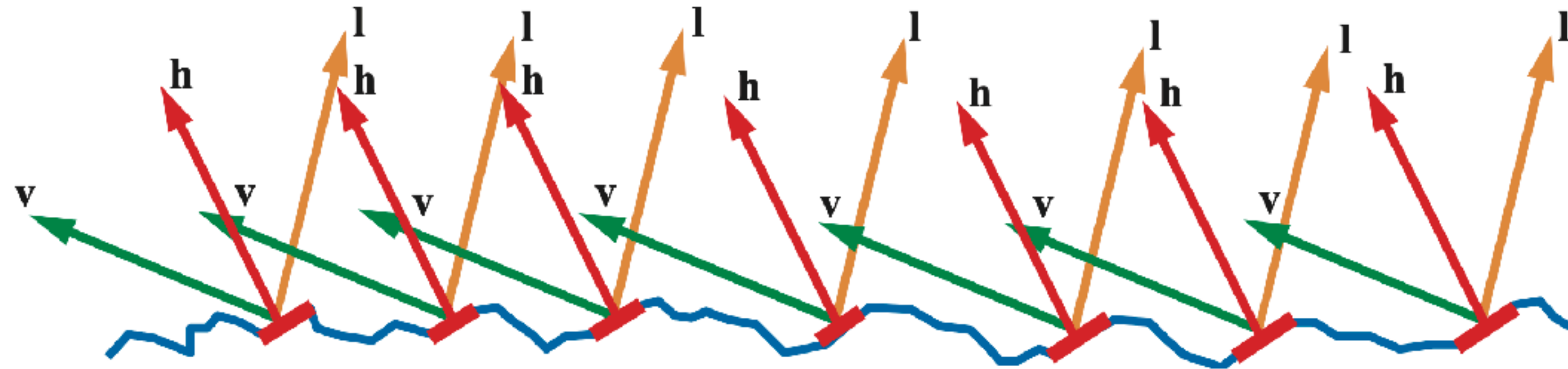


Microfacet models

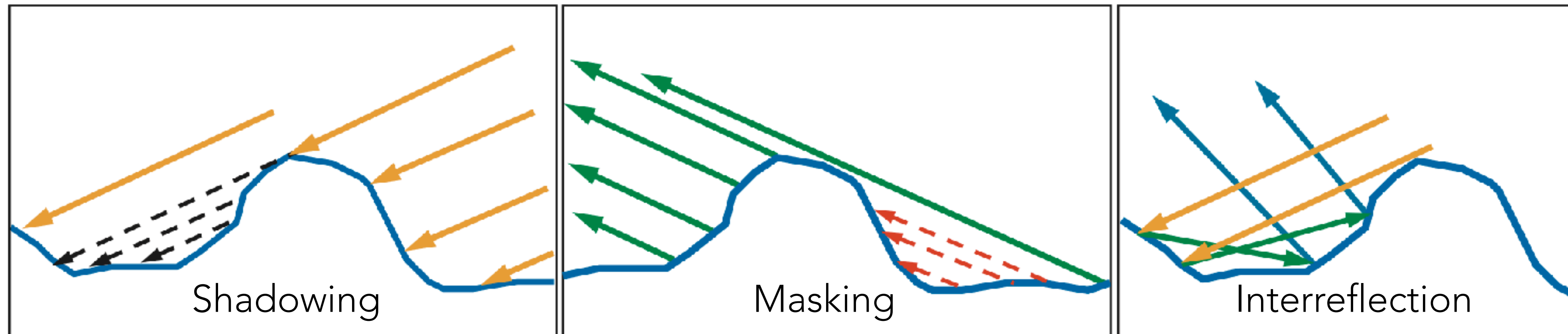
Assume rough surface is actually perfectly specular but bumpy at microscale

Made of small flat patches ("microfacets") with **normal distribution function** $D(\mathbf{h})$





$f_r(\ell \rightarrow \mathbf{v}) = D(\mathbf{h})$? Not quite...

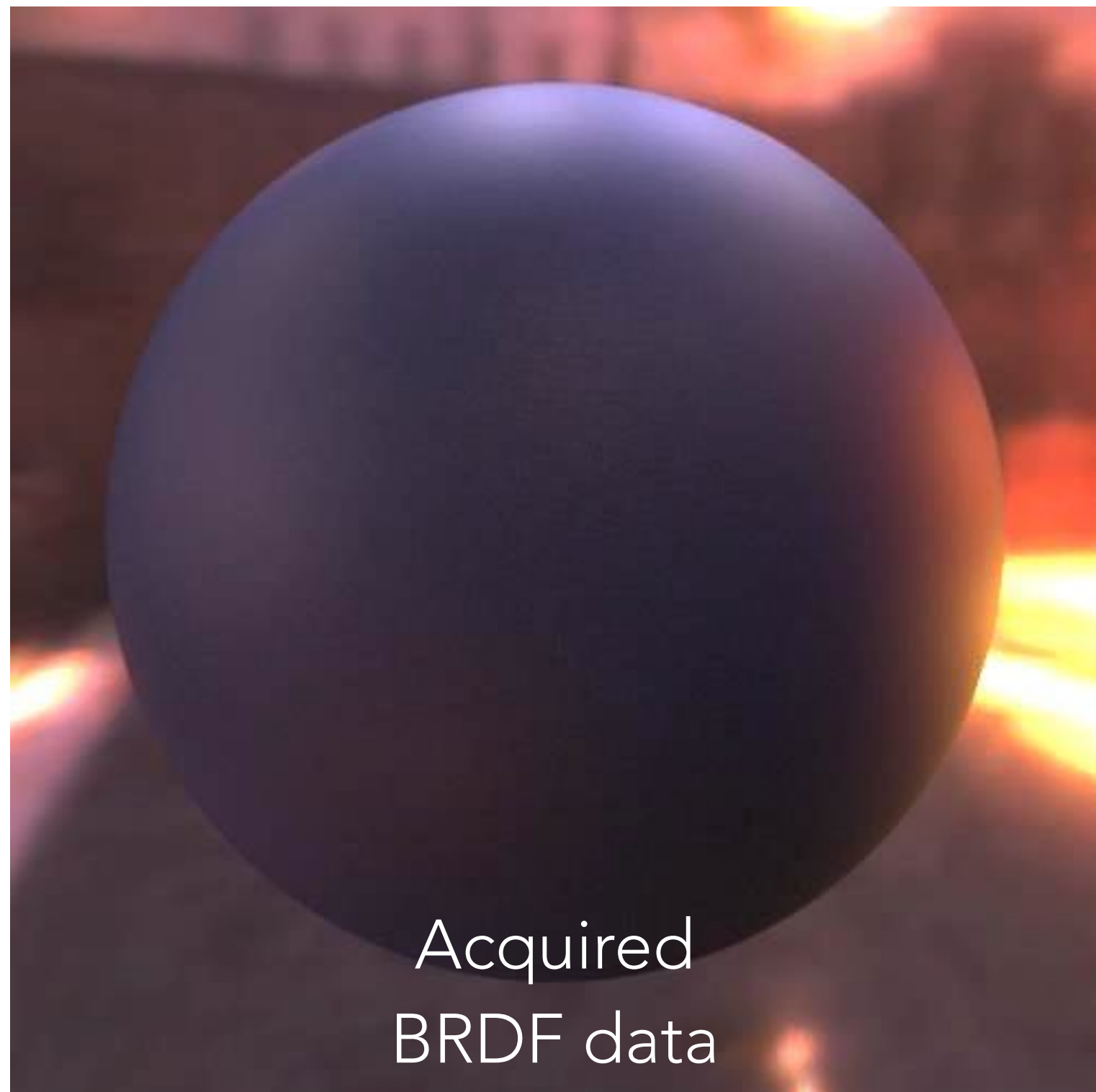


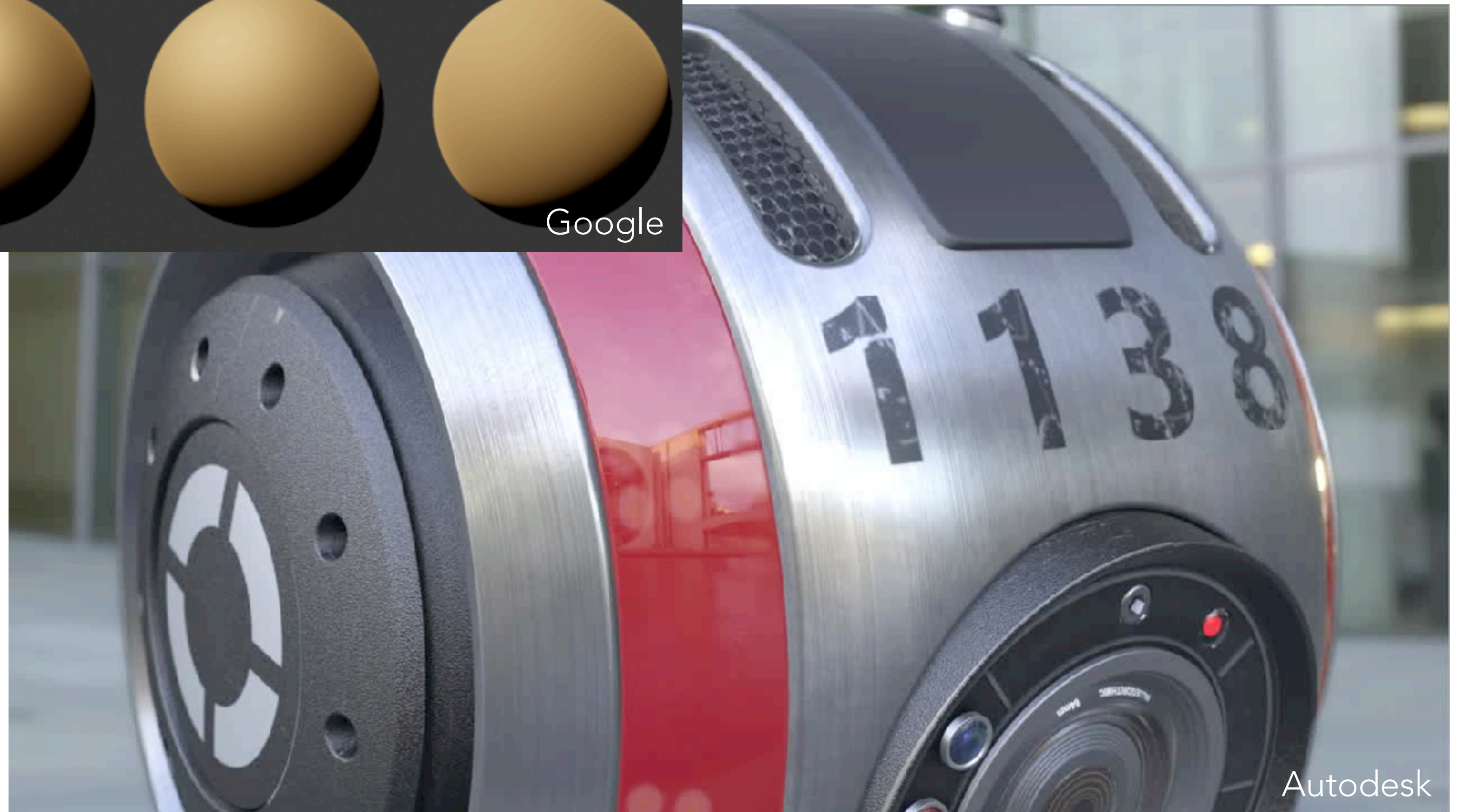
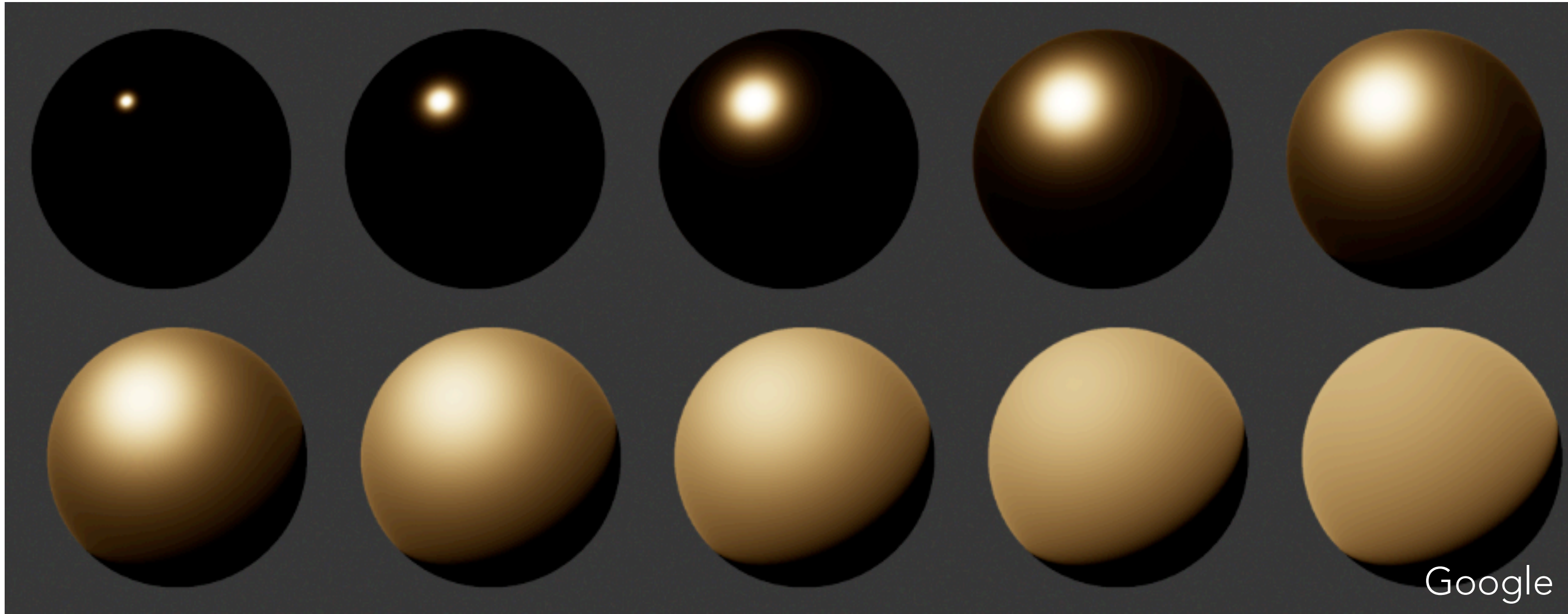
$$f_r(\ell \rightarrow \mathbf{v}) = \frac{F(\mathbf{l}, \mathbf{v})G(\mathbf{l}, \mathbf{v}, \mathbf{h})D(\mathbf{h})}{4(\mathbf{n} \cdot \mathbf{l})(\mathbf{n} \cdot \mathbf{v})}$$

$$f_r(\boldsymbol{\ell} \rightarrow \mathbf{v}) = \frac{F(\mathbf{l}, \mathbf{v})G(\mathbf{l}, \mathbf{v}, \mathbf{h})D(\mathbf{h})}{4(\mathbf{n} \cdot \mathbf{l})(\mathbf{n} \cdot \mathbf{v})}$$

- $F(\boldsymbol{\ell}, \mathbf{v}) \leq 1$: **Fresnel term**
 - To be discussed
- $G(\boldsymbol{\ell}, \mathbf{v}, \mathbf{h}) \leq 1$: **Geometry term**
 - Probability that microfacet with normal \mathbf{h} is visible from both $\boldsymbol{\ell}$ and \mathbf{v}
 - Accounts for shadowing and masking (interreflections ignored)
- $D(\mathbf{h})$: **Normal distribution function**

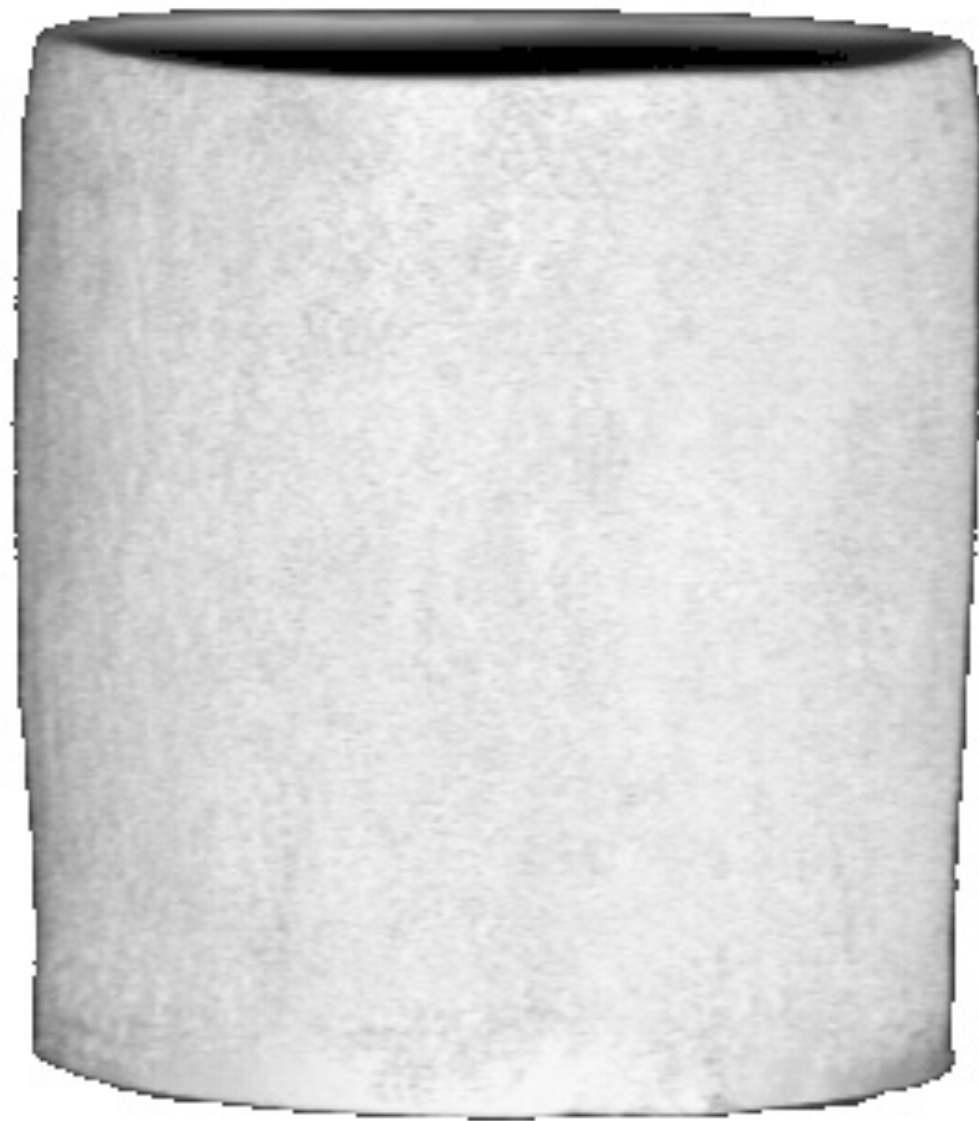
All these terms have various analytical models...



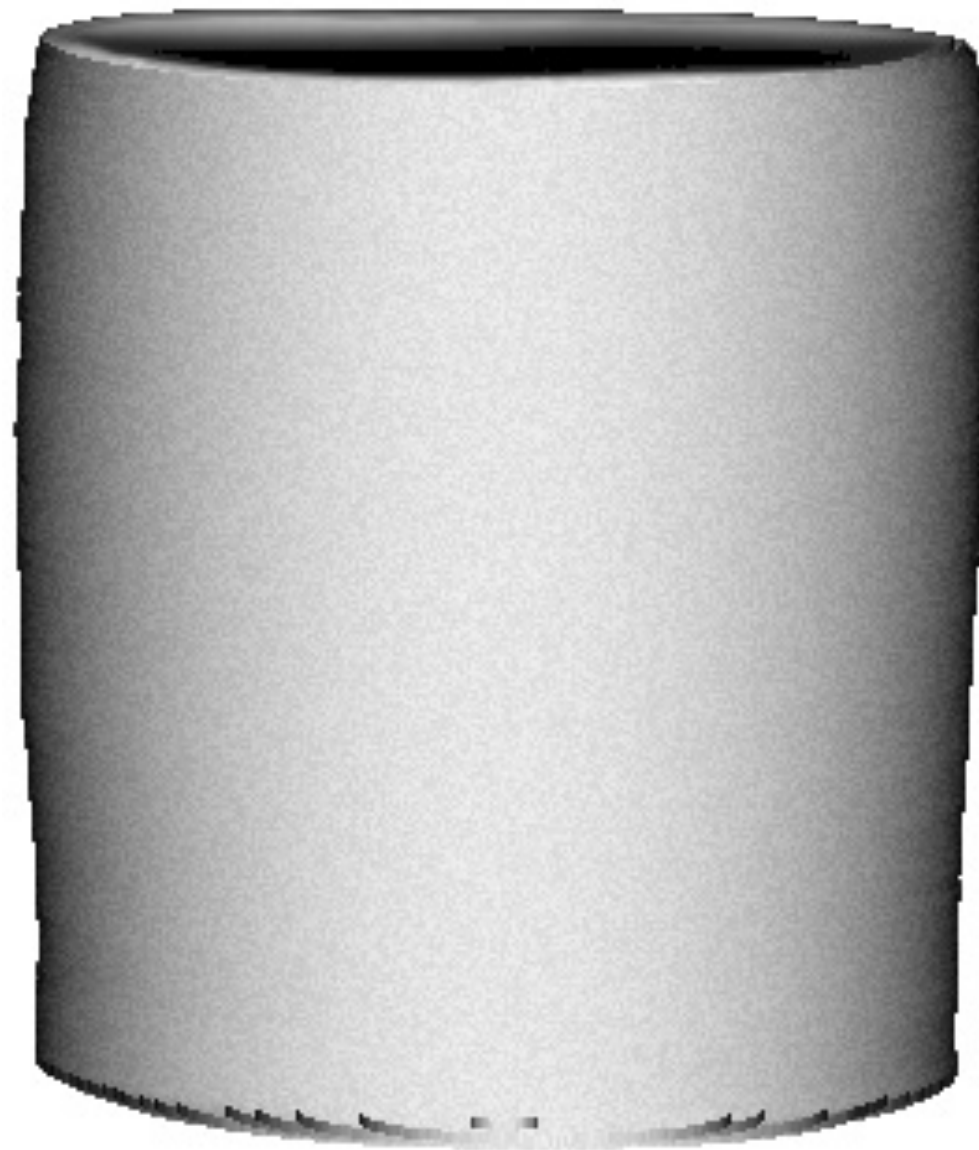


What if the microfacets are diffuse instead of specular?

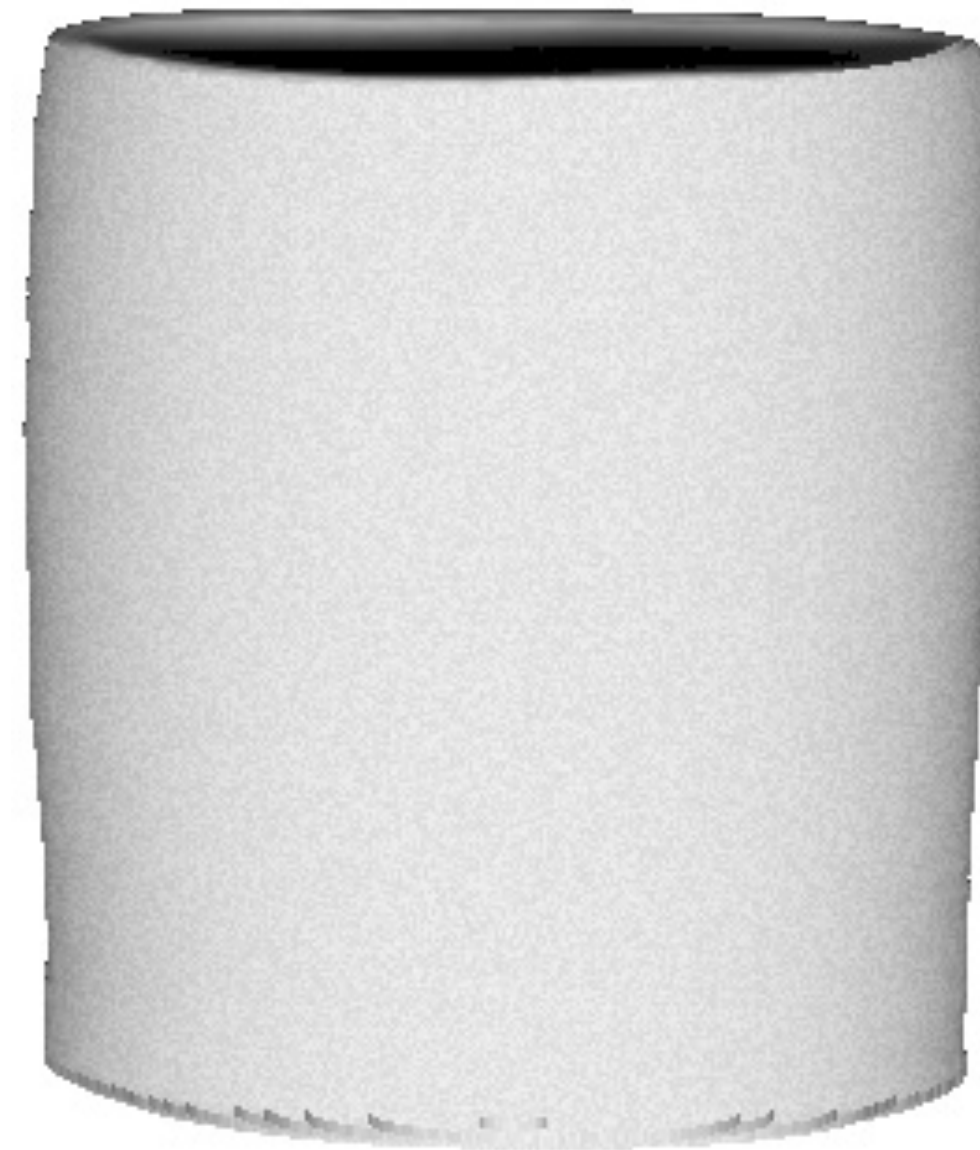
Oren-Nayar model for rough diffuse surfaces



Photograph



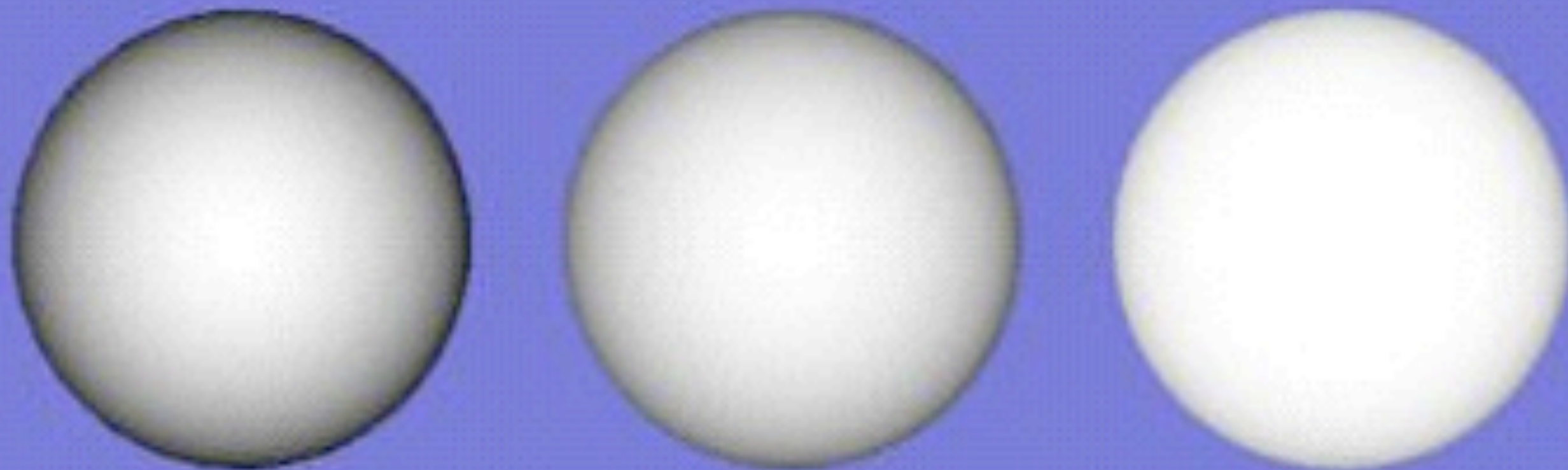
Lambertian



Oren-Nayar

Roughness \longrightarrow

Lambertian

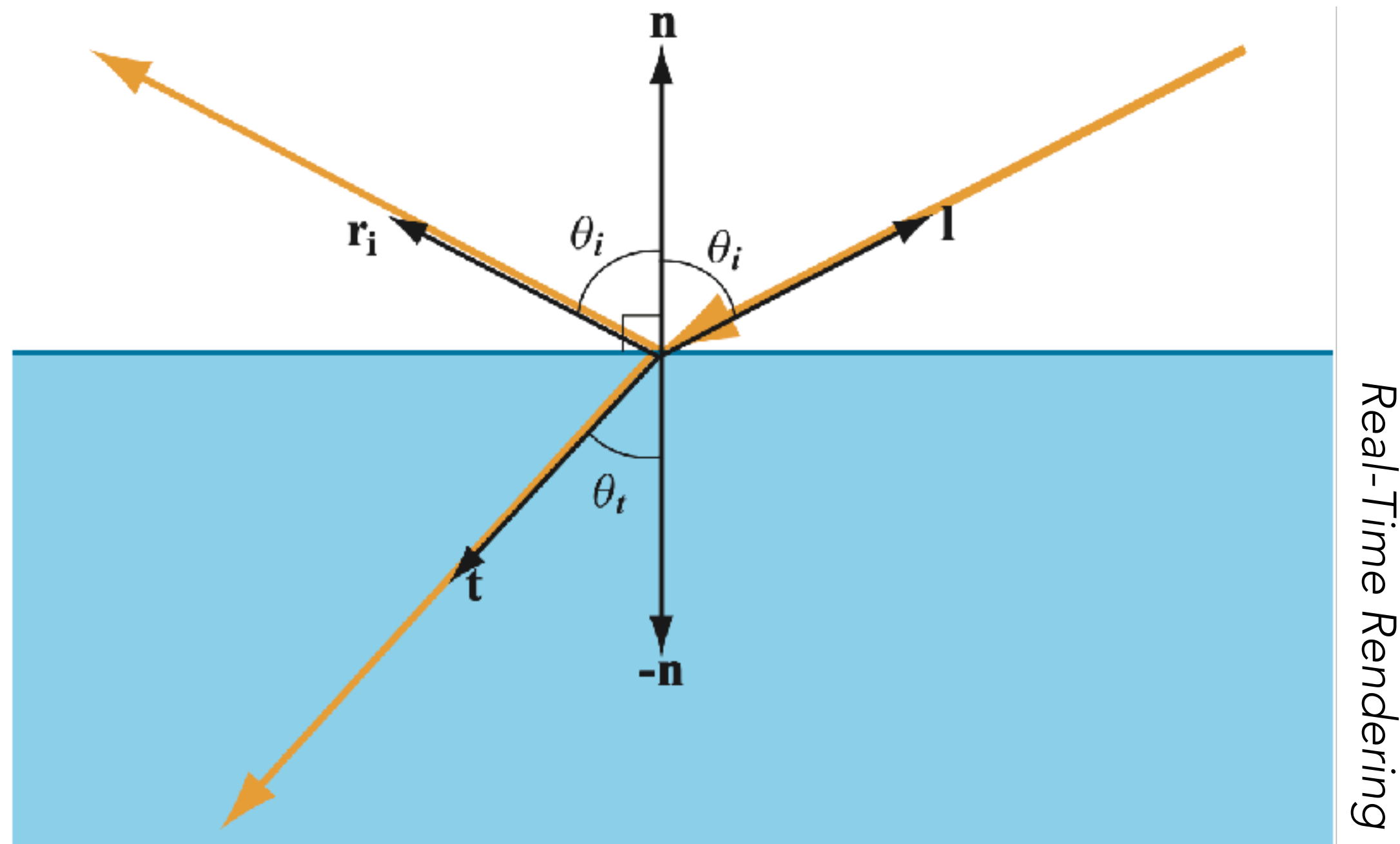


Rendered Spheres



Image of Full Moon

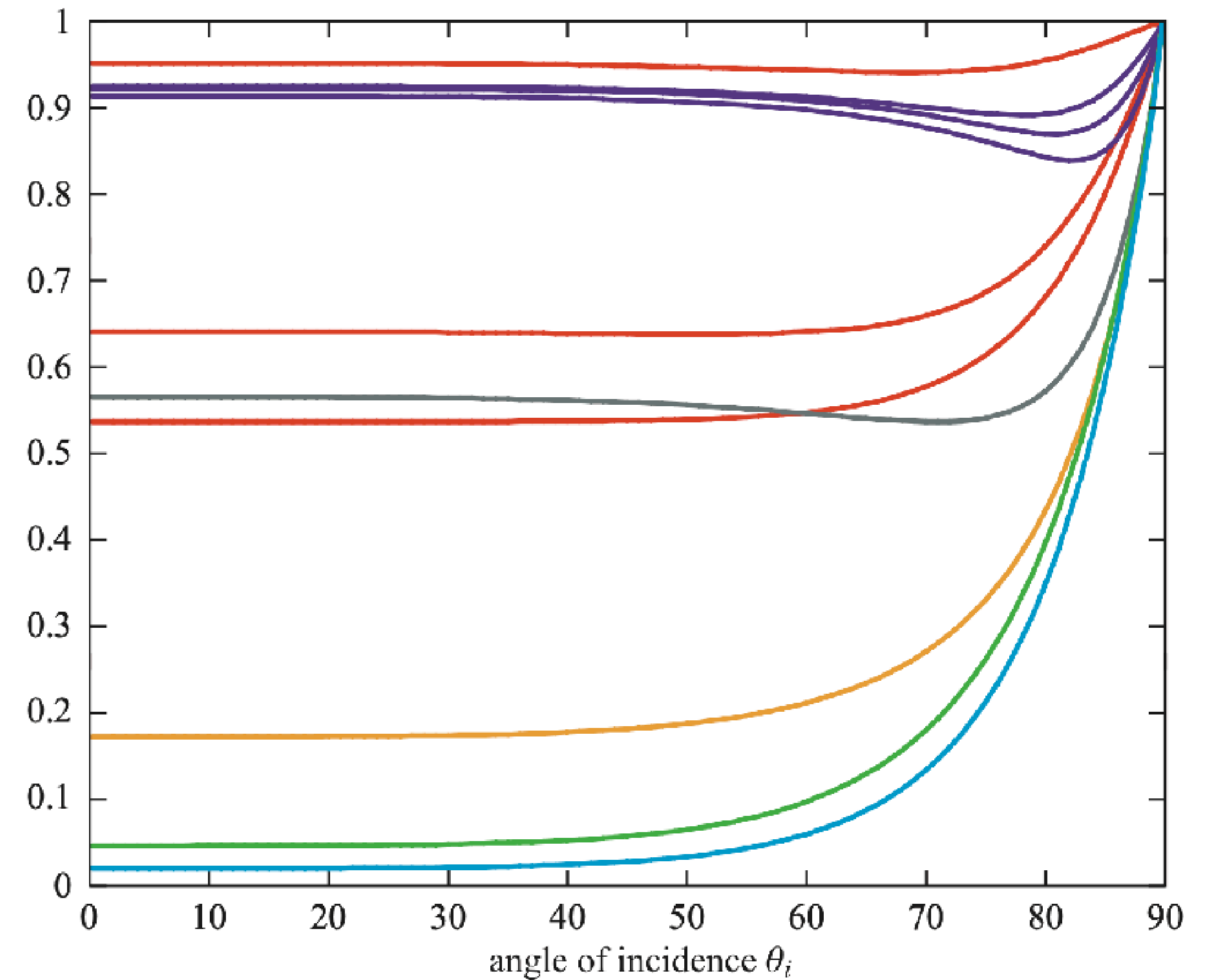
Fresnel reflectance



Real-Time Rendering

Schlick's approximation:

$$F(\mathbf{l}, \mathbf{n}) = F_0 + (1 - F_0)(1 - (\mathbf{l} \cdot \mathbf{n}))^5$$



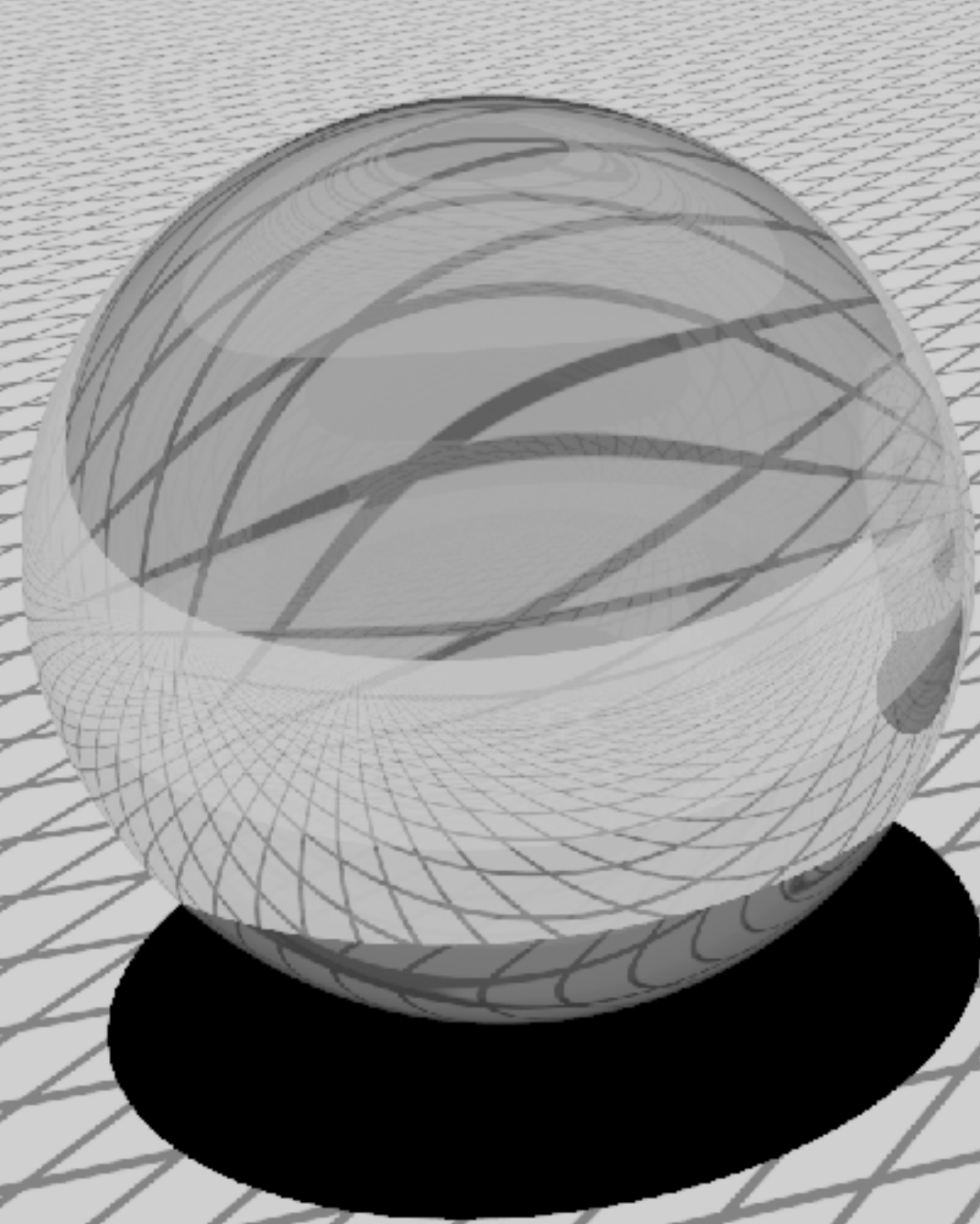
Real-Time Rendering

Legend: copper, aluminum, iron, diamond, glass, water

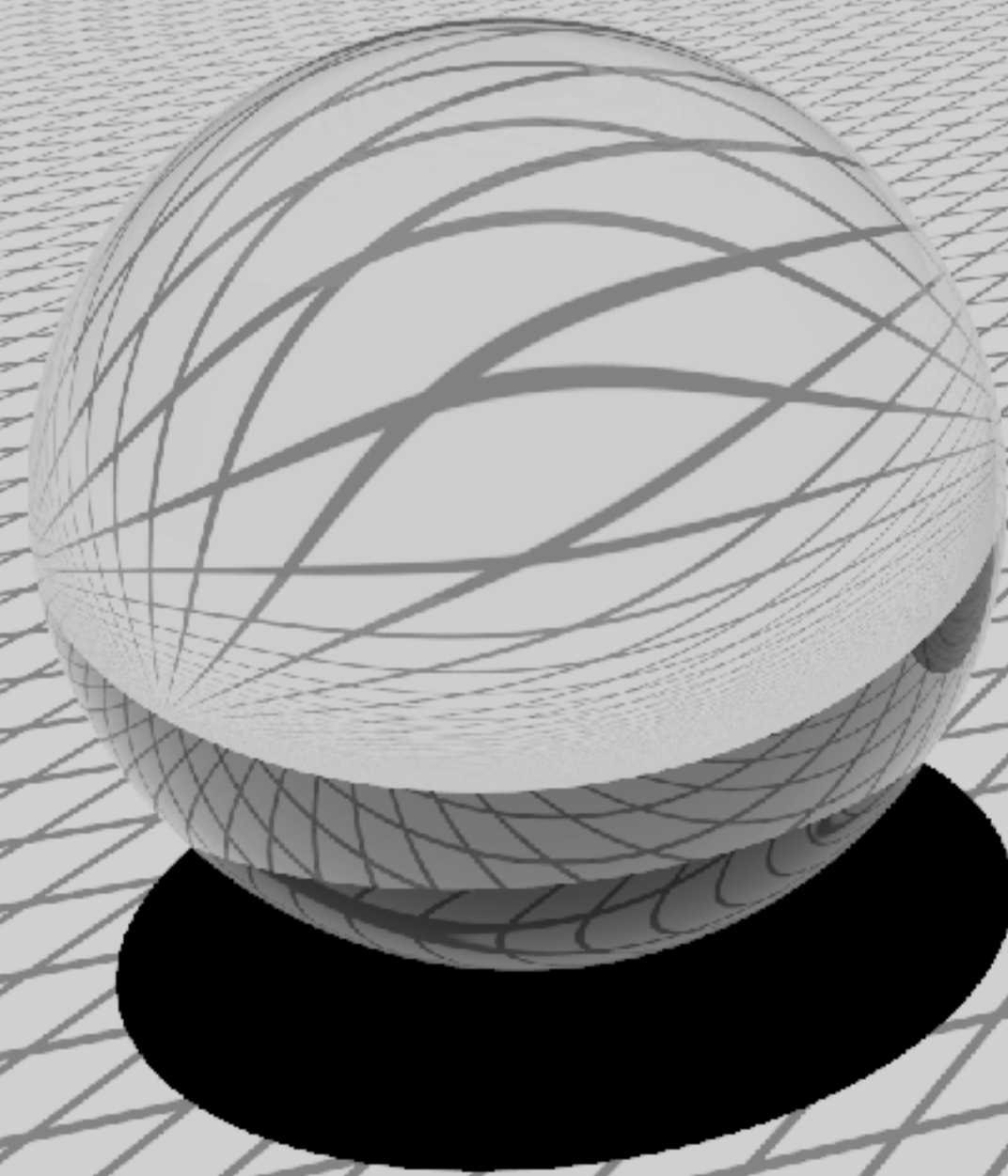
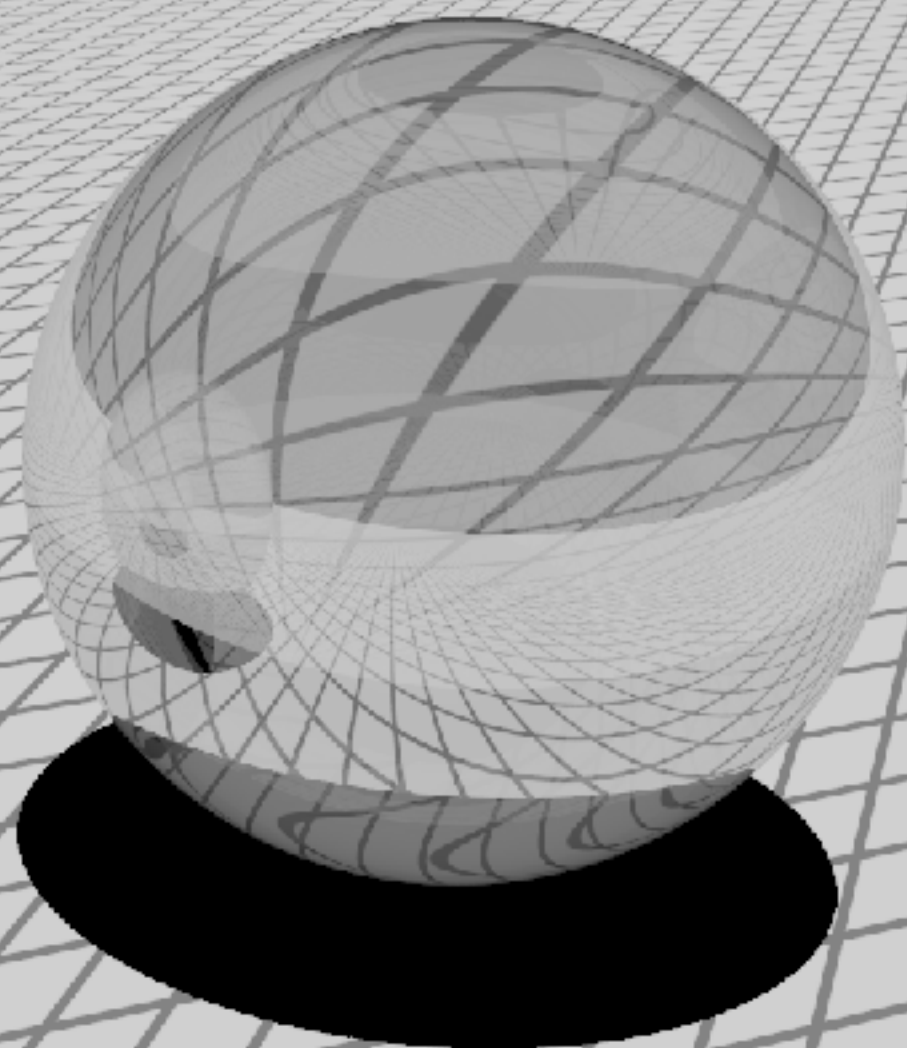




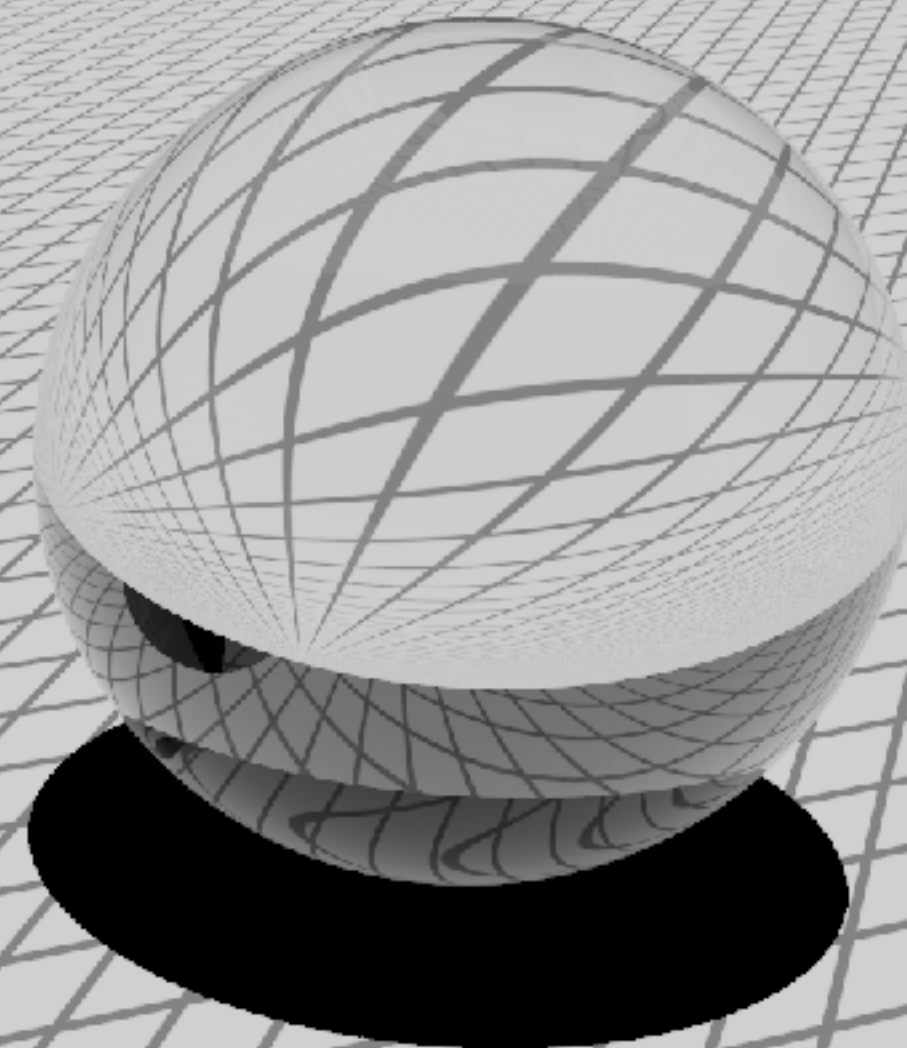
Lafortune et al. 1997

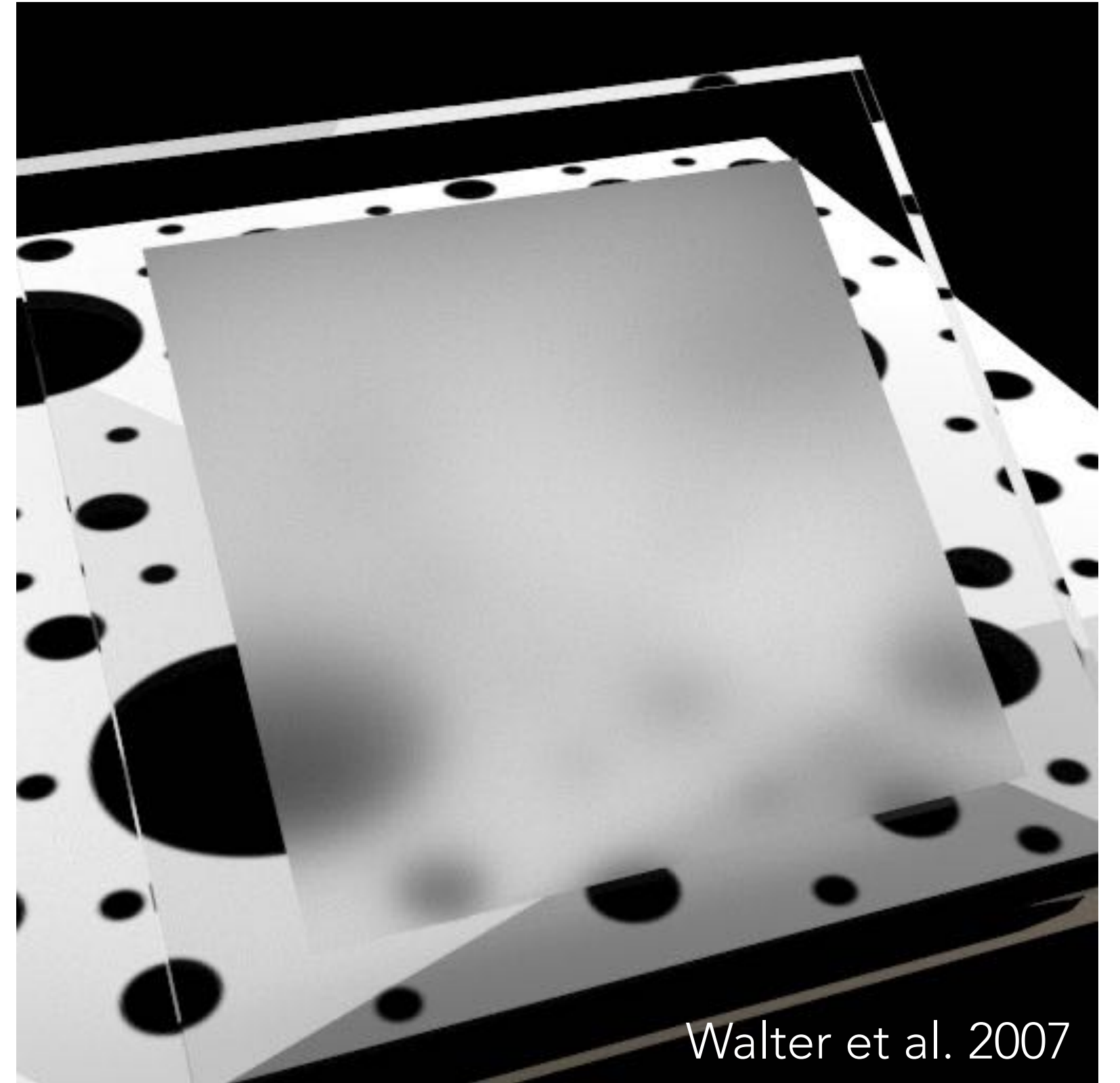
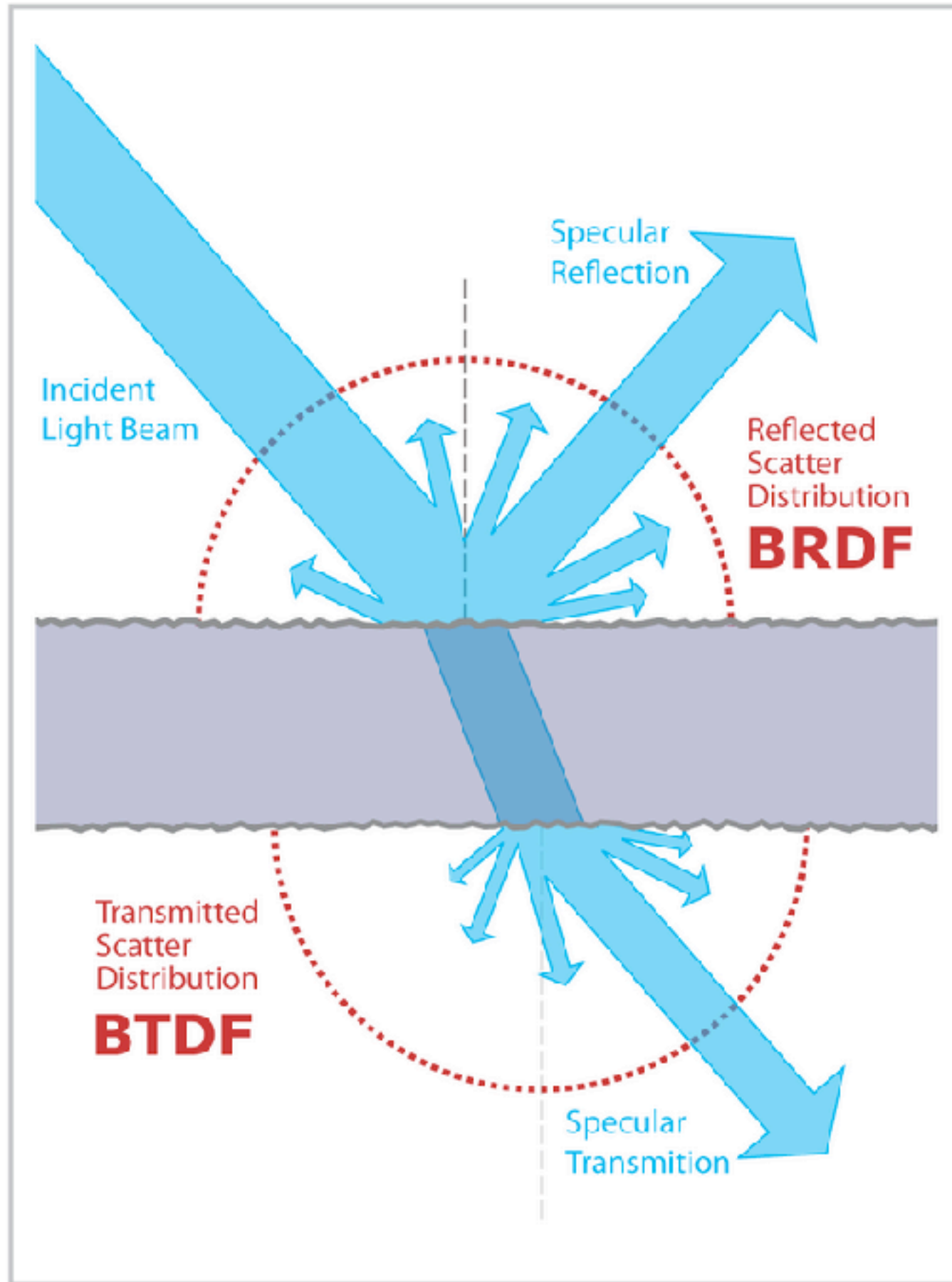


Without Fresnel



With Fresnel





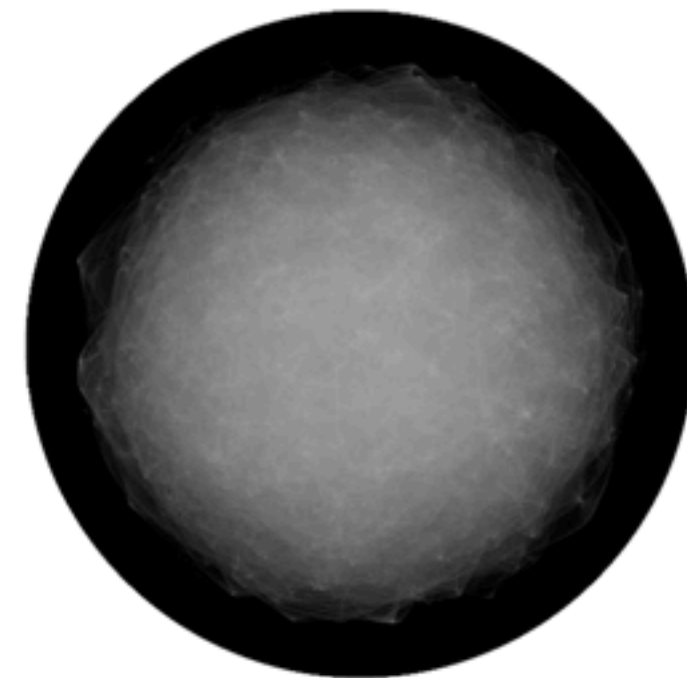
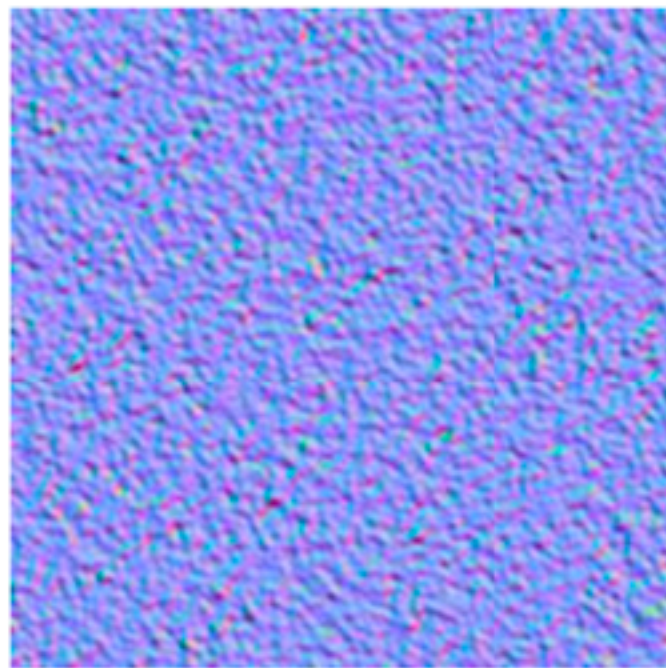
Quick survey of more complicated materials

Anisotropic roughness

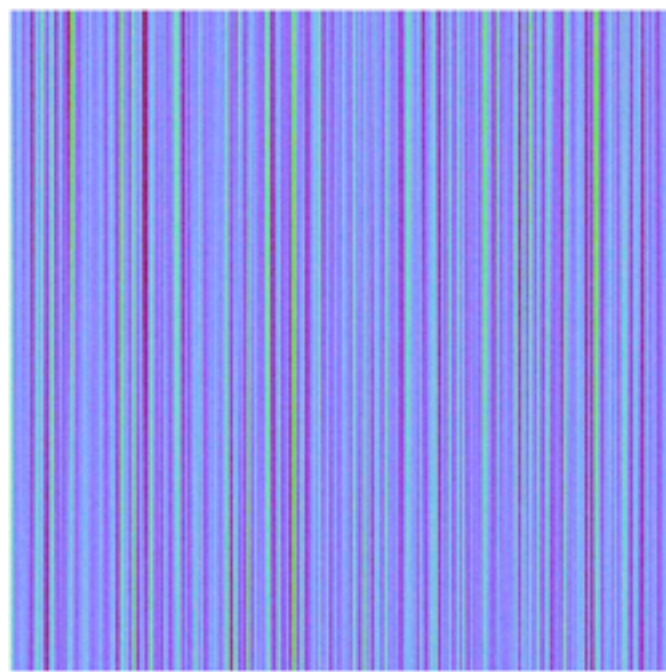
NDF is anisotropic due to oriented microstructure



Isotropic

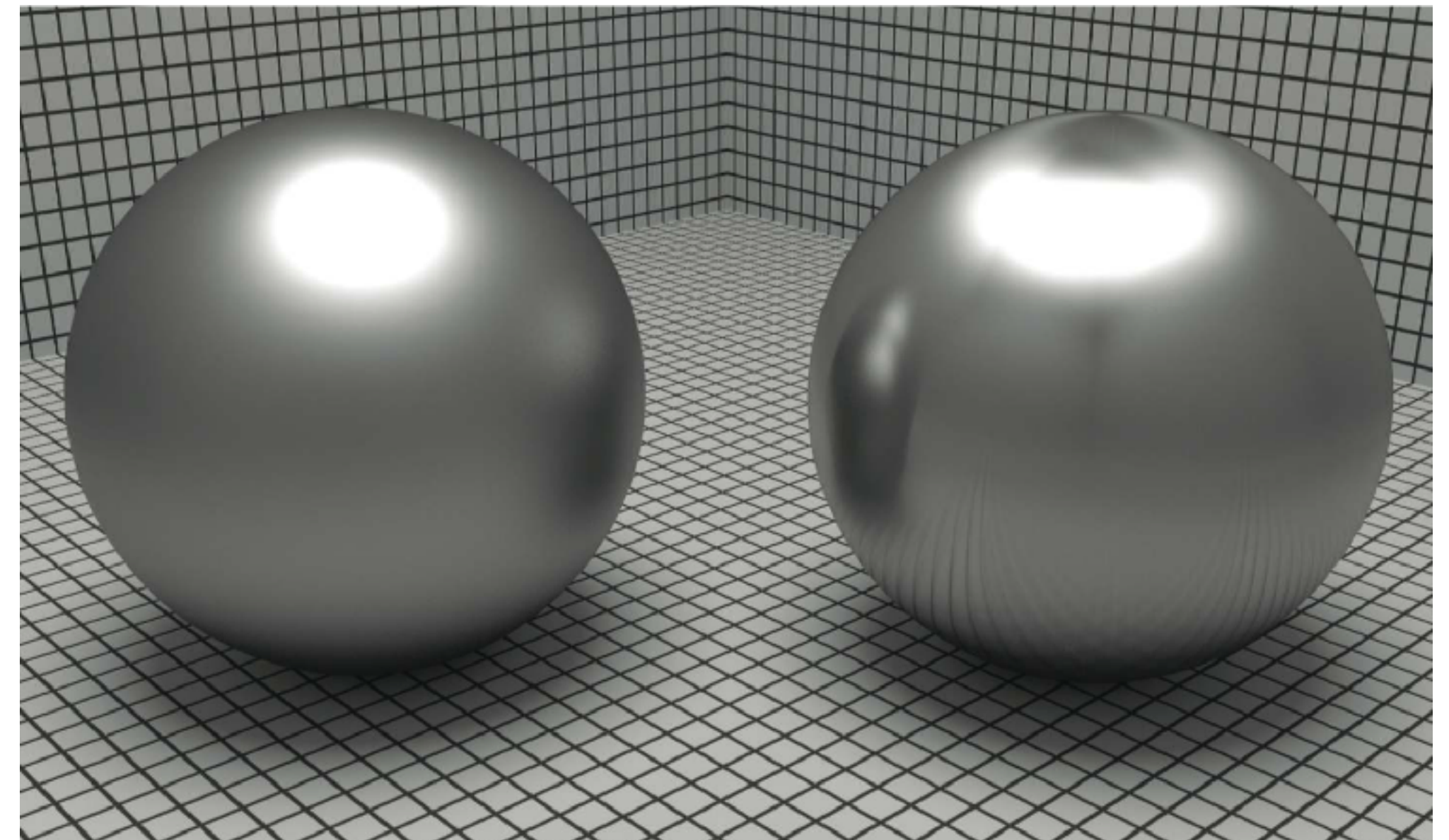


Anisotropic

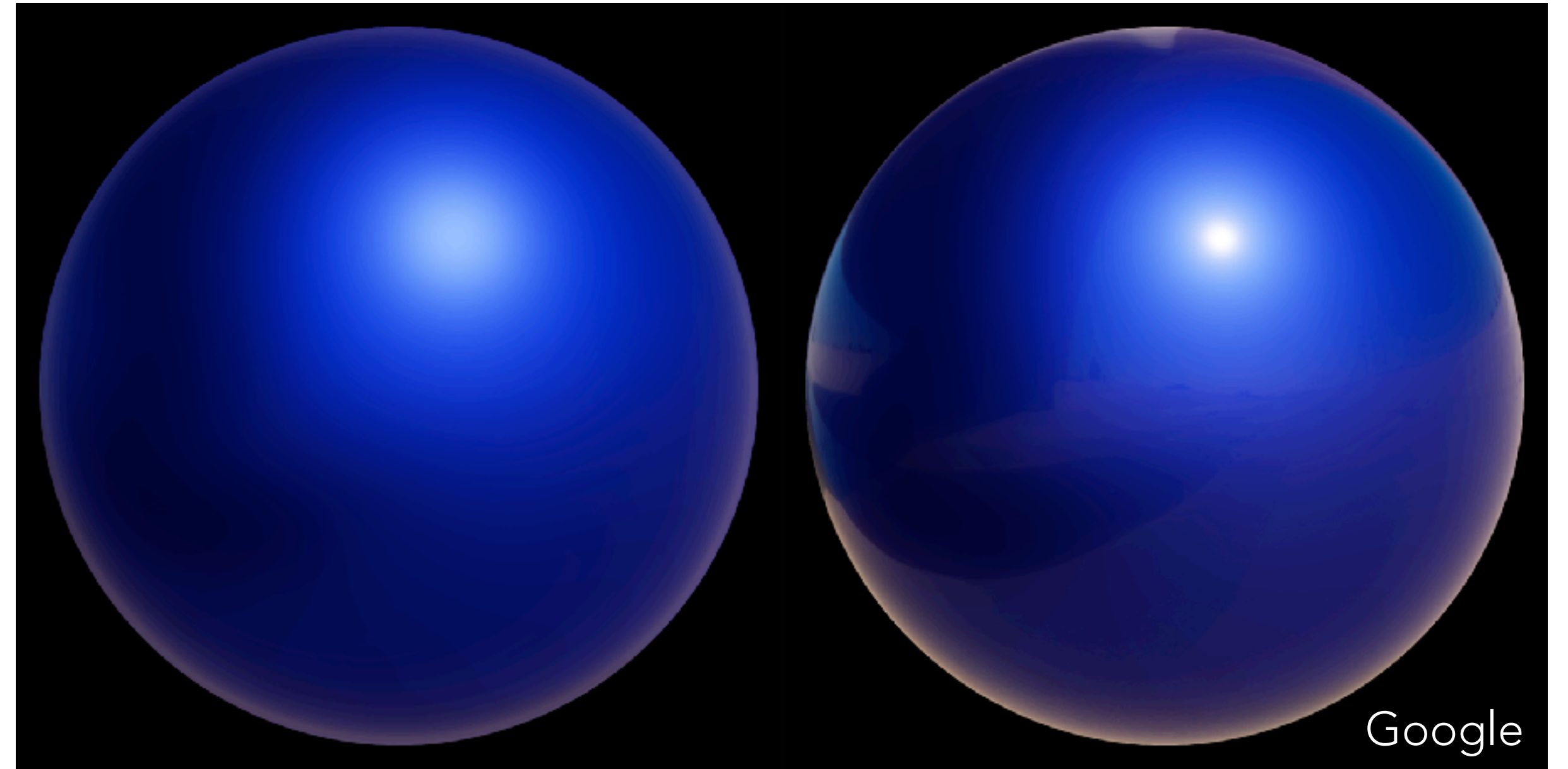
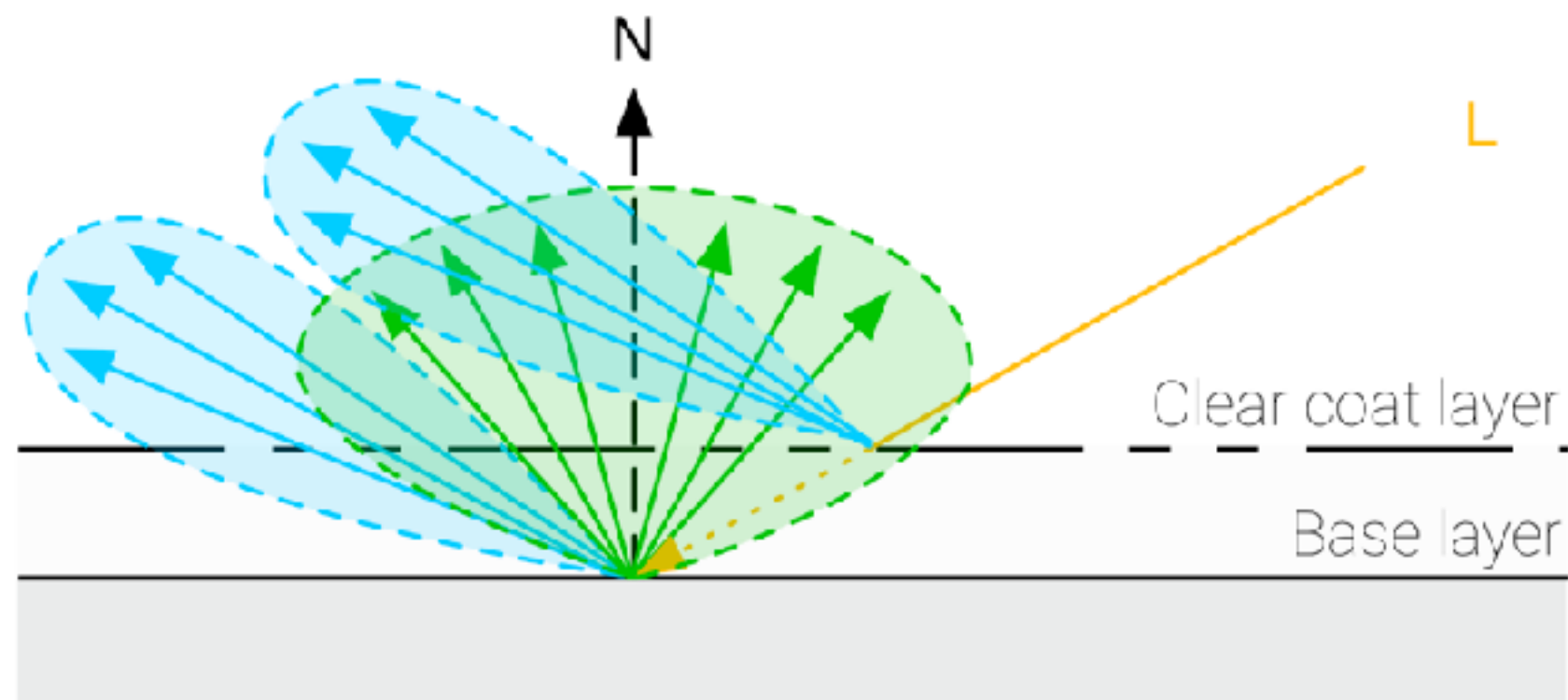


Surface (normals)

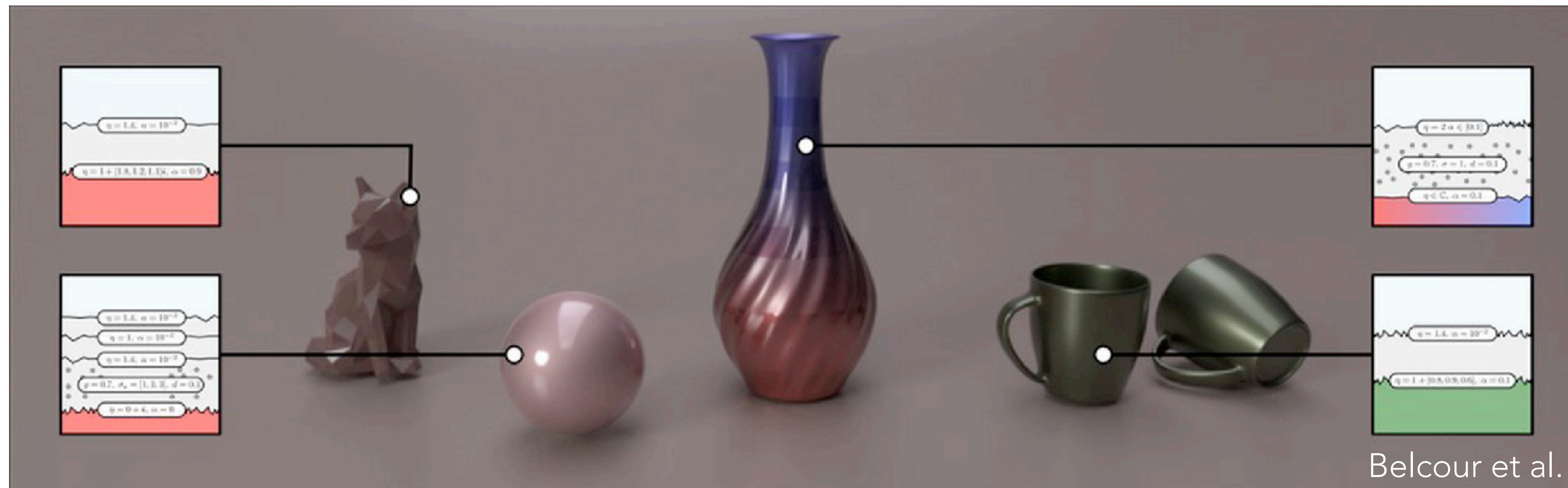
BRDF (fix w_i , vary w_o)



Layered materials

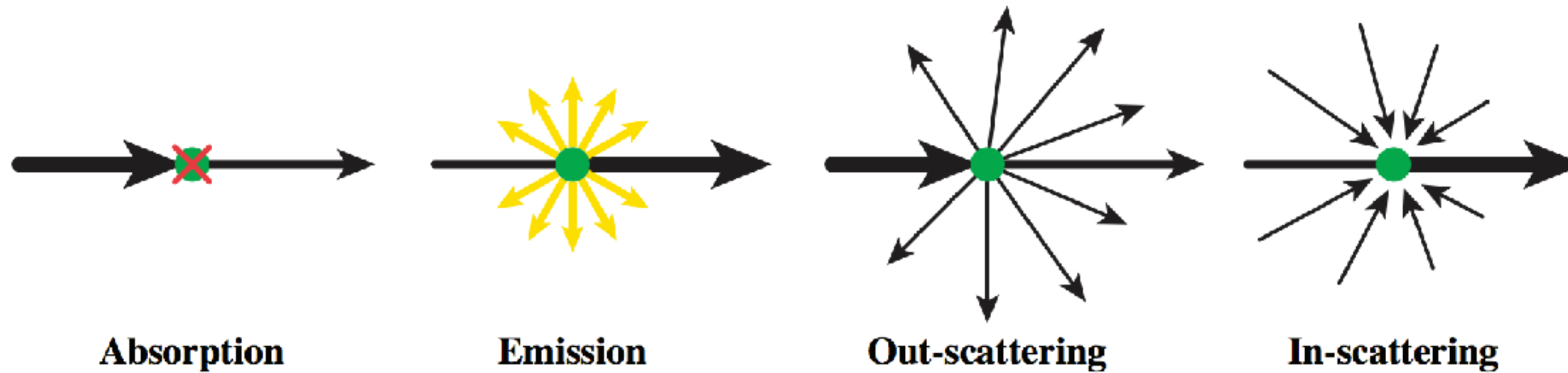


Google



Belcour et al.

Participating media

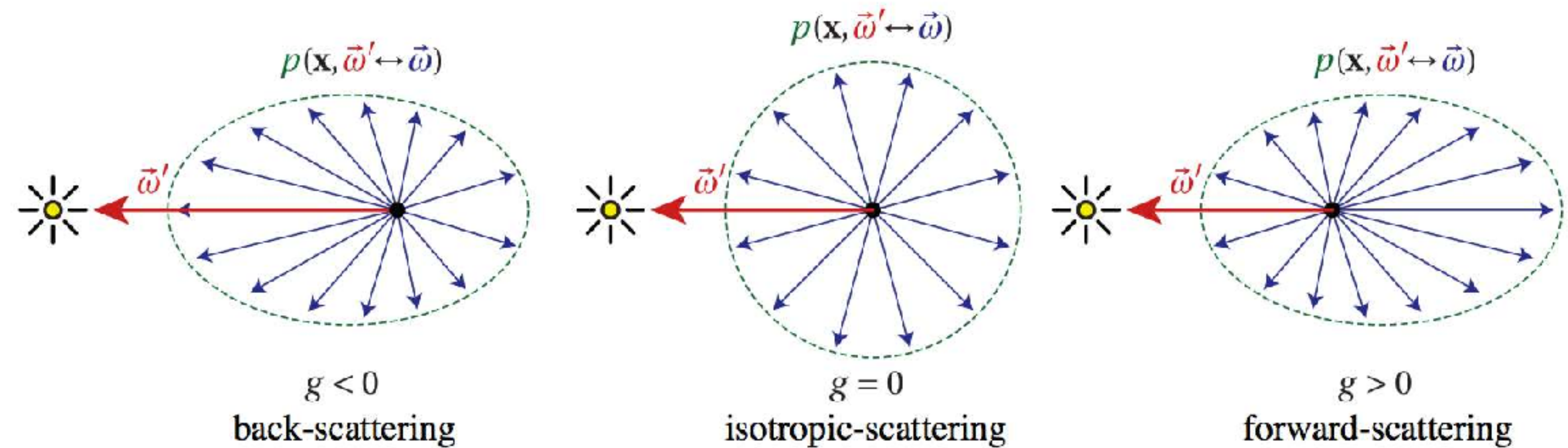


Wojciech Jarosz



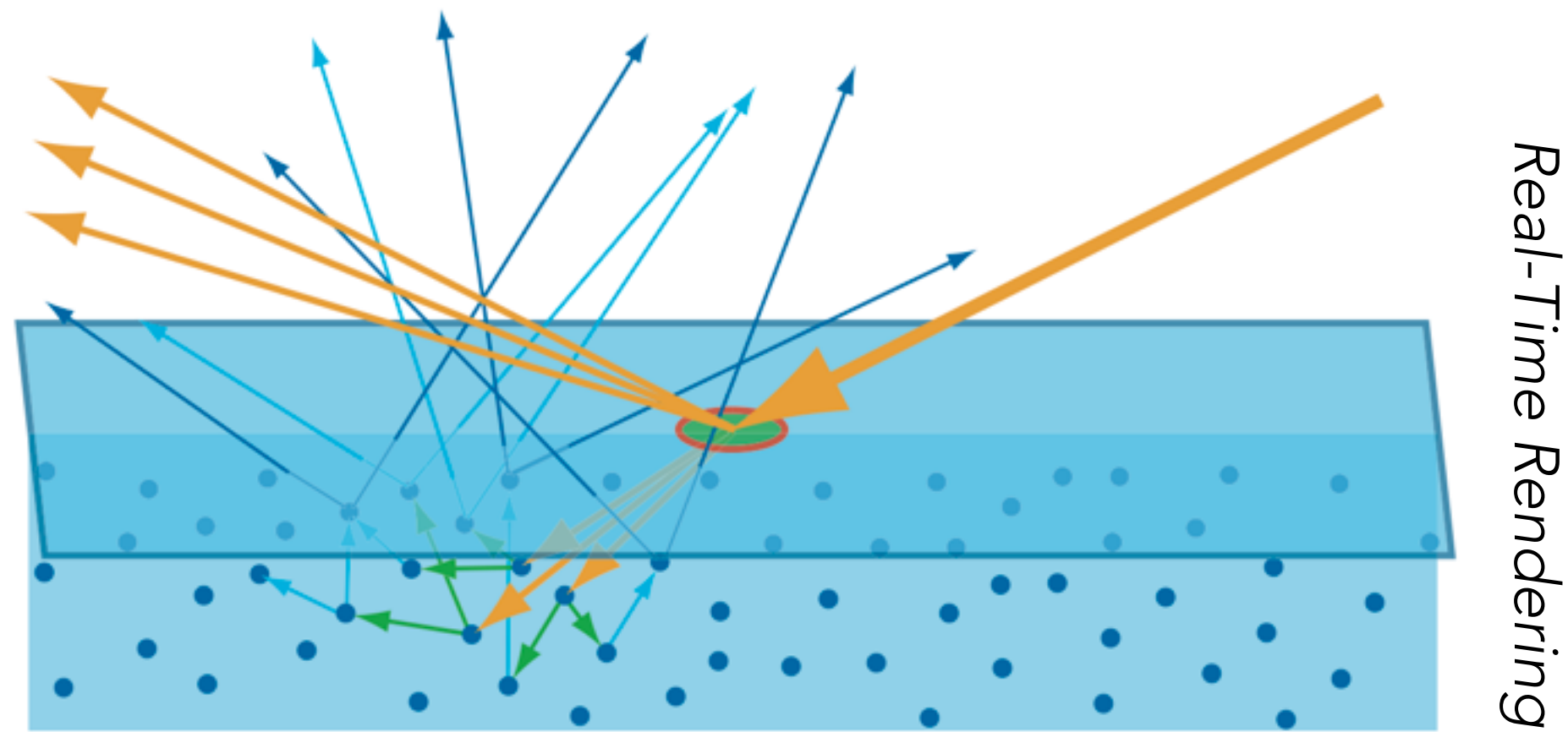
Bitterli et al. 2018

Phase function describes distribution of scattered ray directions



Wojciech Jarosz

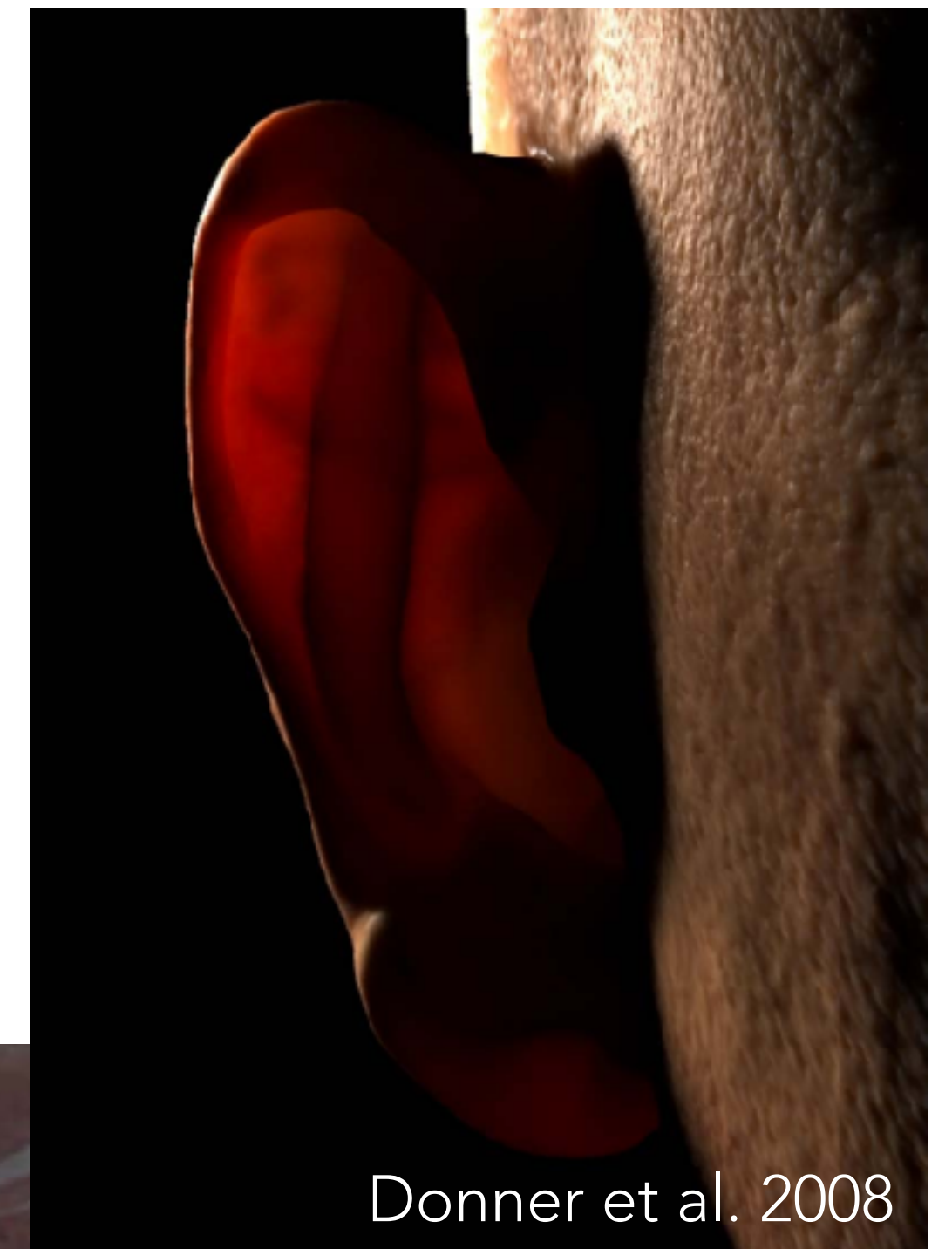
Translucent materials



Subsurface scattering:

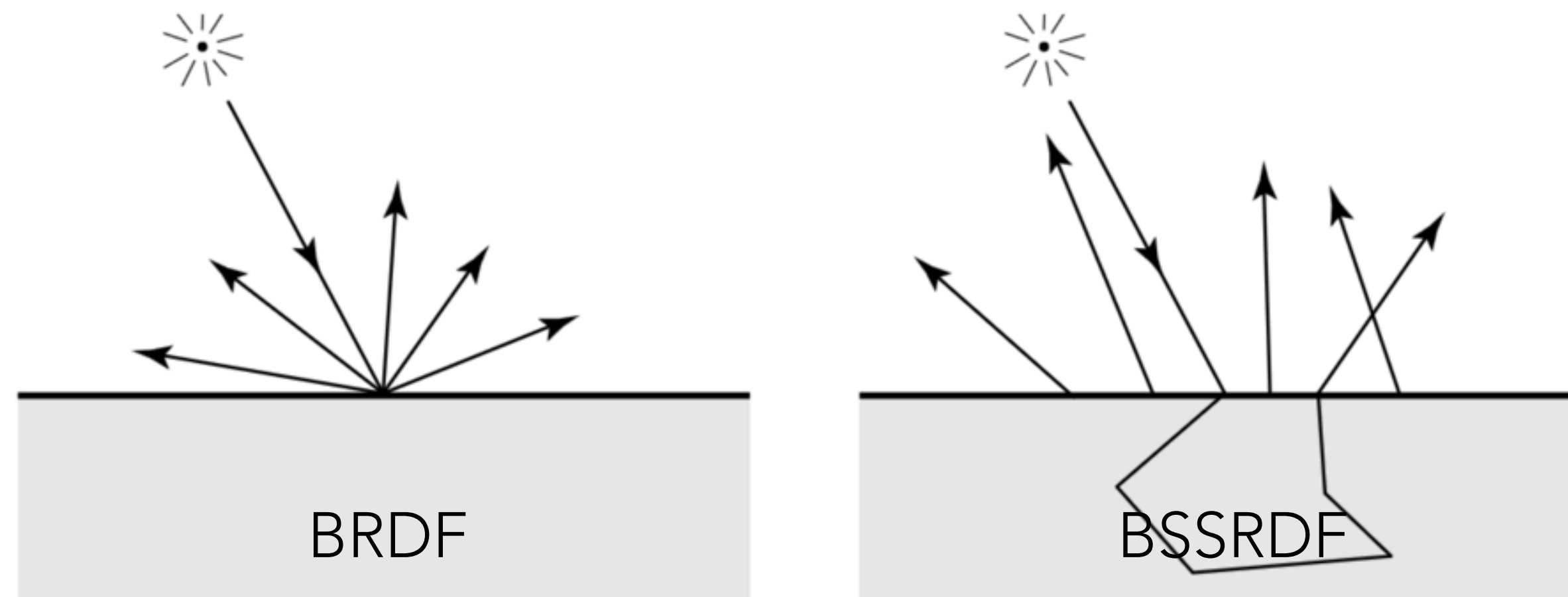
Light bounces around for a non-negligible distance in the material before emerging

Cannot be described by BRDF!



BRDF: $R(\omega_i, \omega_o)$

BSSRDF (bidirectional surface scattering RDF): $S(\mathbf{x}_i, \omega_i, \mathbf{x}_o, \omega_o)$



Now exitant radiance is

$$L_o(\mathbf{x}_o, \omega_o) = \int_A \int_{H^2} S(\mathbf{x}_i, \omega_i, \mathbf{x}_o, \omega_o) L_i(\mathbf{x}_i, \omega_i) \cos(\theta_i) d\omega_i dA$$



BRDF



BSSDF