

**COL781: Computer Graphics**

# 11. Transparency and Shading

# Assignment 1

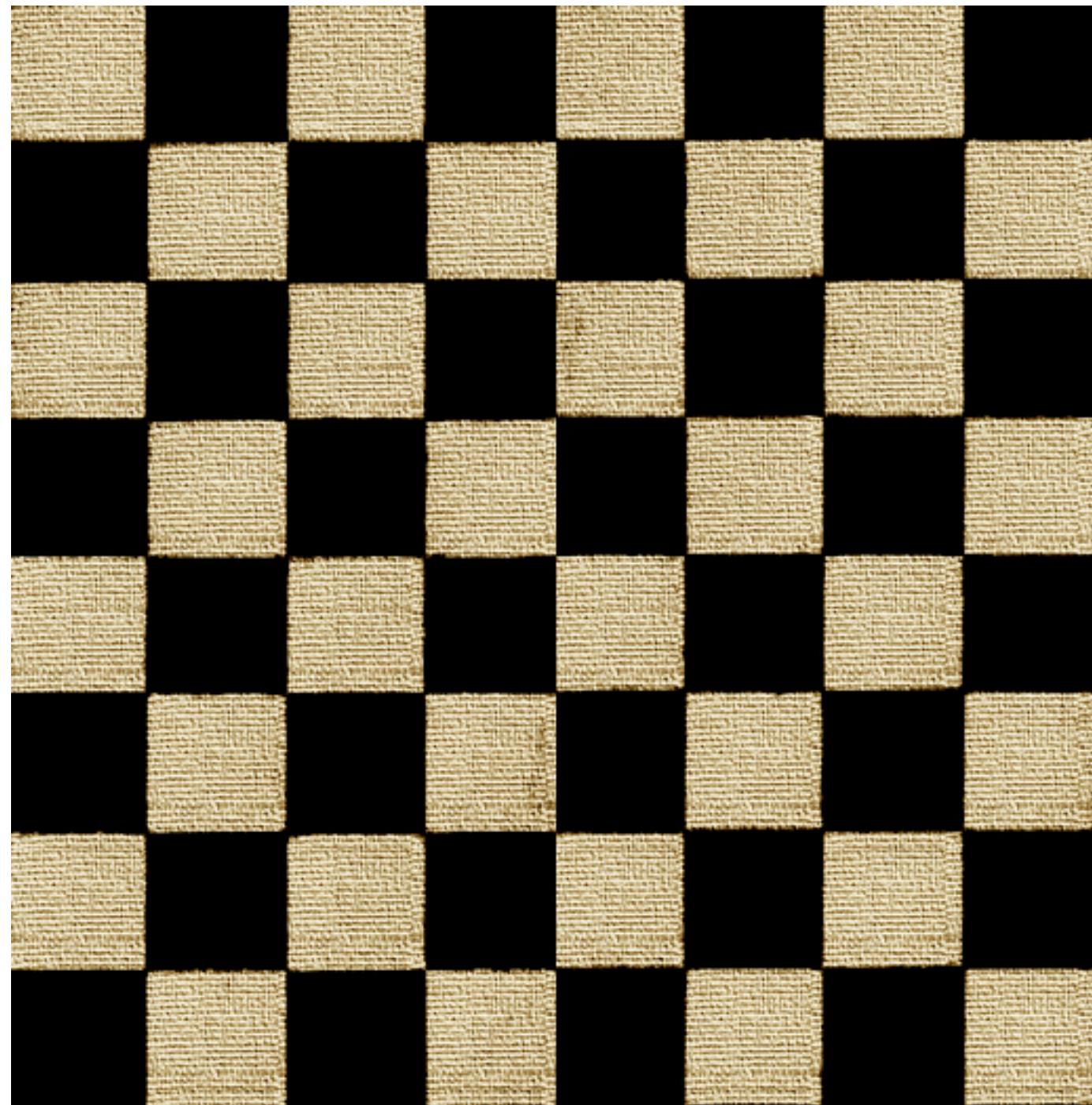
Deadline shifted to after Minor 1: **14 Feb**

Everyone who had not submitted their groups has been paired!

- Check your groups in Moodle: Navigation > 2202-COL781 > Participants
- Contact your groupmate as soon as possible!
- If the grouping is not OK for you (e.g. groupmate planning to withdraw), post on the Q&A forum

Drawing an opaque object: overwrite existing (background) colour with object colour

Drawing a transparent object: **combine** background colour and object colour



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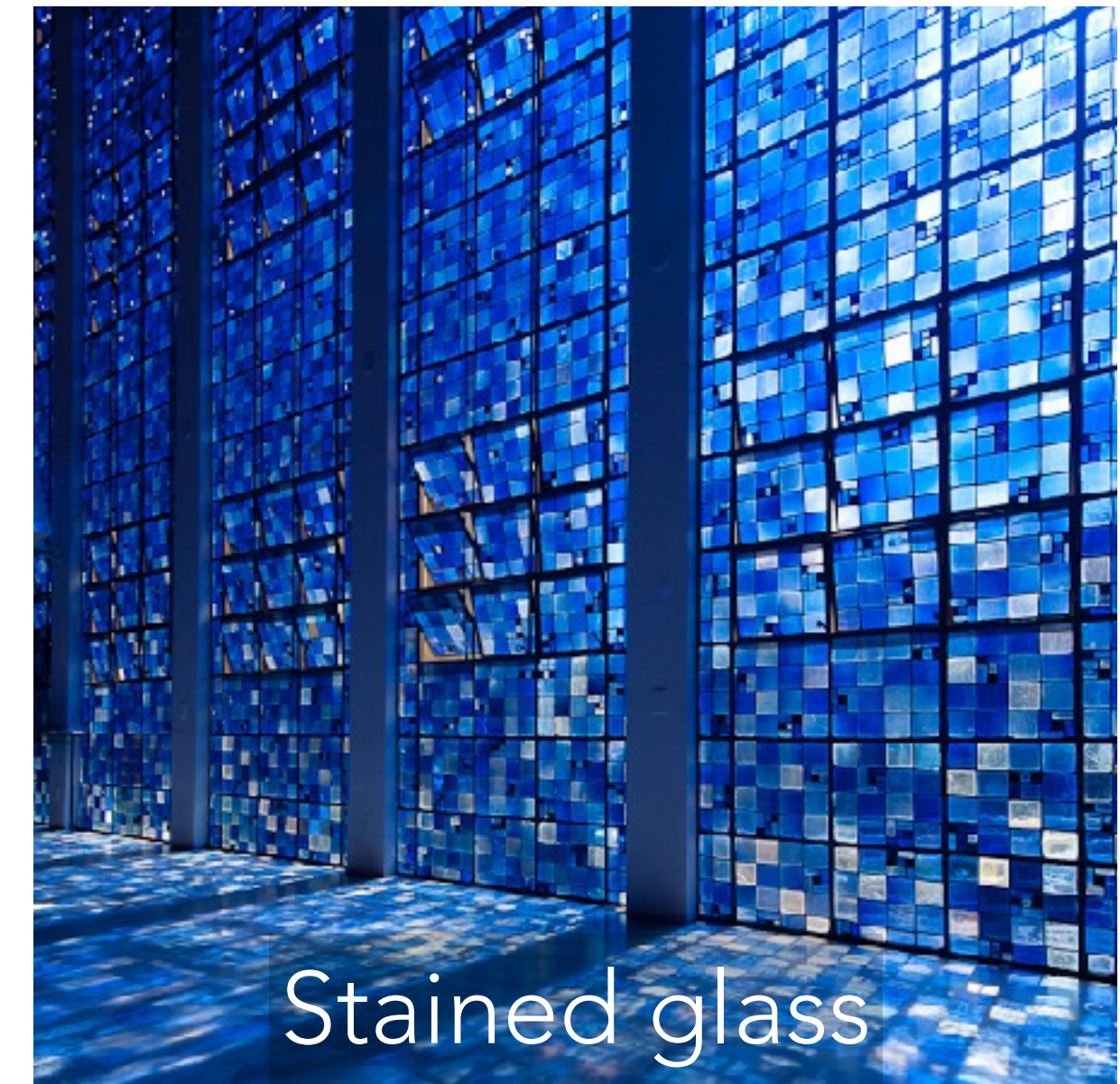


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## Puzzle:

Here are three blue things we might call transparent.  
Do their colours combine with the background in the same way?



Pick any two that behave **differently**, and explain why.

**Emission:**

$$(r_1+r_2, g_1+g_2, b_1+b_2)$$



**Partial occlusion:**

$$(ar_1+(1-a)r_2, ag_1+(1-a)g_2, ab_1+(1-a)b_2)$$

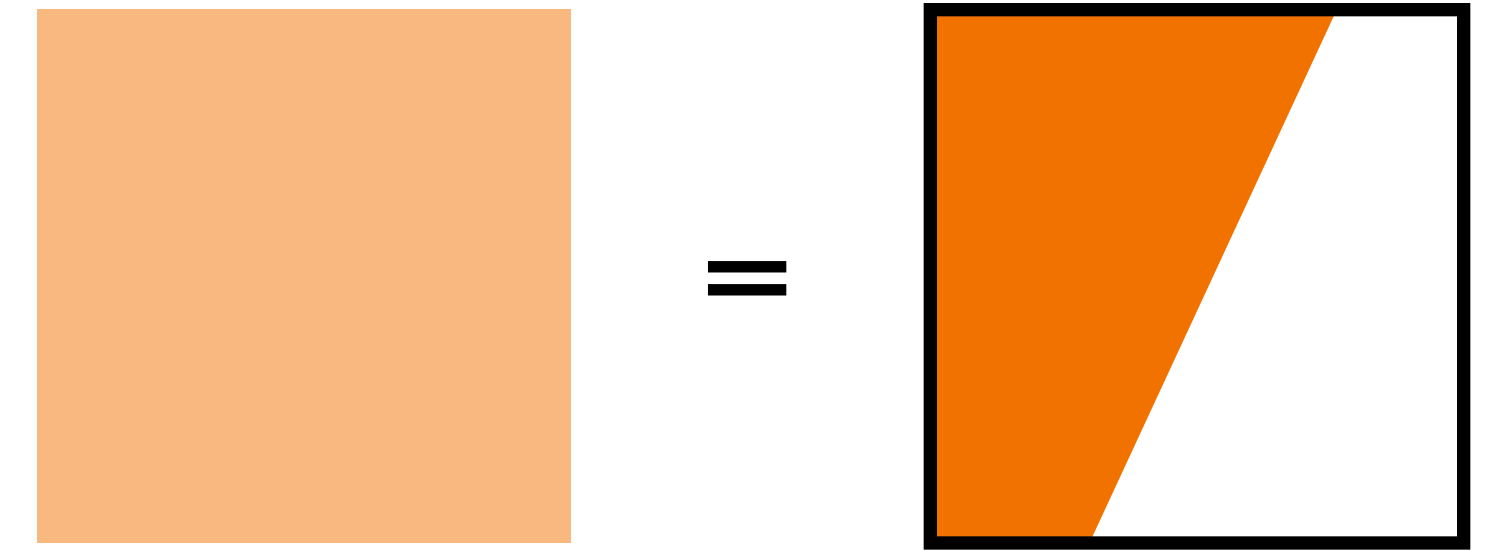


**Absorption:**

$$(r_1r_2, g_1g_2, b_1b_2)$$



# Alpha compositing



Standard interpretation of 4-component  $(r, g, b, a)$ :

Object  $A$  has colour  $(r_A, g_A, b_A)$  and covers a fraction  $a_A$  of the sample.

Suppose we draw it over a background  $B$  with colour  $(r_B, g_B, b_B)$ .

Output colour ( $A$  **over**  $B$ ) = weighted average:

$$\begin{aligned}r_O &= a_A r_A + (1 - a_A) r_B \\g_O &= a_A g_A + (1 - a_A) g_B \\b_O &= a_A b_A + (1 - a_A) b_B\end{aligned}$$

[One of 12 compositing operators defined by Porter and Duff in 1984.]



over



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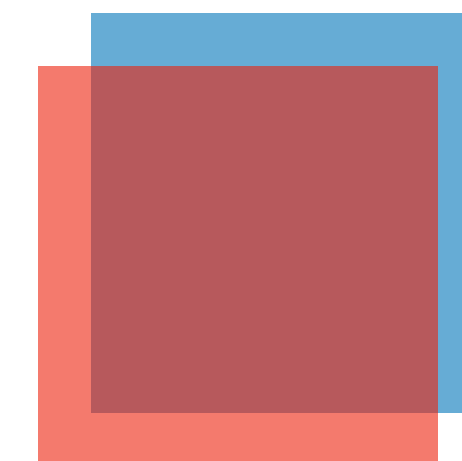
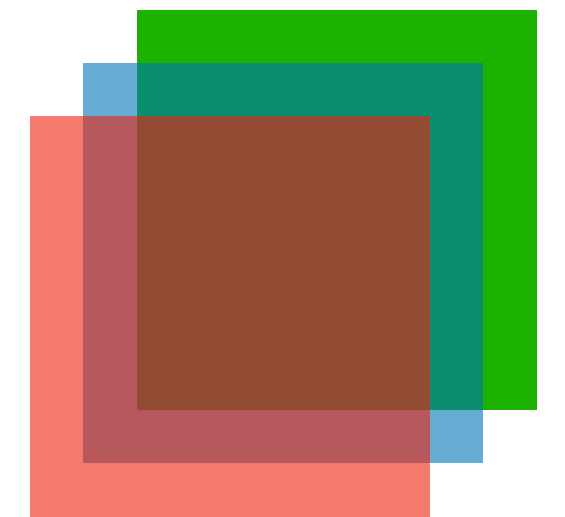


What if  $B$  also has  $\alpha_B < 1$ ?

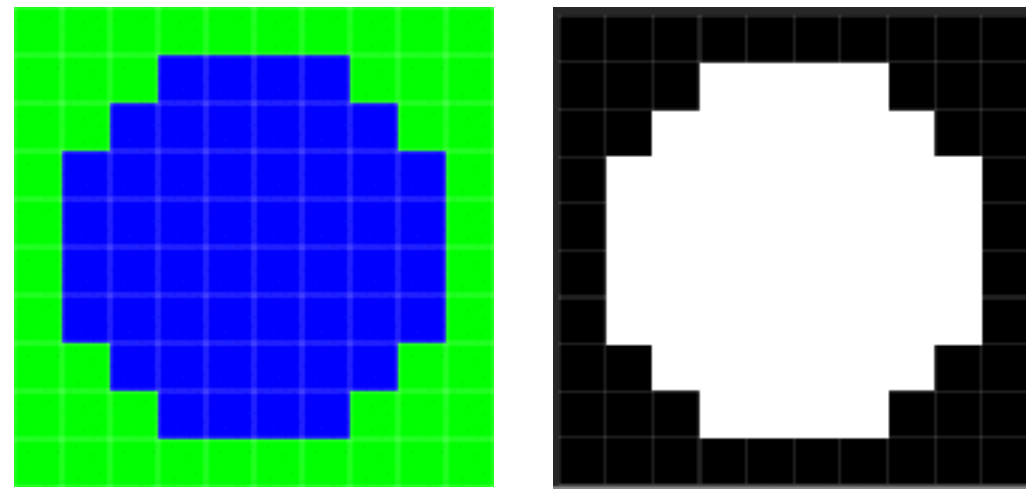
Result should be such that  $(A \text{ over } B) \text{ over } C = A \text{ over } (B \text{ over } C)$

$$\alpha_O = \alpha_A + (1 - \alpha_A)\alpha_B$$
$$c_O = (\alpha_{ACA} + (1 - \alpha_A)\alpha_{BCB}) / \alpha_O$$

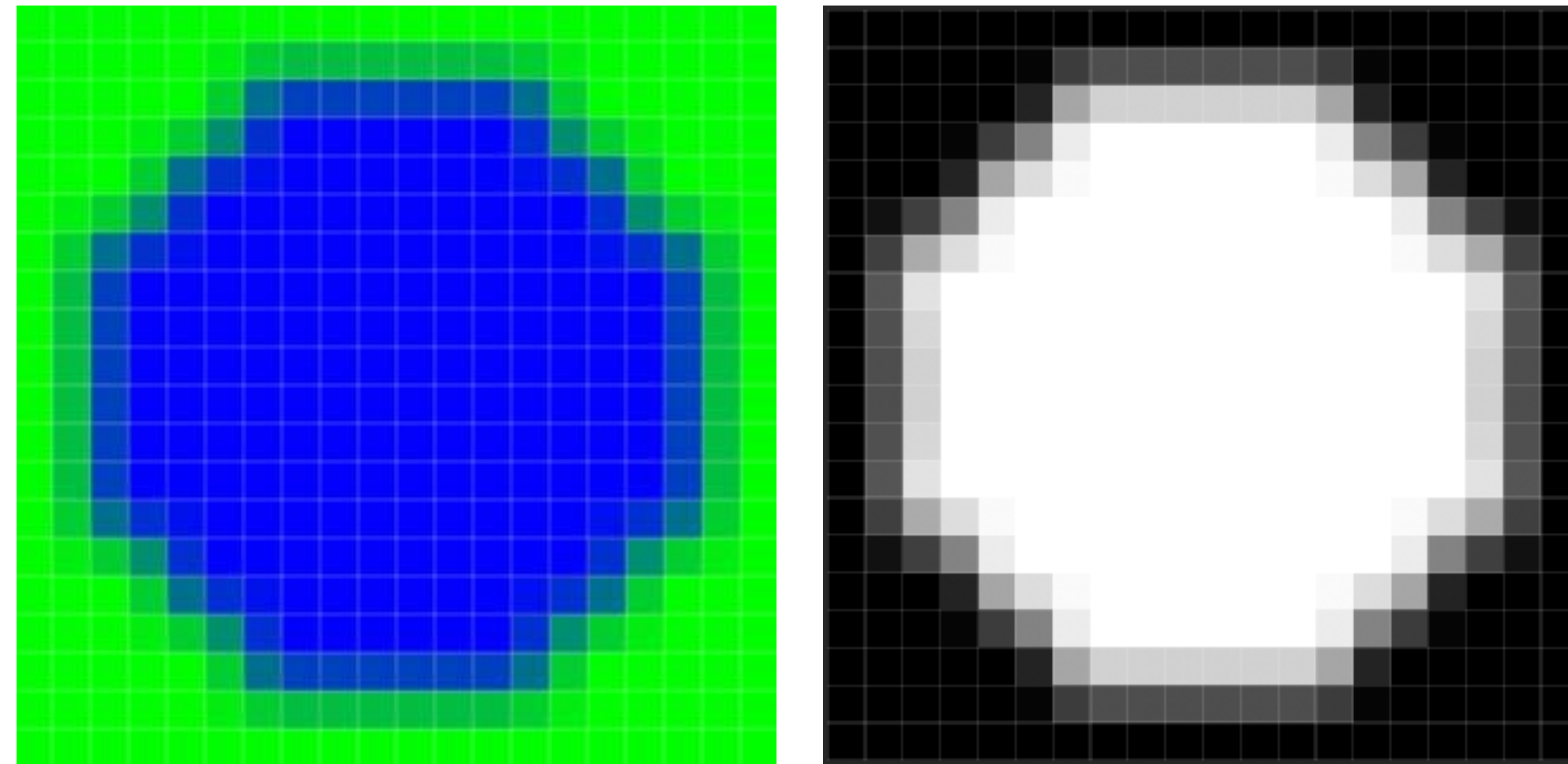
**Non-commutative:**  $A \text{ over } B \neq B \text{ over } A$



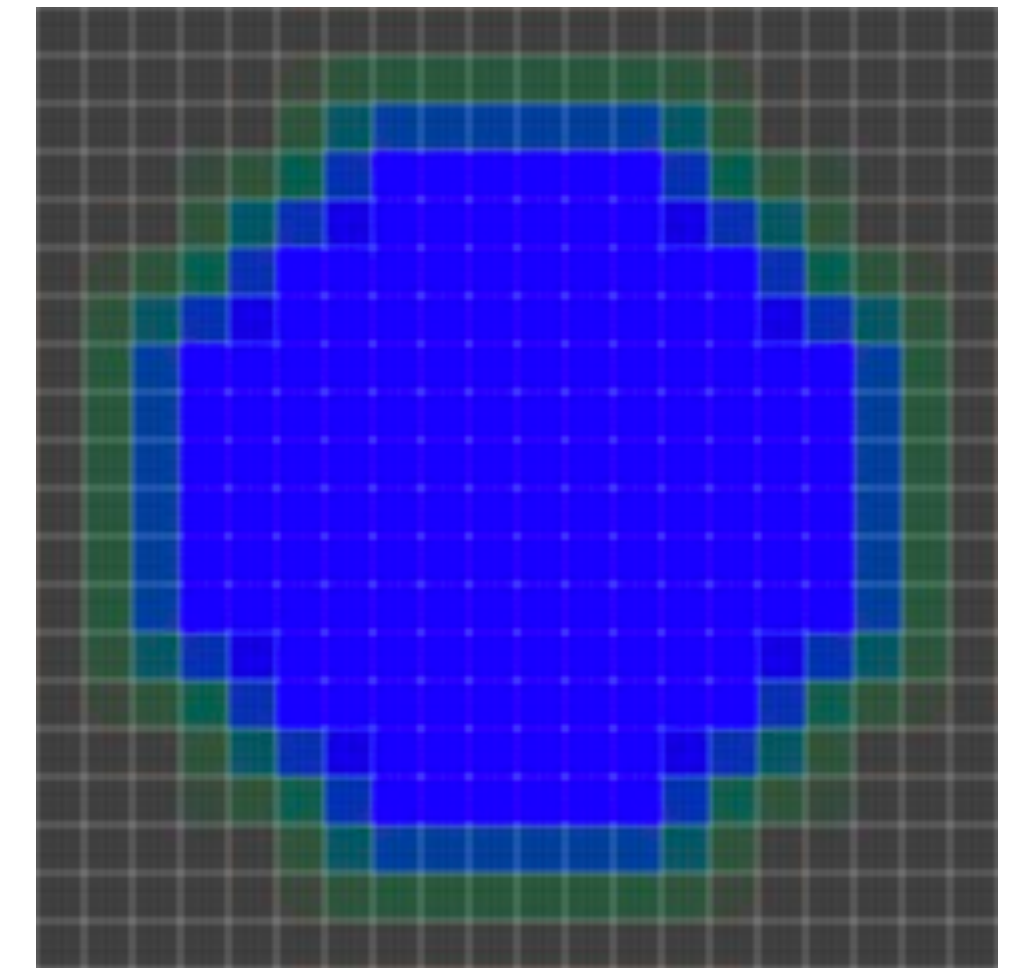




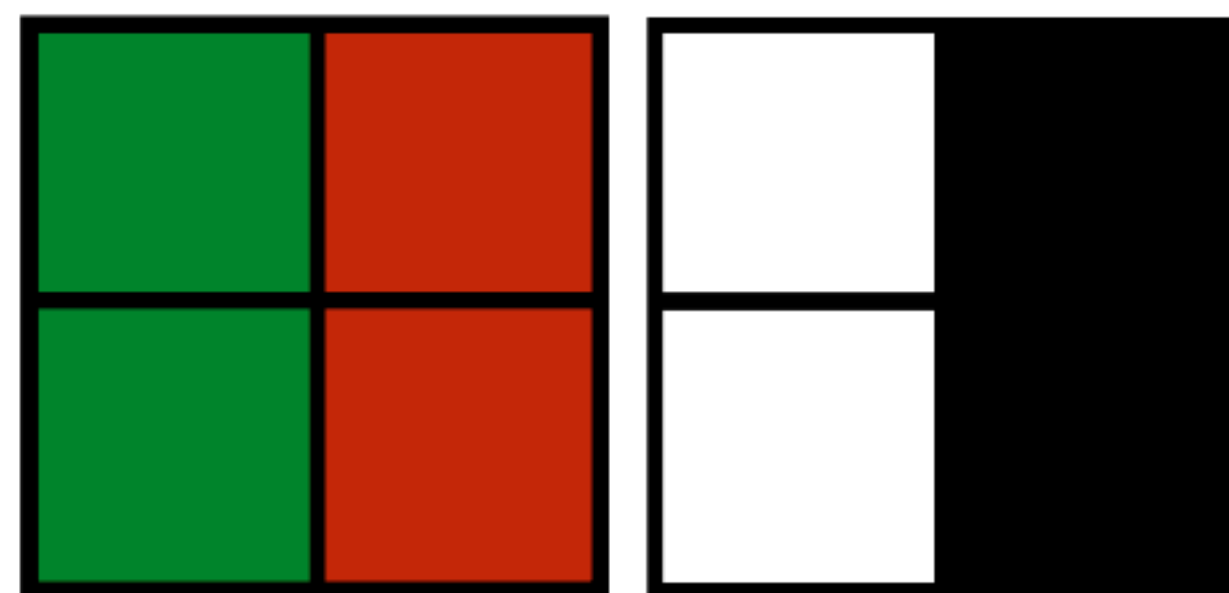
Original  
colour & alpha



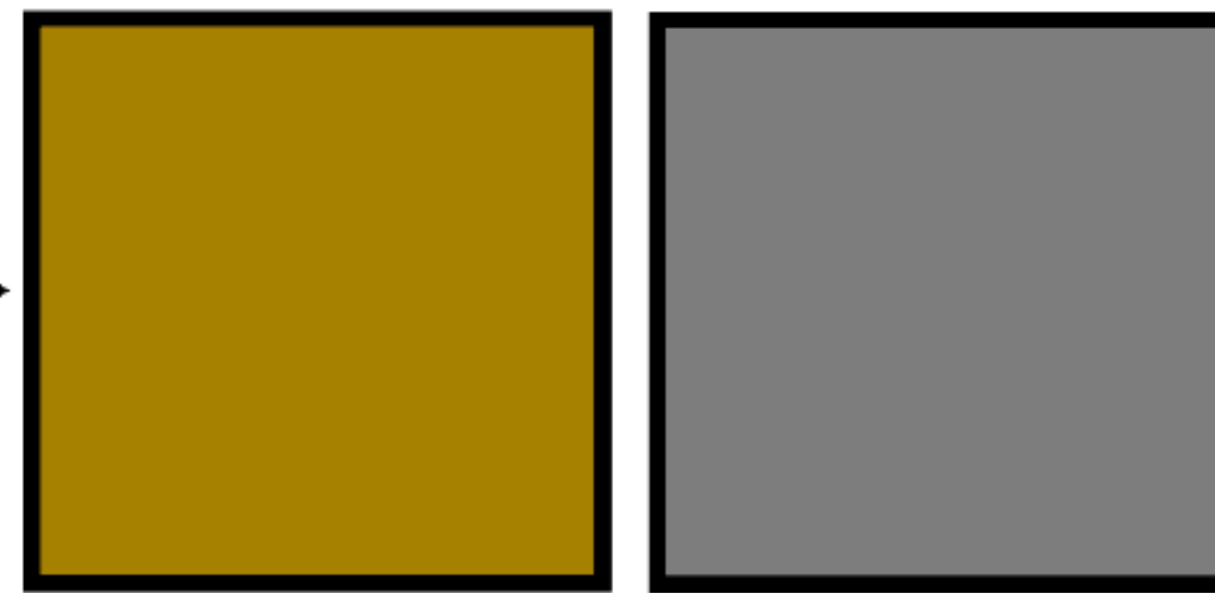
Upsampled colour & alpha



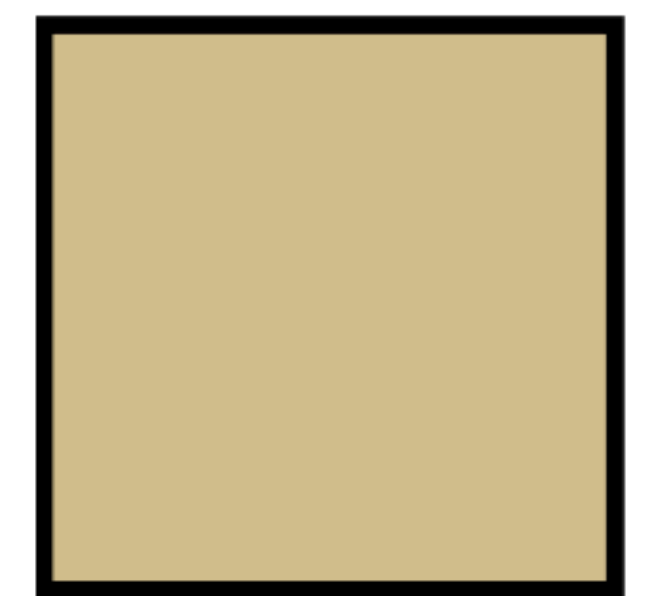
Over gray



Original colour & alpha



Downsampled colour & alpha



Over white

# Premultiplied alpha

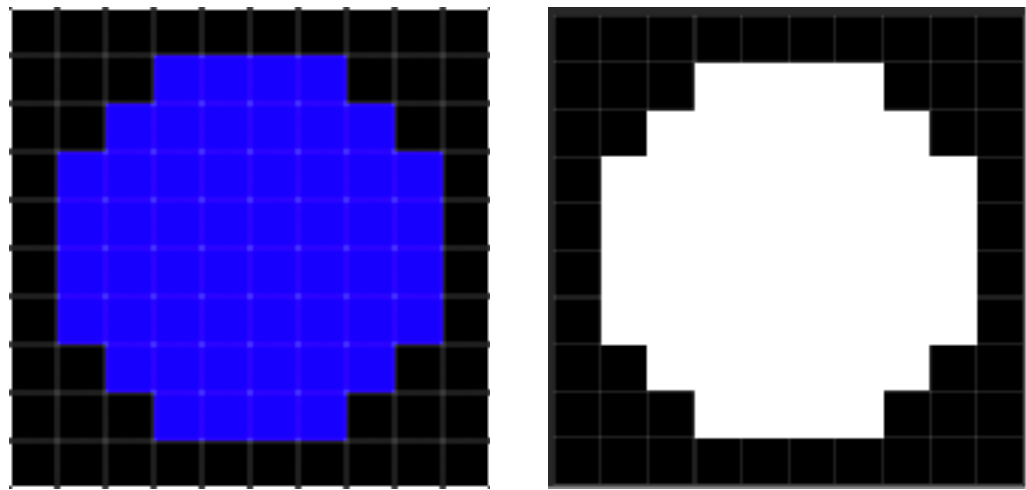
Instead of  $(r, g, b, a)$ , store  $(r', g', b', a)$  where  $r' = ar$ ,  $g' = ag$ ,  $b' = ab$

Compositing formula becomes much simpler:

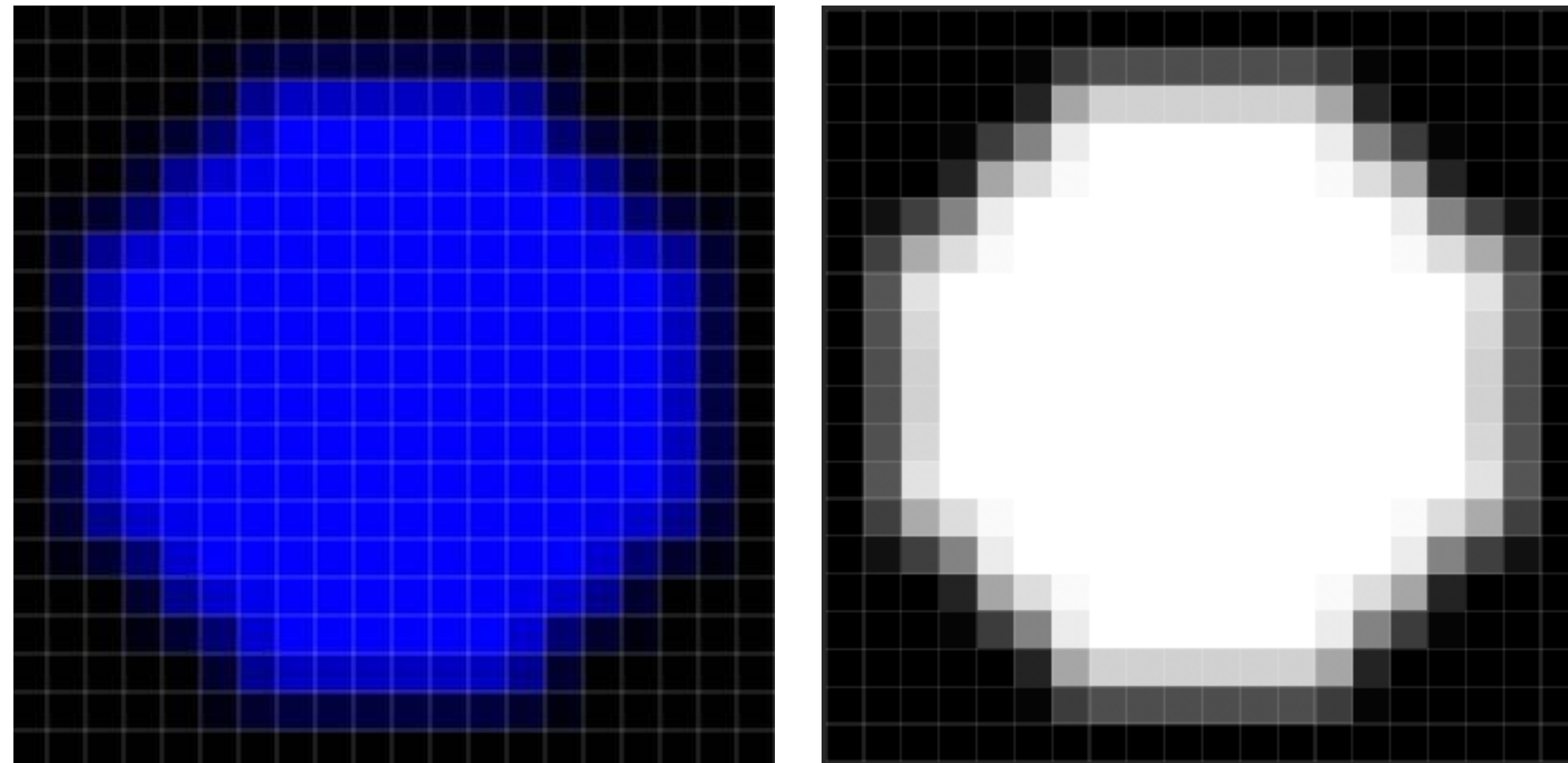
$$\begin{aligned}a_O &= a_A + (1 - a_A)a_B \\c_O' &= c_A' + (1 - a_A)c_B'\end{aligned}$$

In the end, get final colour  $(r, g, b) = (r'/a, g'/a, b'/a, a)$

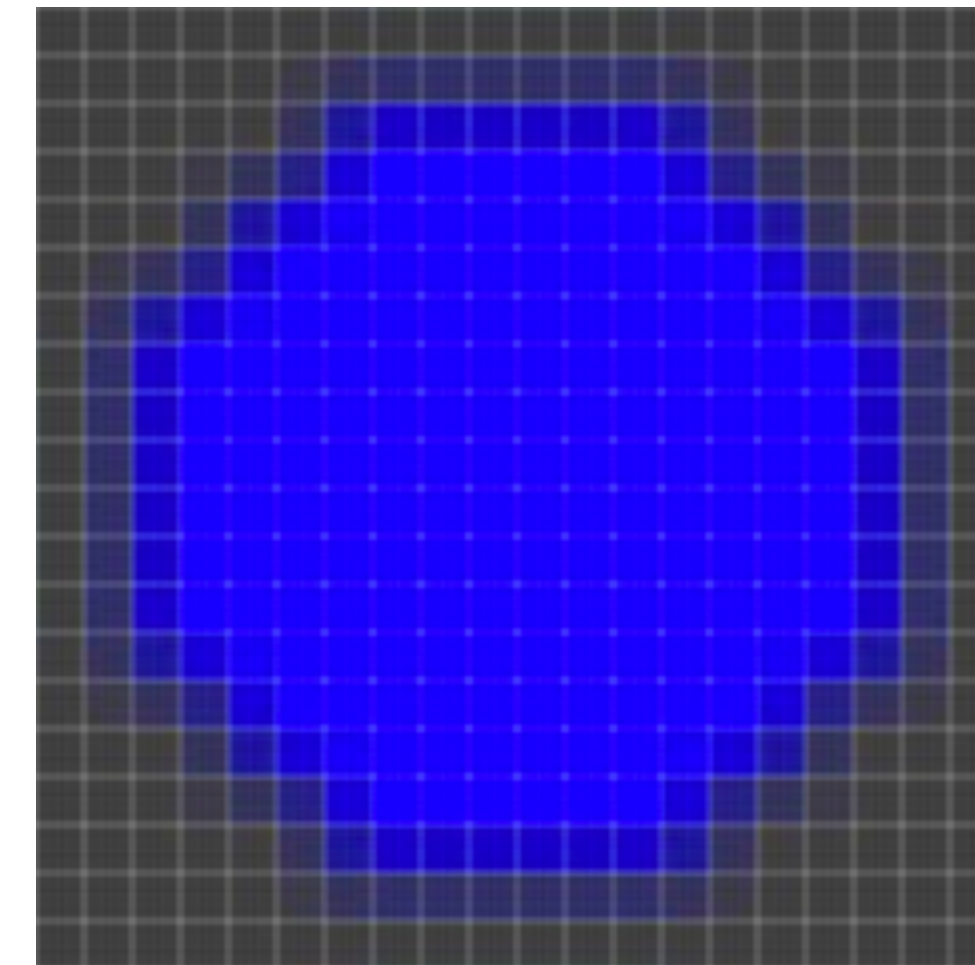
(Basically homogeneous coordinates for colours!)



Premultiplied colour & alpha



Upsampled premultiplied colour & alpha



Over gray



Premultiplied colour & alpha



Downsampled premultiplied colour & alpha



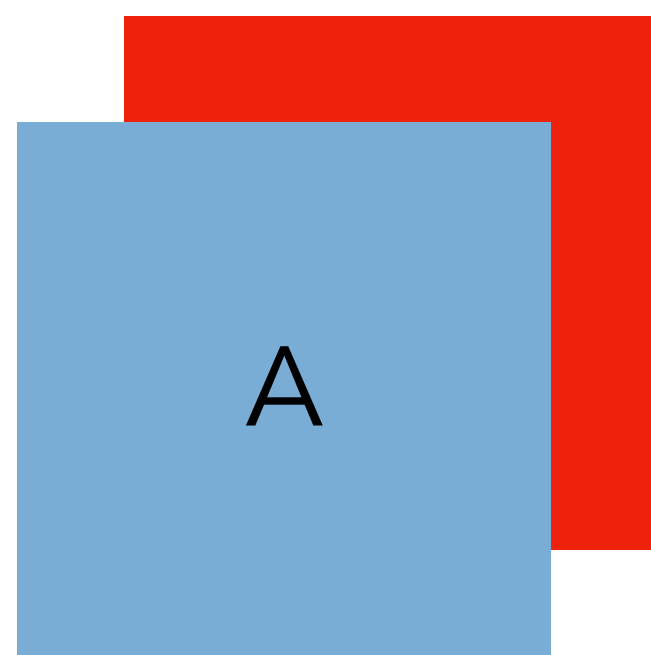
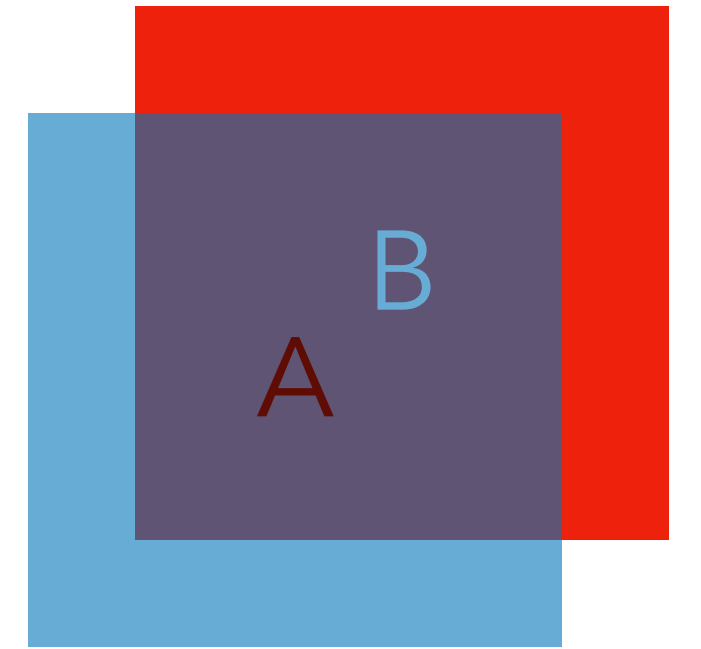
Over white

# Transparency in 3D

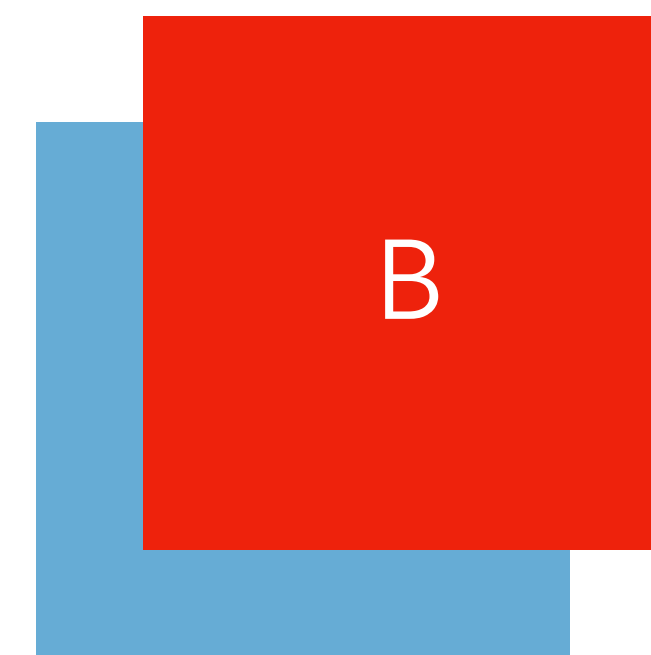
Suppose transparent object *A* is in front of opaque object *B*.

**If *B* is drawn first:** no problem.

**If *A* is drawn first:** what to do with the z-buffer?



z-buffer updated by *A*

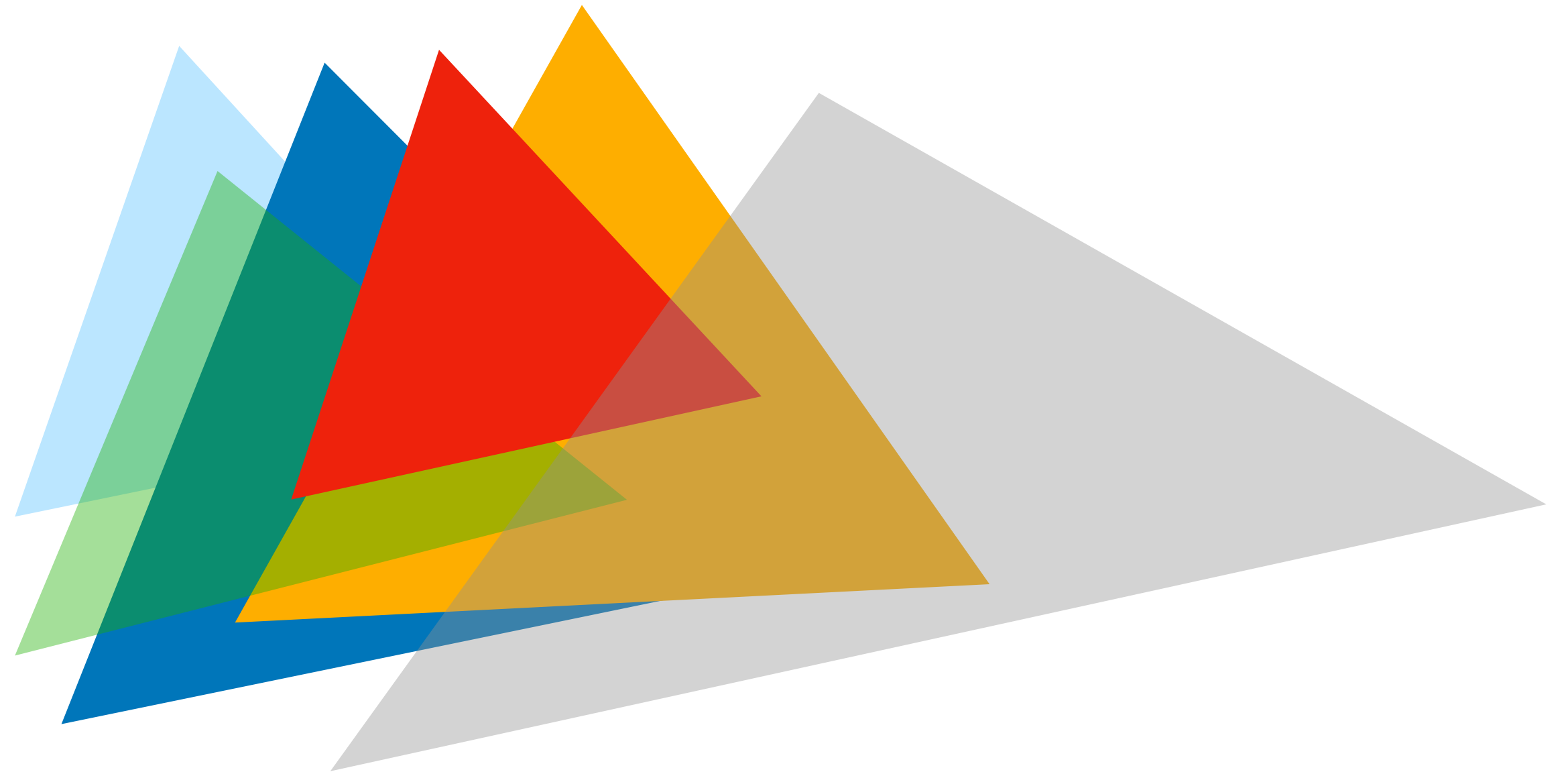


z-buffer not updated by *A*

If only one transparent object in the scene: just draw it last

If multiple transparent objects:

1. Draw all opaque objects (in any order)
2. Draw transparent objects (in back-to-front order)



**Order-independent transparency** on the CPU: A-buffer [Carpenter 1984].  
On the GPU: hard problem! Many approximation techniques...

No problem at all for ray tracing (later lecture)

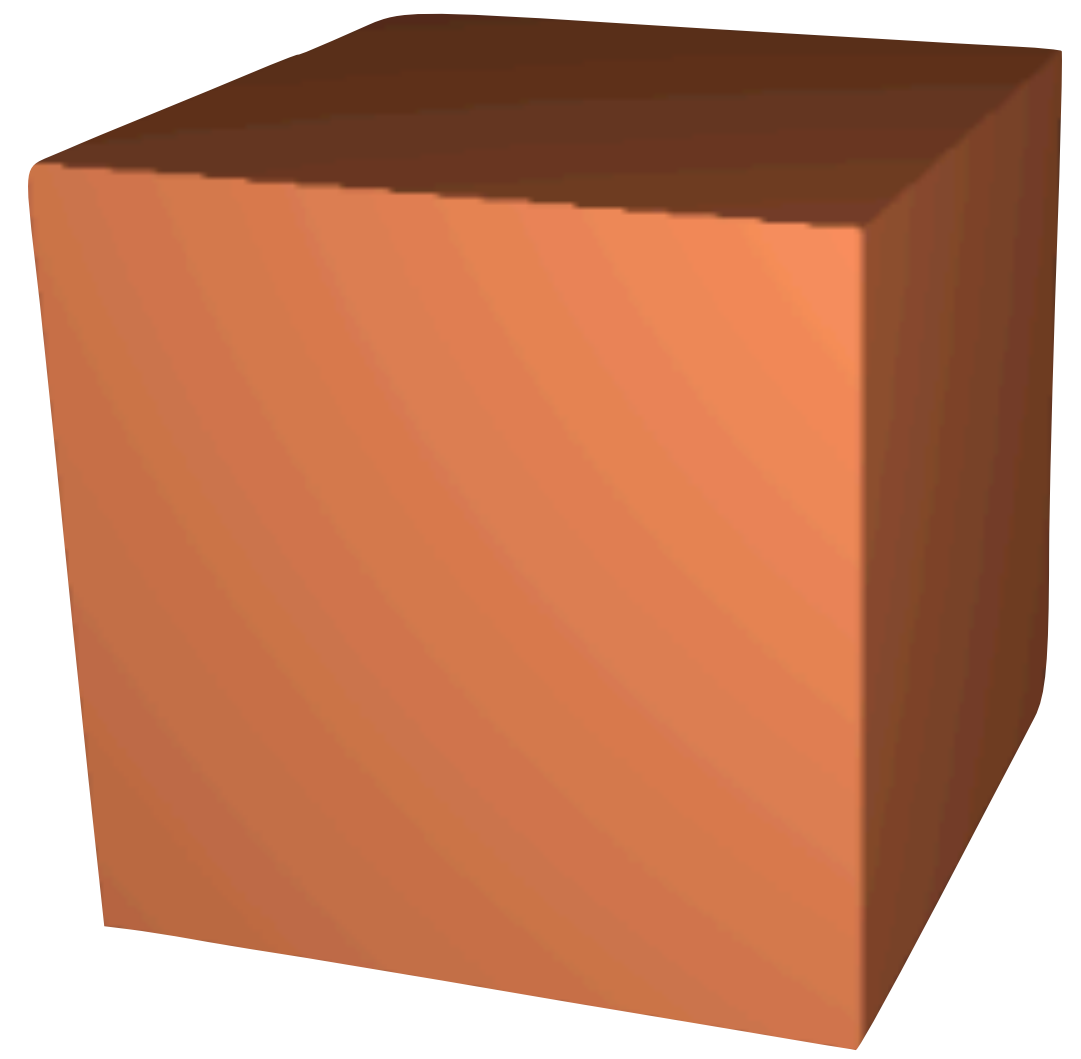
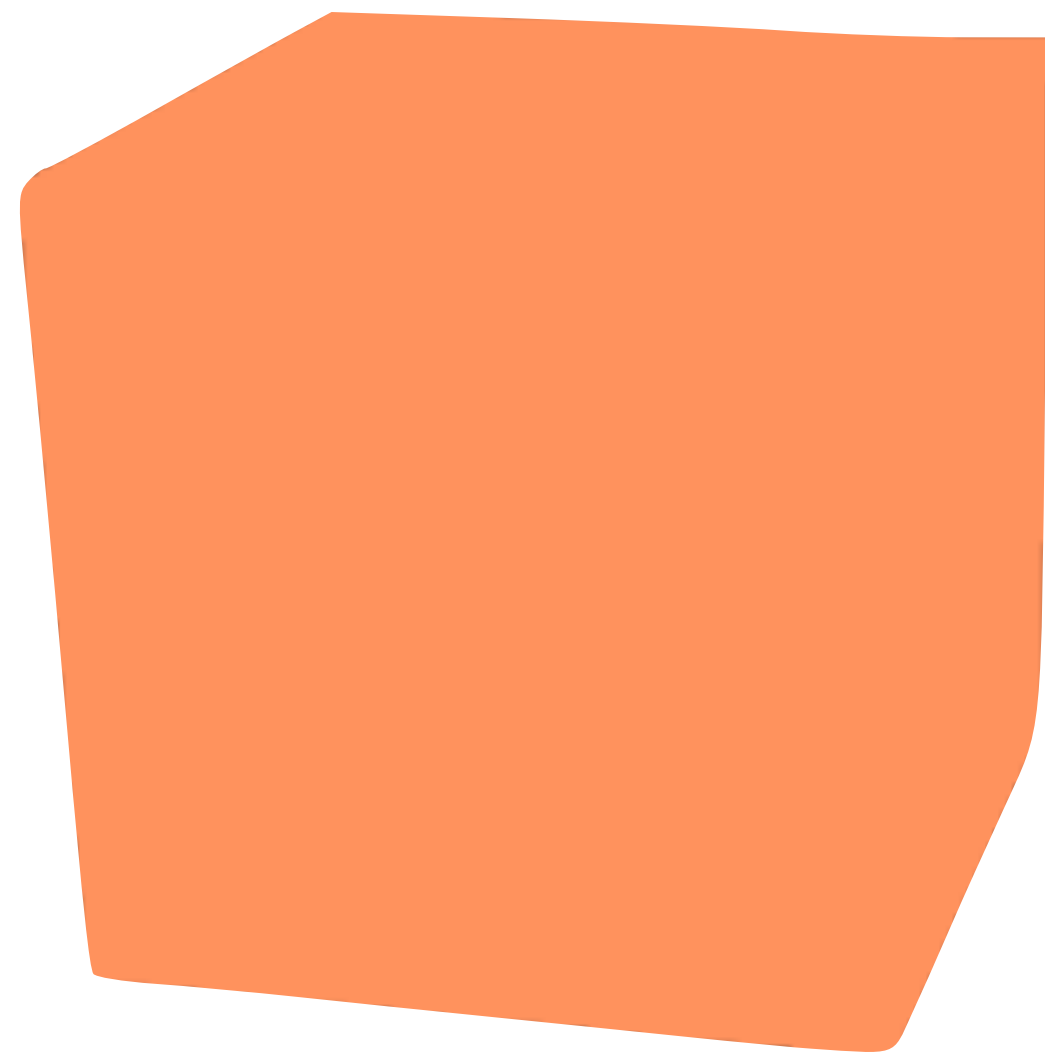
# Exercise

Show that weighted averaging of semi-transparent colours only works correctly with premultiplied alpha. That is,

- averaging  $A$  and  $B$  and then compositing the result over  $C$ , and
  - compositing  $A$  over  $C$ , and  $B$  over  $C$ , then averaging the results
- are always the same when  $A$ ,  $B$ ,  $C$  are premultiplied, but not otherwise.



**Shading**



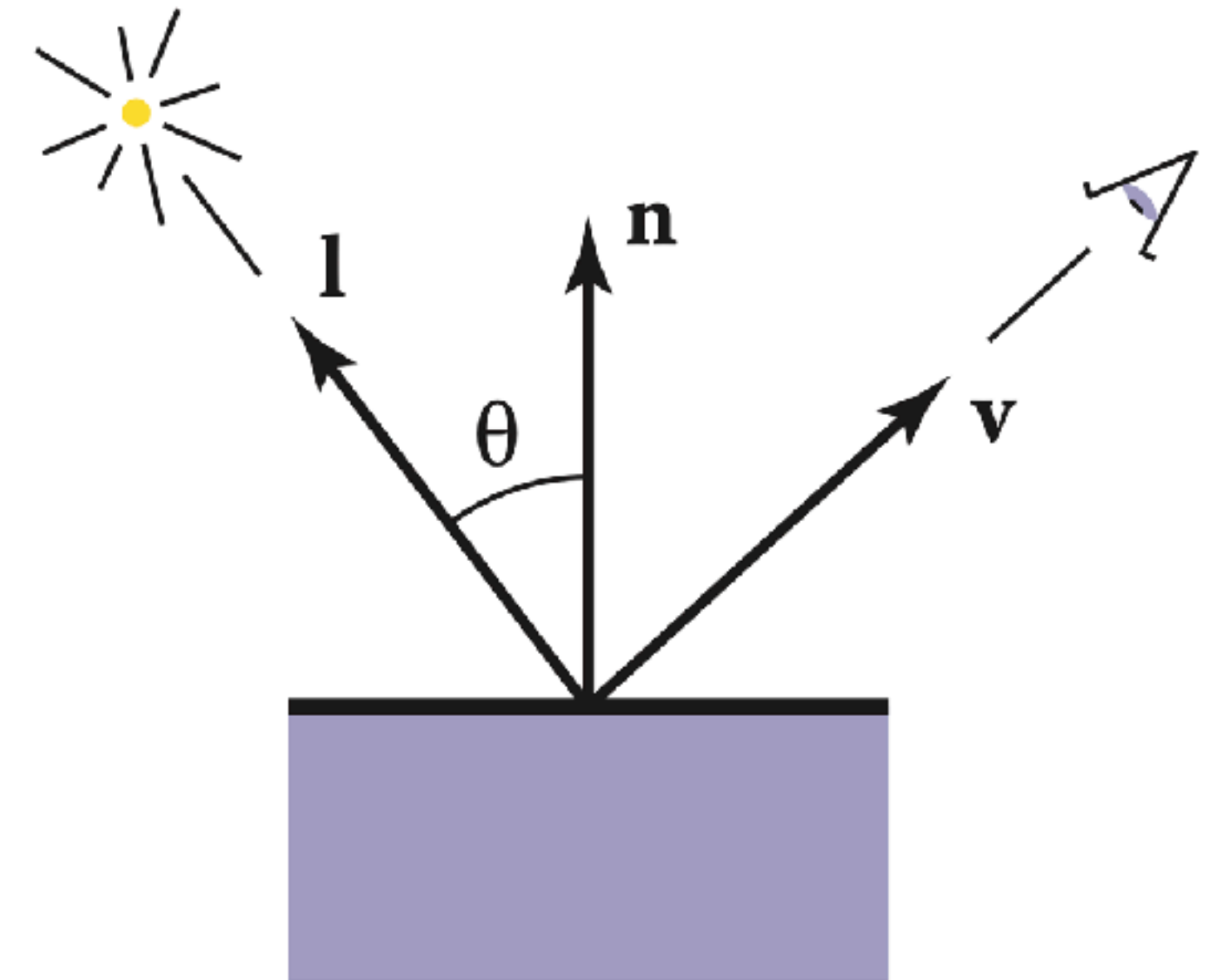
# Local illumination

Light from a light source with some given intensity hits the surface point

- Light direction  $\mathbf{l}$
- Surface normal  $\mathbf{n}$
- Viewer direction  $\mathbf{v}$

What intensity / colour of light is reflected towards the viewer?

Depends on surface properties (material, colour, roughness, coating, etc.)

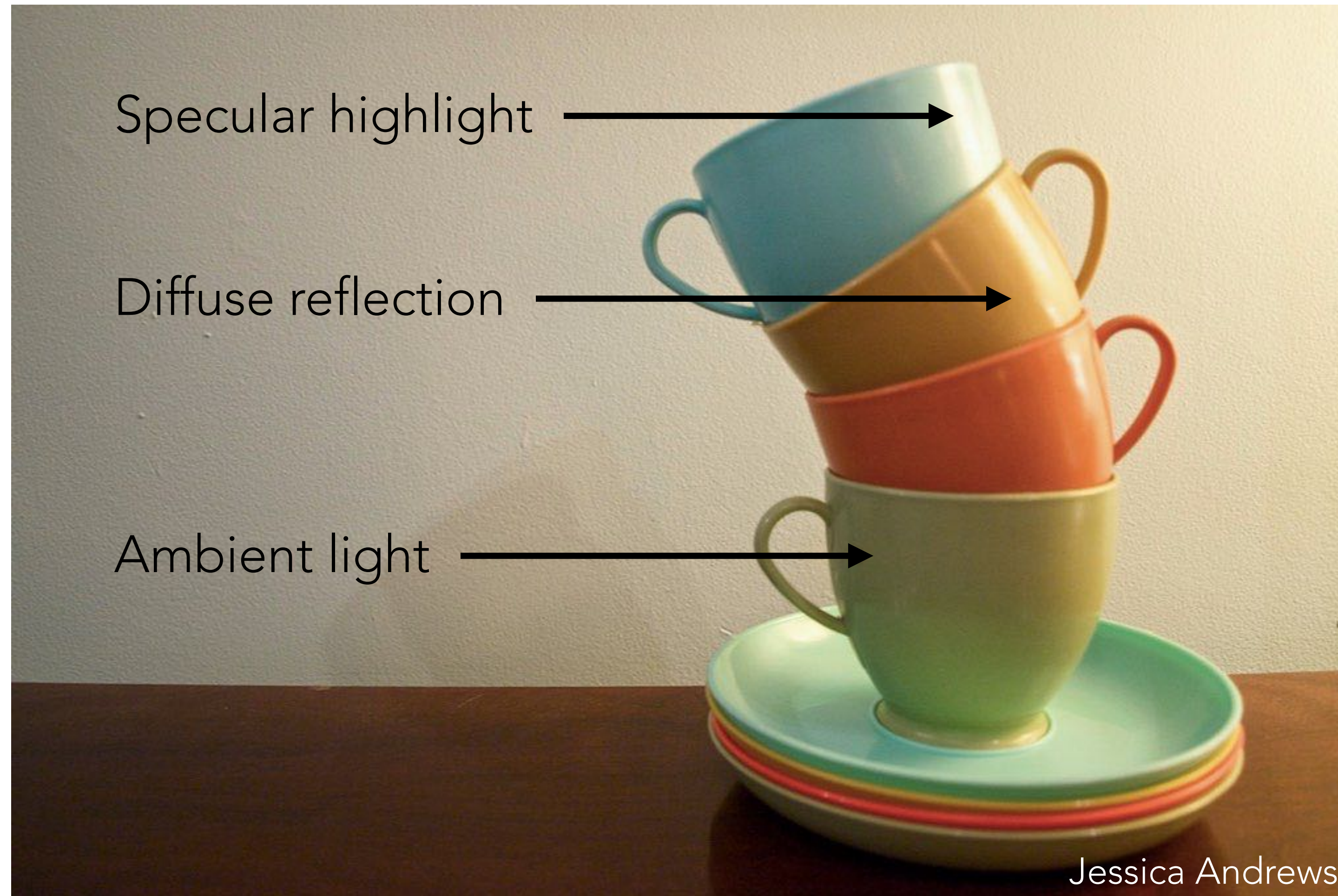






For realistic materials, this can be pretty complicated...

# Today: a very simple shading model



# Diffuse reflection: Lambertian model

Assume the surface scatters the received light equally in all directions, i.e. the shaded colour is independent of view direction  $\mathbf{v}$ .

But how much light is received?

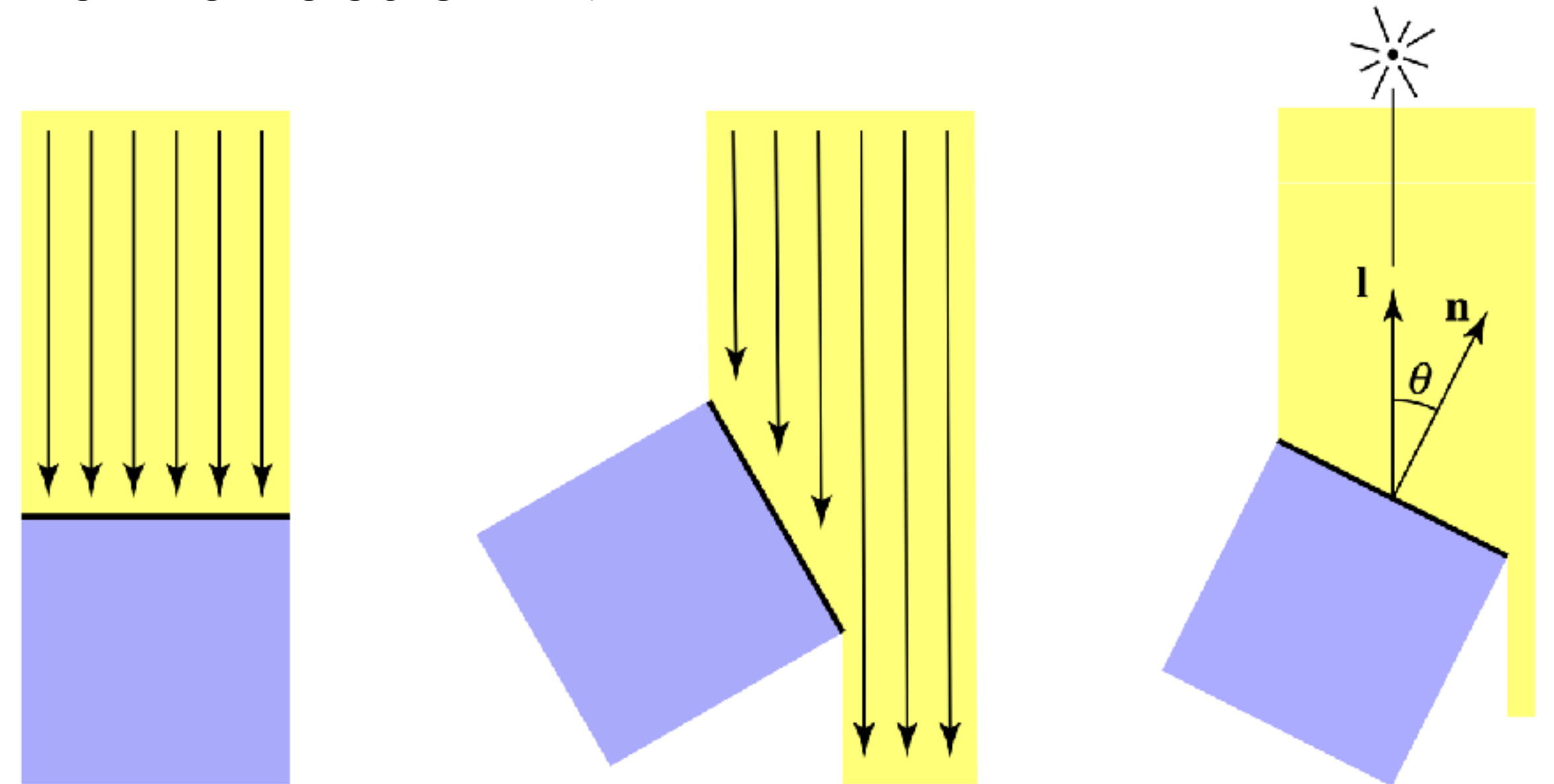
Light **per unit area**  $\propto \cos \theta = \mathbf{n} \cdot \boldsymbol{\ell}$

So, reflected light:

$$L_d = k_d I \max(0, \mathbf{n} \cdot \boldsymbol{\ell})$$

diffuse coefficient

incident light



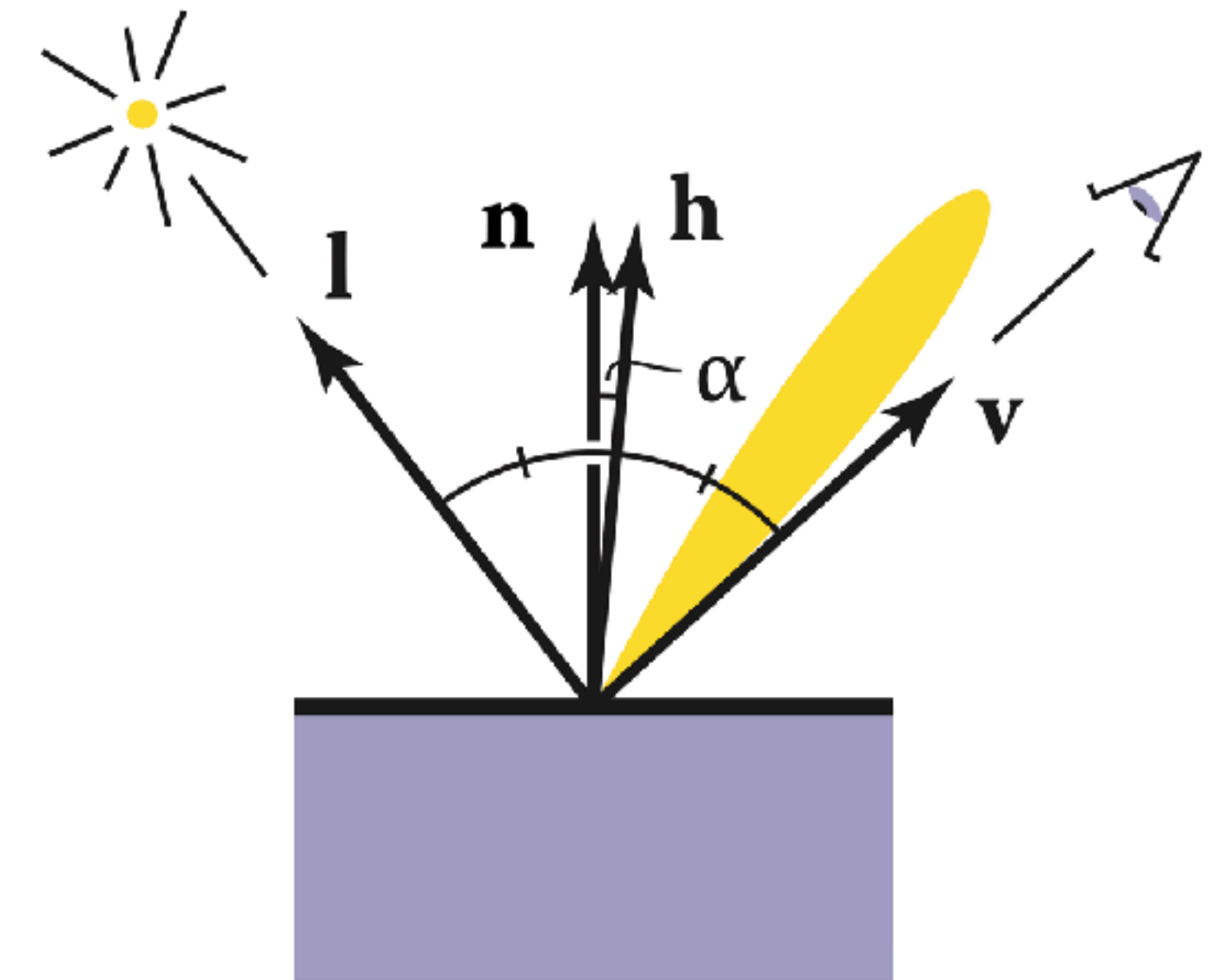
Both  $k_d$  and  $I$  can (should!) be RGB colours: multiplied componentwise

# Specular reflection: Blinn-Phong model

**Perfect mirror:** Reflection is bright if and only if  $\mathbf{v}$  is exactly "opposite" to  $\ell$

$$\text{bisector}(\mathbf{v}, \ell) = \mathbf{n}$$

**Shiny surface:** Reflection is bright if  $\mathbf{v}$  is **close to** being opposite to  $\ell$



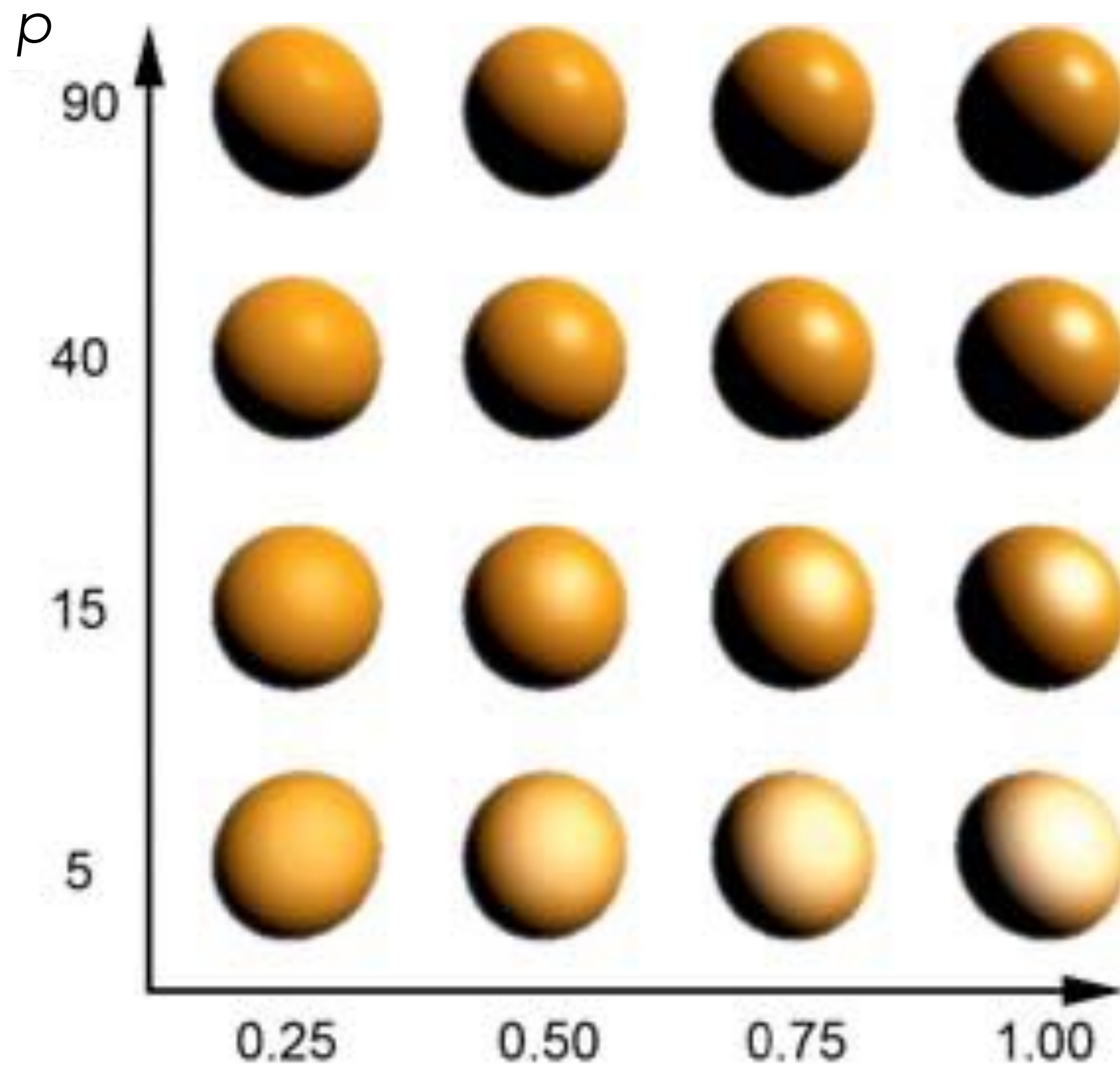
$$\mathbf{h} = \text{bisector}(\mathbf{v}, \ell) = \frac{\mathbf{v} + \mathbf{l}}{\|\mathbf{v} + \mathbf{l}\|}$$

halfway vector

$$L_s = k_s I \max(0, \mathbf{n} \cdot \mathbf{h})^p$$

specular coefficient

Phong exponent



Hughes et al.

$k_s$

Light is coming from the right. Why isn't the left side totally black?



Light is coming from the right. Why isn't the left side totally black?

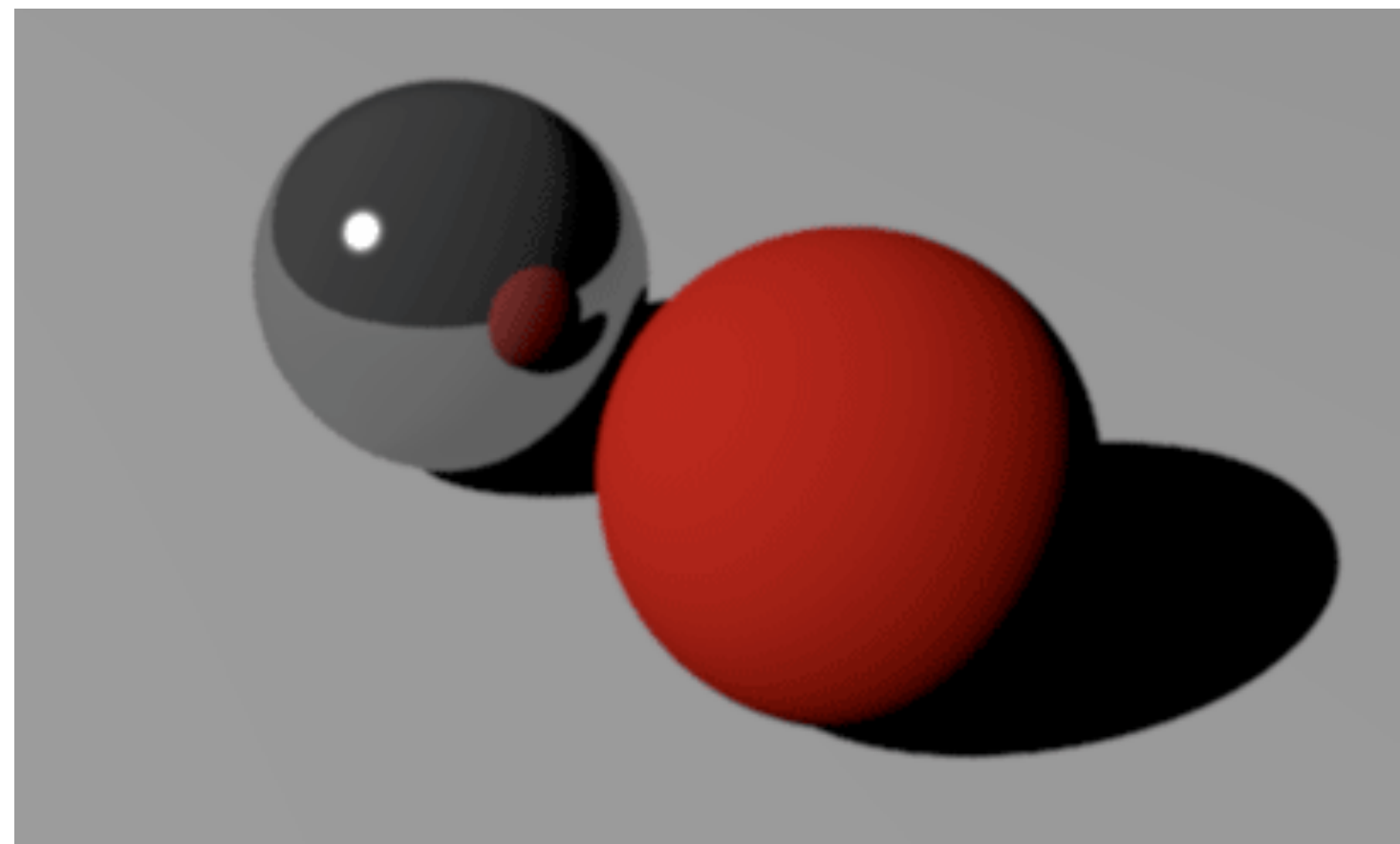


# Ambient light

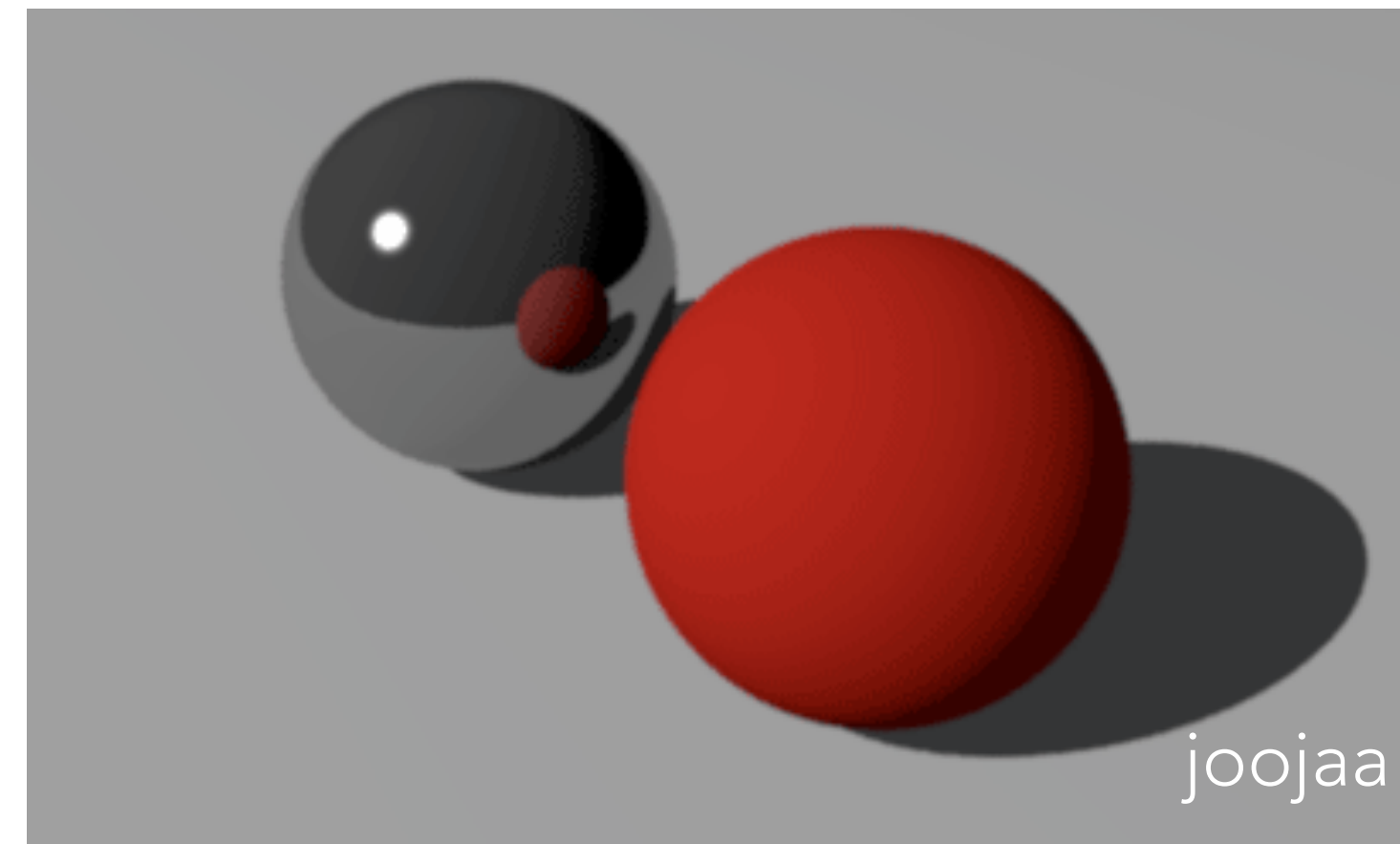
Light bounced around the scene is **nonlocal**: can't compute from  $\mathbf{v}$ ,  $\mathbf{n}$ ,  $\ell$  only

Instead, just assume there is a constant amount of indirect lighting everywhere

$$L_a = k_a I_a$$

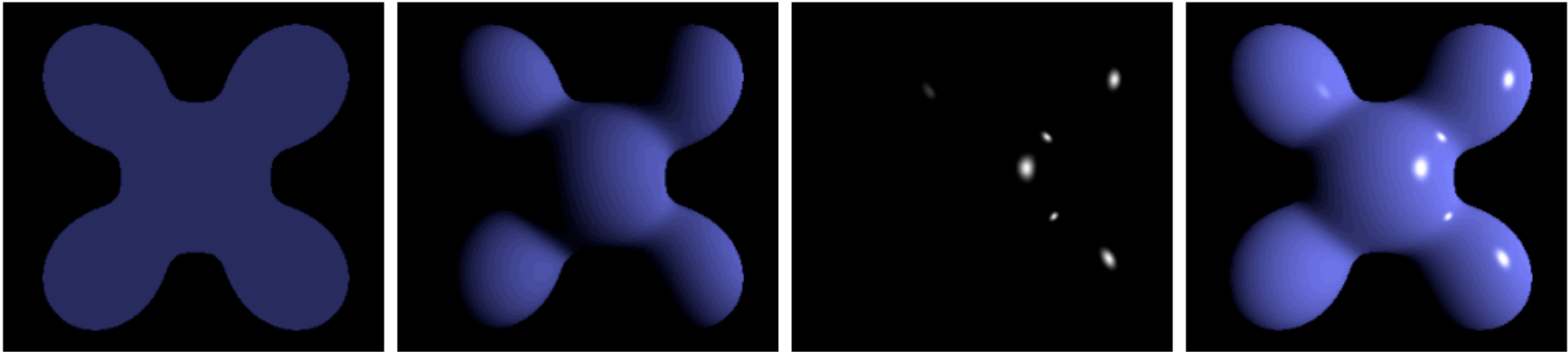


Without ambient light



With ambient light





Ambient + Diffuse + Specular = **Blinn-Phong**  
reflectance model

$$\begin{aligned} L &= L_a + L_d + L_s \\ &= k_a I_a + k_d I \max(0, \mathbf{n} \cdot \boldsymbol{\ell}) + k_s I \max(0, \mathbf{n} \cdot \mathbf{h})^p \end{aligned}$$

$k_a$ ,  $k_d$ ,  $k_s$  (colours) and  $p$  (scalar) control the material's appearance

If multiple lights, add up diffuse and specular contributions for each light

# What phenomena are not captured?

