# CS105L: Discrete Structures I semester, 2006-07 

Homework \# 5
Due before class on Thursday, September 14th, 2006

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September 10, 2006

|  | 6 |  | 1 |  | 4 |  | 5 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 8 | 3 |  | 5 | 6 |  |  |
| 2 |  |  |  |  |  |  |  | 1 |
| 8 |  |  | 4 |  | 7 |  |  | 6 |
|  |  | 6 |  |  |  | 3 |  |  |
| 7 |  |  | 9 |  | 1 |  |  | 4 |
| 5 |  |  |  |  |  |  |  | 2 |
|  |  | 7 | 2 |  | 6 | 9 |  |  |
|  | 4 |  | 5 |  | 8 |  | 7 |  |

Figure 1: The rules of sudoku: Fill in the grid so that each row, each column and each of the $3 \times 3$ boxes marked contain all the digits 1 through 9 . Warning: the sudoku in the figure has not been checked for correctness.

- Each solution must be fully argued. Simply writing the answer will be marked with a 0 even if the answer is correct.
- We will number the rows of the Sudoku grid 1 to 9 from top to bottom and number the columns 1 to 9 from left to right. The boxes will be numbered left to right column by column i.e. the top left box will be box 1 , immediately to it's right will be box 2 , immediately below it will be box 4 and so on.
- When we say a row, column or box is filled we mean it is filled feasibly i.e. according to the rules of Sudoku.

1. Given that row 1 has been filled, how many ways are there of filling row 2 ?
2. Given that row 3 has been filled, how many ways are there of filling row 4 ?
3. Given that box 1 has been filled, how many ways are there of filling box 2 ?
4. Given that box 1 and box 2 have been filled, how many ways are there of filling box 3 ?
5. Given that box 1 and box 2 have been filled, how many ways are there of filling box 6 ?
