

CS105L: Discrete Structures
I semester, 2006-07

Homework # 11

Due before class on **Friday, November 17, 2006**

Instructor: Amitabha Bagchi

November 9, 2006

1. Let G be a 2-connected graph but not a triangle, and let e be an edge of G . Show that either $G - e$ or G/e is again 2-connected.
2. (a) Show that every cubic 3-edge connected graph is 3 connected.
(b) Show that a graph is cubic and 3-connected if and only if it can be constructed from a K^4 by successive applications of the following operation: subdivide two edges by inserting a new vertex on each of them, and join the two new subdividing vertices by an edge.
3. For $k \geq 2$ show that every k -connected graph of order at least $2k$ contains a cycle of length at least $2k$.