1. Consider the following greedy algorithm for the minimum makespan problem discussed in class:

Sort the jobs in decreasing order of their duration. Consider jobs in this order and schedule a job on a machine with the smallest current load.

By a simple argument, you can show that the above algorithm gives a 3/2 approximation factor. You have to use a more clever argument to show that this algorithm gives a  $\left(\frac{4}{3} - \frac{1}{3m}\right)$  approximation factor.

2. Given a sorted array A containing distinct integers, you want to find if there is an index such that A[i] = i. Design an algorithm.