CSL 105: Discrete Mathematical Structures Instructor: Ragesh Jaiswal

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- 1. Discuss Homework-3 and Minor-2 problems.
- 2. Six swimmers training together either swam in a race or watched the others swim. At least how many races must have been scheduled if every swimmer had opportunity to watch all of the others?
- 3. Consider the following two theorems:

Theorem 1 (Permutation with indistinguishable objects) The number of different permutations of n objects, where there are n_1 indistinguishable objects of type 1, n_2 indistinguishable objects of type 2, ..., and n_k indistinguishable objects of type k, is

$$\frac{n!}{n_1!n_2!\dots n_k!}$$

Theorem 2 (Distinguishable objects into distinguishable boxes) The number of ways to distribute n distinguishable objects into k distinguishable boxes so that n_i objects are placed into box i, i = 1, 2, ..., k, equals

$$\frac{n!}{n_1!n_2!\dots n_k!}$$

Prove the second theorem by first setting up a one-to-one correspondence between permutations of n objects with n_i indistinguishable objects of type i, i = 1, 2, ..., k and the distribution of n objects in k boxes such that n_i objects are placed in box i, i = 1, 2, ..., kand then applying the first theorem.

- 4. In how many ways can you place n distinguishable objects into k indistinguishable boxes?
- 5. In how many ways can you place n indistinguishable objects into k indistinguishable boxes?