Regular Expressions and Finite State Automata

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(Based on slides by Jurafsky & Martin, Julia Hirschberg)

Regular Expressions and Text Searching

- Everybody does it
 - Emacs, vi, perl, grep, etc..
- Regular expressions are a compact textual representation of a set of strings representing a language.

RE	Example Patterns Matched	
/woodchucks/	"interesting links to woodchucks and lemurs"	
/a/	"Mary Ann stopped by Mona's"	
/Claire_says,/	" "Dagmar, my gift please," Claire says,"	
/DOROTHY/	"SURRENDER DOROTHY"	
/1/	"You've left the burglar behind again!" said Nori	

RE	Match	Example Patterns
/[wW]oodchuck/	Woodchuck or woodchuck	" <u>Woodchuck</u> "
/[abc]/	'a', 'b', <i>or</i> 'c'	"In uomini, in sold <u>a</u> ti"
/[1234567890]/	any digit	"plenty of <u>7</u> to 5"

RE	Match	Example Patterns Matched
/[A-Z]/	an upper case letter	"we should call it ' <u>D</u> renched Blossoms' "
/[a-z]/	a lower case letter	"my beans were impatient to be hoed!"
/[0-9]/	a single digit	"Chapter <u>1</u> : Down the Rabbit Hole"

RE	Match (single characters)	Example Patterns Matched
[^A-Z]	not an upper case letter	"Oyfn pripetchik"
[^Ss]	neither 'S' nor 's'	"I have no exquisite reason for't"
[^\.]	not a period	" <u>o</u> ur resident Djinn"
[e^]	either 'e' or '^'	"look up _ now"
a^b	the pattern 'a^b'	"look up <u>a^ b</u> now"

Regular Expressions: ? * + .

Pattern	Matches	
colou?r	Optional previous char	<u>color</u> <u>colour</u>
oo*h!	0 or more of previous char	<u>oh! ooh! oooh! ooooh!</u>
o+h!	1 or more of previous char	<u>oh! ooh! oooh! ooooh!</u>
baa+		<u>baa baaa baaaa baaaaa</u>
beg.n		<u>begin begun begun beg3n</u>



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Regular Expressions: Anchors

Pattern	Matches
^[A-Z]	<u>P</u> alo Alto
^[^A-Za-z]	<u>1</u> <u>"</u> Hello"
\.\$	The end.
.\$	The end? The end!

RE	Expansion	Match	Examples
\d	[0-9]	any digit	Party_of_ <u>5</u>
\D	[^0-9]	any non-digit	Blue_moon
\w	[a-zA-Z0-9_]	any alphanumeric/underscore	<u>D</u> aiyu
$\setminus W$	[^\w]	a non-alphanumeric	<u>!</u> !!!
\s	[_\r\t\n\f]	whitespace (space, tab)	
\S	[^\s]	Non-whitespace	in_Concord

RE	Match	Example Patterns Matched
*	an asterisk "*"	"K <u>*</u> A*P*L*A*N"
١.	a period "."	"Dr. Livingston, I presume"
\?	a question mark	"Why don't they come and lend a hand?"
\n	a newline	
\t	a tab	

- Find all the instances of the word "the" in a text.
 - /the/
 - / [tT]he/
 - /\b[tT]he\b/
 - [^a-zA-Z] [tT]he[^a-zA-Z]
 - (^|[^a-zA-Z])[tT]he(\$|[^a-zA-Z])

Errors

- The process we just went through was based on two fixing kinds of errors
 - Matching strings that we should not have matched (there, then, other)
 - False positives (Type I)
 - Not matching things that we should have matched (The)
 - False negatives (Type II)

Errors

- We'll be telling the same story for many tasks, all semester. Reducing the error rate for an application often involves two antagonistic efforts:
 - Increasing accuracy, or precision, (minimizing false positives)
 - Increasing coverage, or recall, (minimizing false negatives).

Precision & Recall

	Predicted		
ıal		" P "	"N"
Actu	Р	ТР	FN
7	Ν	FP	TN

Precision = TP/(TP+FP) Recall = TP/(TP+FN) F-measure = 2pr/(p+r)

$$F_eta = (1+eta^2) \cdot rac{ ext{precision} \cdot ext{recall}}{(eta^2 \cdot ext{precision}) + ext{recall}}$$

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Finite State Automata

 Regular expressions can be viewed as a textual way of specifying the structure of finite-state automata.

FSAs as Graphs

Let's start with the sheep language /baa+!/



Sheep FSA

- We can say the following things about this machine
 - It has 5 states
 - b, a, and ! are in its alphabet
 - q₀ is the start state
 - q₄ is an accept state
 - It has 5 transitions



But Note

• There are other machines that correspond to this same language





Finite State Automata (FSAs)

A finite-state automaton $M = \langle Q, \Sigma, q_0, F, \delta \rangle$ consists of:

- A finite set of states $Q = \{q_0, q_1, ..., q_n\}$
- A finite alphabet Σ of input symbols (e.g. Σ = {a, b, c,...})
- A designated start state $q_0 \in Q$
- A set of final states $F \subseteq Q$
- A transition function δ:
 - The transition function for a deterministic (D)FSA: $Q \times \Sigma \to Q$ $\delta(q,w) = q'$ for $q, q' \in Q, w \in \Sigma$

If the current state is q and the current input is w, go to q'

- The transition function for a nondeterministic (N)FSA: $Q \times \Sigma \rightarrow 2^Q$

 $\delta(q,w) = Q' \qquad \text{for } q \in Q, \ Q' \subseteq Q, \ w \in \Sigma$

If the current state is q and the current input is w, go to any $q' \in Q'$

Dollars and Cents



Dollars and Cents



Yet Another View





Recognition

- Recognition is the process of determining if a string should be accepted by a machine
- Or... it's the process of determining if a string is in the language we're defining with the machine
- Or... it's the process of determining if a regular expression matches a string
- Those all amount the same thing in the end

Recognition

- Simply a process of starting in the start state
- Examining the current input
- Consulting the table
- Going to a new state and updating the input pointer.
- Until you run out of input.

D-Recognize

function D-RECOGNIZE(tape, machine) returns accept or reject

```
index \leftarrow Beginning of tape
current-state — Initial state of machine
loop
 if End of input has been reached then
  if current-state is an accept state then
    return accept
  else
     return reject
 elsif transition-table[current-state,tape[index]] is empty then
    return reject
 else
    current-state \leftarrow transition-table[current-state,tape[index]]
    index \leftarrow index + 1
```

end

Key Points

- Deterministic means that at each point in processing there is always one unique thing to do (no choices).
- D-recognize is a simple table-driven interpreter
- The algorithm is universal for all unambiguous regular languages.
 - To change the machine, you simply change the table.

Generative Formalisms

- Formal Languages consist of words whose letters are taken from an alphabet and are well-formed according to a specific set of rules
- Finite-state automata define formal languages (without having to enumerate all the strings in the language)
- The term *Generative* is based on the view that you can run the machine as a generator to get strings from the language.

Generative Formalisms

- FSAs can be viewed from two perspectives:
 - Acceptors that can tell you if a string is in the language
 - Generators to produce *all and only* the strings in the language

Non-Determinism





Non-Determinism cont.

- Yet another technique
 - Epsilon transitions
 - Key point: these transitions do not examine or advance the tape during recognition



Equivalence

- Non-deterministic machines can be converted to deterministic ones with a fairly simple construction
- That means that they have the same power; non-deterministic machines are not more powerful than deterministic ones in terms of the languages they can accept

ND Recognition

- Two basic approaches (used in all major implementations of regular expressions, see Friedl 2006)
 - Either take a ND machine and convert it to a D machine and then do recognition with that.
 - 2. Or explicitly manage the process of recognition as a state-space search (leaving the machine as is).





















Key Points

- States in the search space are pairings of tape positions and states in the machine.
- By keeping track of as yet unexplored states, a recognizer can systematically explore all the paths through the machine given an input.

Uses of Regexes

- Observing simple subcomponents
 - Dollars and cents
 - Date, Time
 - Chemical compounds
 - Mathematical formulas
 - Word search in crossword puzzles
 - Noun compounds, Lexico-POS patterns
- Use regexes in low-data setting
- Use regexes as features in ML

Summing Up

- Regular expressions and FSAs can represent subsets of natural language as well as regular languages
 - Both representations may be difficult for humans to use for any real subset of a language
 - But quick, powerful and easy to use for small problems
- Finite state transducers and rules are common ways to incorporate linguistic ideas in NLP for small applications
- Particularly useful for no data setting