


# Sequence Labeling

Neural CRFs & Learning with Constraints

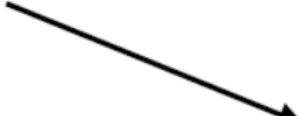
Mausam

# Types of Prediction Tasks


- Two classes (**binary classification**)

I hate this movie  positive  
negative

- Multiple classes (**multi-class classification**)

I hate this movie  very good  
good  
neutral  
bad  
very bad

- Exponential/infinite labels (**structured prediction**)

I hate this movie  PRP VBP DT NN

I hate this movie  *kono eiga ga kirai*

# Sequence problems

- Many problems in NLP have data which is a sequence of characters, words, phrases, lines, or sentences ...
- We can think of our task as one of labeling each item

<b>VBG</b>	<b>NN</b>	<b>IN</b>	<b>DT</b>	<b>NN</b>	<b>IN</b>	<b>NN</b>
Chasing	opportunity	in	an	age	of	upheaval

**POS tagging**

<b>PERS</b>	<b>O</b>	<b>O</b>	<b>O</b>	<b>ORG</b>	<b>ORG</b>
Murdoch	discusses	future	of	News	Corp.

**Named entity recognition**

<b>B</b>	<b>B</b>	<b>I</b>	<b>I</b>	<b>B</b>	<b>I</b>	<b>B</b>	<b>I</b>	<b>B</b>	<b>B</b>
而	相	对	于	这	些	品	牌	的	价

**Word segmentation**



# POS Tagging

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DT NNP NN VBD VBN RP NN NNS

The Georgia branch had taken on loan commitments ...

DT NN IN NN VBD NNS VBD

The average of interbank offered rates plummeted ...

# POS Tagging Ambiguity

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- Words often have more than one POS: *back*
  - The back door = JJ
  - On my back = NN
  - Win the voters back = RB
  - Promised to back the bill = VB
- The POS tagging problem is to determine the POS tag for a particular instance of a word.

# Named Entity Recognition (NER)

- A very important sub-task: **find** and **classify** names in text, for example:
  - The decision by the independent MP Andrew Wilkie to withdraw his support for the minority Labor government sounded dramatic but it should not further threaten its stability. When, after the 2010 election, Wilkie, Rob Oakeshott, Tony Windsor and the Greens agreed to support Labor, they gave just two guarantees: confidence and supply.

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# Named Entity Recognition (NER)

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Person

Date

Location

Organi-  
zation



# The Named Entity Recognition Task

Task: Predict entities in a text

Foreign	ORG	
Ministry	ORG	
spokesman	O	
Shen	PER	} Standard evaluation is per entity, <i>not</i> per token
Guofang	PER	
told	O	
Reuters	ORG	
:	O	

# Precision/Recall/F1 for IE/NER

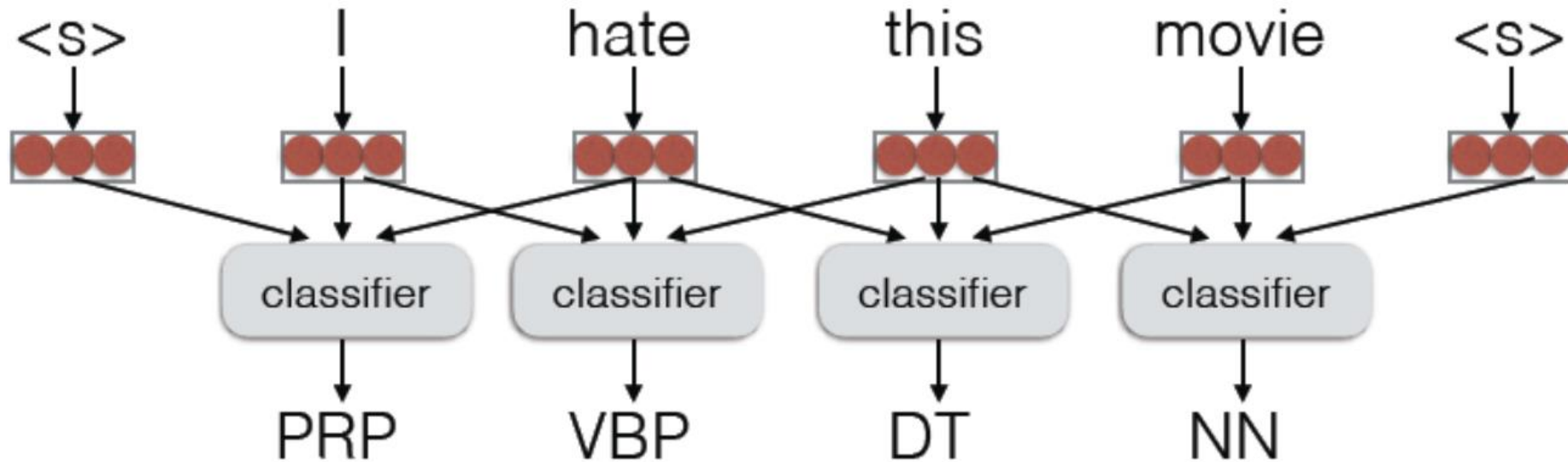
- Recall and precision are straightforward for tasks like IR and text categorization, where there is only one grain size (documents)
- The measure behaves a bit funnily for IE/NER when there are *boundary errors* (which are *common*):
  - First Bank of Chicago announced earnings ...
- This counts as both a fp and a fn
- Selecting *nothing* would have been better
- Some other metrics (e.g., MUC scorer) give partial credit (according to complex rules)

# Encoding classes for NER

	IO encoding	IOB encoding
Fred	PER	B-PER
showed	O	O
Sue	PER	B-PER
Mengqiu	PER	B-PER
Huang	PER	I-PER
's	O	O
new	O	O
painting	O	O

Practically negligible differences in performance. BIO is more standard..

# Sequence Labeling as Independent Classification

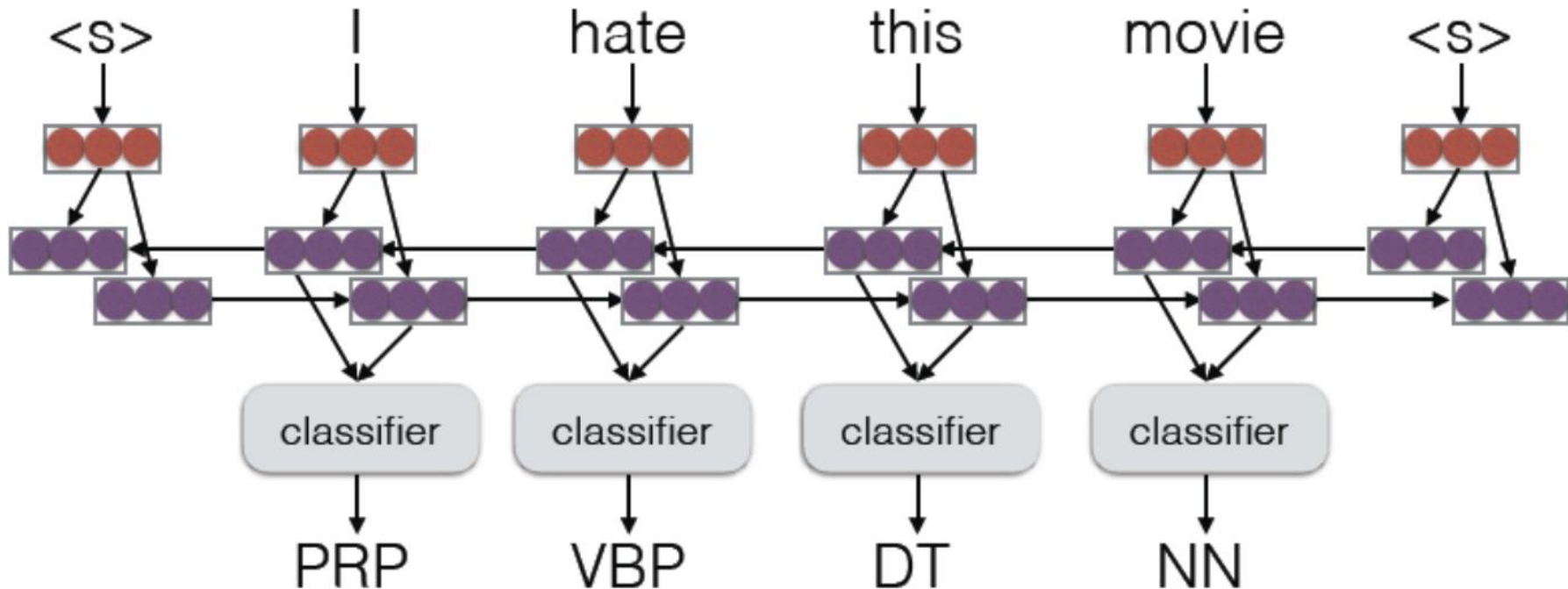


Structured Prediction task

But not a Structured Prediction Model

Instead: independent multi-class classification

# Sequence Labeling with BiLSTM / Transformer



What is missing?

Still not modeling output structure!

Outputs are independent (of each other)

# Why Model Interactions in Output?

- Consistency is important!

time	flies	like	an	arrow	
NN	VBZ	IN	DT	NN	(time moves similarly to an arrow)
NN	NNS	VB	DT	NN	("time flies" are fond of arrows)
VB	NNS	IN	DT	NN	(please measure the time of flies similarly to how an arrow would)
		↓			
NN	NNS	IN	DT	NN	("time flies" that are similar to an arrow)

- Example 2: Paris Hilton

# Conditional Random Fields

- Models w/ Local Dependencies
- Some independence assumptions on the output space, but not entirely independent (local dependencies)
- Exact and optimal decoding/training via dynamic programs

# Local vs Global Normalization

- **Locally normalized models:** each decision made by the model has a probability that adds to one

$$P(Y | X) = \prod_{j=1}^{|Y|} \frac{e^{S(y_j | X, y_1, \dots, y_{j-1})}}{\sum_{\tilde{y}_j \in V} e^{S(\tilde{y}_j | X, y_1, \dots, y_{j-1})}}$$

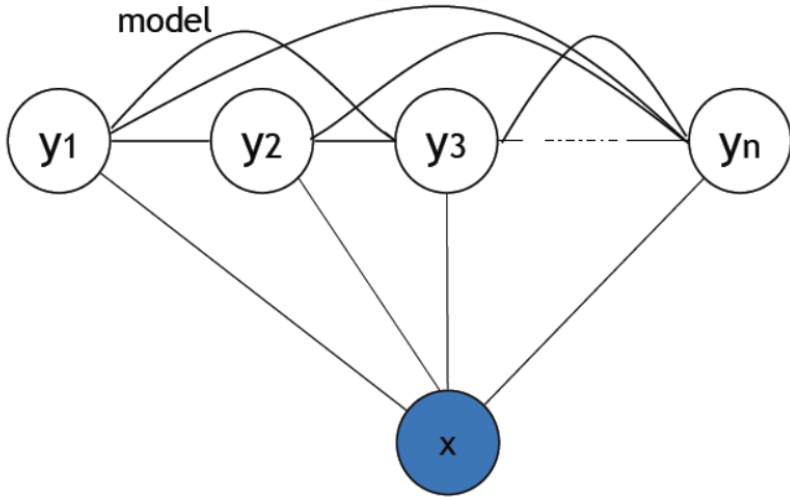
- **Globally normalized models (a.k.a. energy-based models):** each sequence has a score, which is not normalized over a particular decision

$$P(Y | X) = \frac{e^{\sum_{j=1}^{|Y|} S(y_j | X, y_1, \dots, y_{j-1})}}{\sum_{\tilde{Y} \in V_*} e^{\sum_{j=1}^{|\tilde{Y}|} S(\tilde{y}_j | X, \tilde{y}_1, \dots, \tilde{y}_{j-1})}}$$



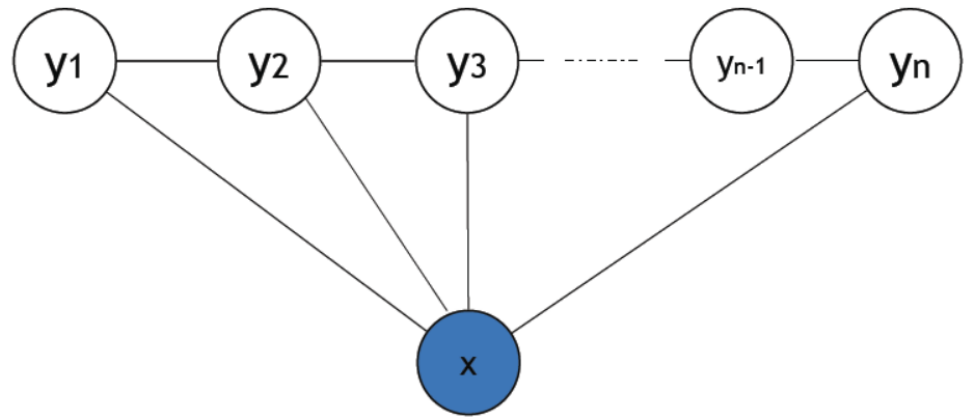
# CRFs

General form of globally normalized model



$$P(Y|X) = \frac{\psi(Y, X)}{\sum_{Y'} \psi(Y', X)}$$

First-order linear CRF



$$P(Y|X) = \frac{\prod_{i=1}^L \psi_i(y_{i-1}, y_i, X)}{\sum_{Y'} \prod_{i=1}^L \psi_i(y'_{i-1}, y'_i, X)}$$

# Potential Functions

$$\psi_i(y_{i-1}, y_i, X) = \exp(\overset{\text{"Transition"}}{W^T T(y_{i-1}, y_i, X, i)} + \overset{\text{"Emission"}}{U^T S(y_i, X, i)} + b_{y_{i-1}, y_i})$$

- Using neural features in DNN:

$$\psi_i(y_{i-1}, y_i, X) = \exp(W_{y_{i-1}, y_i}^T F(X, i) + U_{y_i}^T F(X, i) + b_{y_{i-1}, y_i})$$

- Number of parameters:  $O(|Y|^2 d_F)$

- Simpler version:

$$\psi_i(y_{i-1}, y_i, X) = \exp(W_{y_{i-1}, y_i} + U_{y_i}^T F(X, i) + b)$$

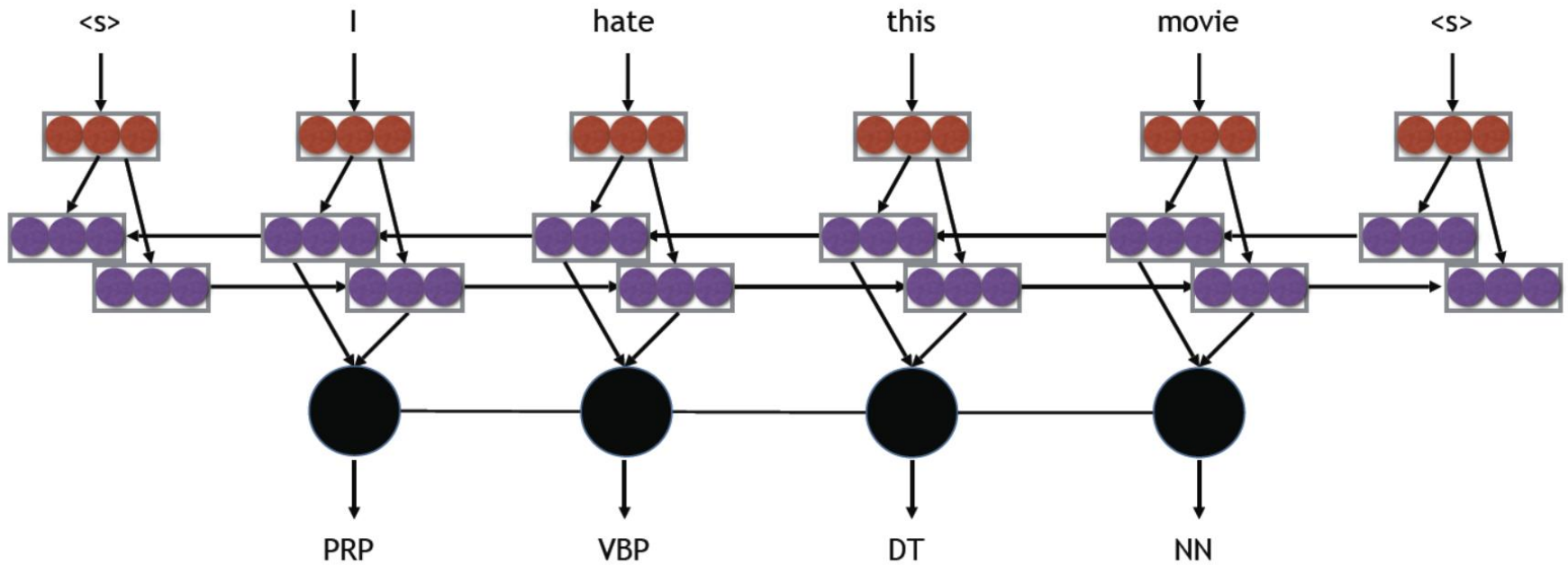
- Number of parameters:  $O(|Y|^2 + |Y|d_F)$

# Linear Chain CRF (in practice)

$$\psi_i(y_{i-1}, y_i, X) = \exp(W_{y_{i-1}, y_i} + U_{y_i}^T F(X, i) + b)$$

- $\text{Score}(X, Y) = \sum_{i=1}^{T+1} W_{[y_{i-1}, y_i]} + \sum_{i=1}^T e(x_i, y_i)$
- For a tagset of  $K$  possible tags,
  - introduce a scoring matrix  $W \in \mathbb{R}^{K \times K}$  in which
  - $W[g, h]$  = compatibility score of the tag sequence  $g$   $h$ .
- Global inference

# BiLSTM-CRF



# Properties

$$Z(X) = \sum_Y \prod_{i=1}^L \psi_i(y_{i-1}, y_i, X)$$

- Each label depends on the input, and the nearby labels
- But given *adjacent* labels, others do not matter
- If we knew the score of every sequence  $y_1, \dots, y_{n-1}$ , we could compute easily the score of sequence  $y_1, \dots, y_{n-1}, y_n$
- So we really only need to know the score of all the sequences ending in **each**  $y_{n-1}$
- Think of that as some “precalculation” that happens before we think about  $y_n$

# Decoding Problem

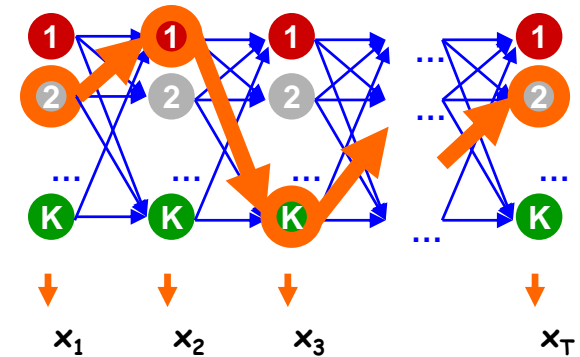
Given  $X=x_1 \dots x_T$ , what is “best” tagging  $Y_1 \dots Y_T$ ?

Several possible meanings of ‘solution’

1. States which are individually most likely
2. Single best state sequence

We want *sequence*  $Y_1 \dots Y_T$ ,  
such that  $P(Y|X)$  is maximized

$$Y^* = \operatorname{argmax}_Y P(Y|X)$$



# Most Likely Sequence

- Problem: find the most likely (Viterbi) sequence under the model
  - Given model parameters, we can score any sequence pair

NNP	VBZ	NN	NNS	CD	NN	.
Fed	raises	interest	rates	0.5	percent	.

- In principle, we're done – list all possible tag sequences, score each one, pick the best one (the Viterbi state sequence)

NNP VBZ NN NNS CD NN → logP = -23

NNP NNS NN NNS CD NN → logP = -29

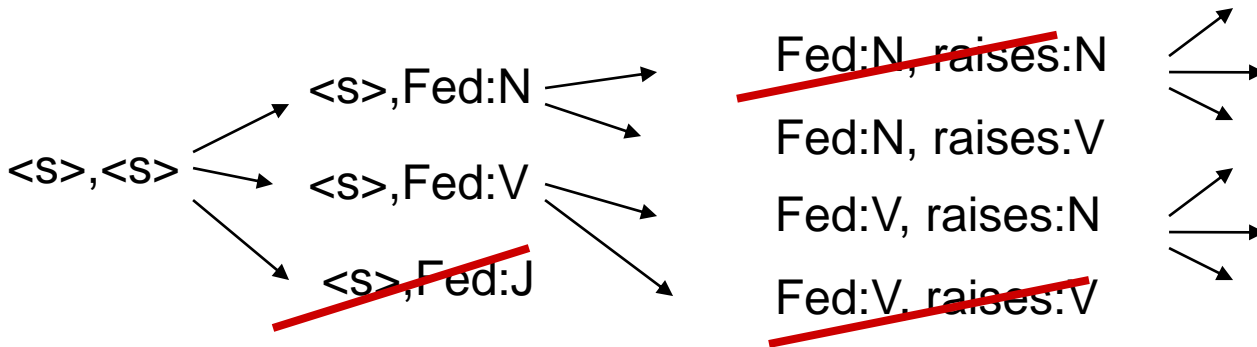
NNP VBZ VB NNS CD NN → logP = -27

**2T+1 operations  
per sequence**

**$|Y|^T$  tag sequences!**

# Finding the Best Trajectory

- Brute Force: Too many trajectories (state sequences) to list
- Option 1: Beam Search

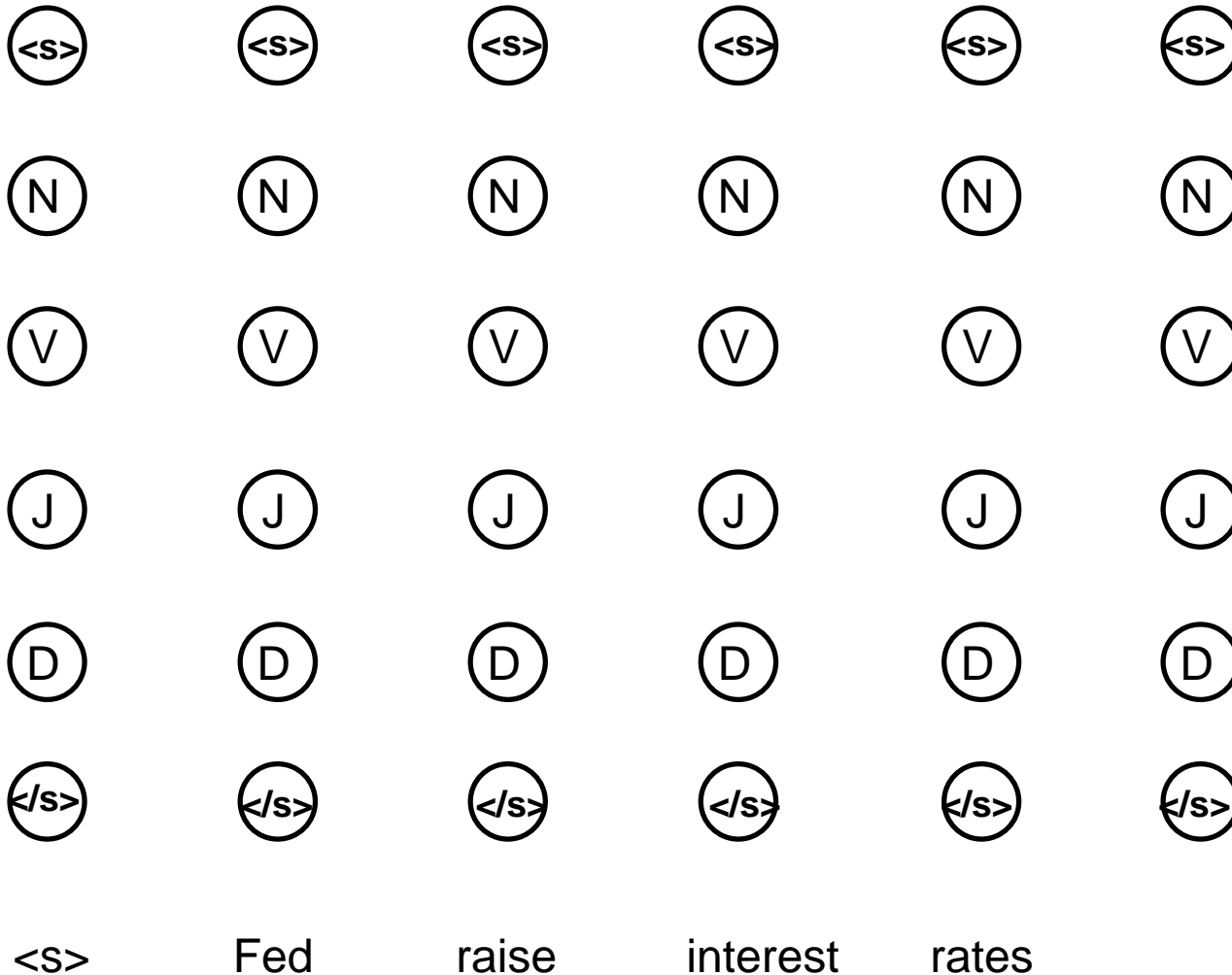


- A beam is a set of partial hypotheses
  - Start with just the single empty trajectory
  - At each derivation step:
    - Consider all continuations of previous hypotheses
    - Discard most, keep top k
- **Beam search works ok in practice**
    - ... but sometimes you want the optimal answer
    - ... and there's often a better option than naïve beams

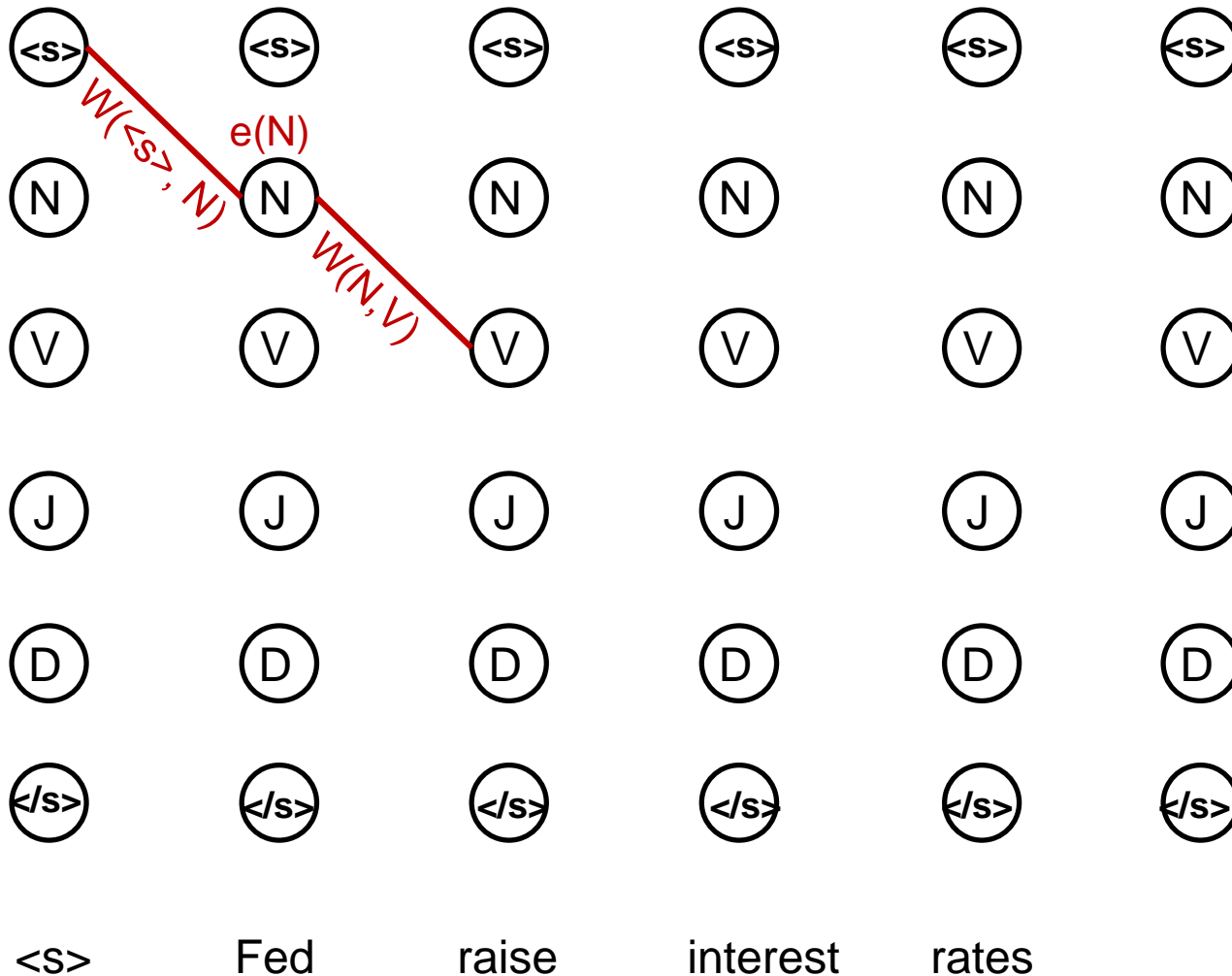


# State Lattice / Trellis

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# State Lattice / Trellis



# Dynamic Programming

- Decoding: 
$$Y^* = \arg \max_Y P(Y | X) = \arg \max_Y \text{score}(X, Y)$$
$$= \arg \max_Y \sum_{t=1}^{T+1} W(y_{t-1}, y_t) + \sum_{t=1}^T e(X, y_t)$$

- First consider how to compute max

- Define 
$$\delta_i(y_i) = \max_{y_{[1:i-1]}} \text{score}(X, y_{[1..i]})$$

- score of **most likely** label sequence ending with tag  $y_i$  at position  $i$ , given words  $x_1, \dots, x_T$

$$\begin{aligned} \delta_i(y_i) &= \max_{y_{[1:i-1]}} e(X, y_i) + W(y_{i-1}, y_i) + \text{score}(X, y_{[1..i-1]}) \\ &= e(X, y_i) + \max_{y_{i-1}} W(y_{i-1}, y_i) + \max_{y_{[1:i-2]}} \text{score}(X, y_{[1..i-1]}) \\ &= e(X, y_i) + \max_{y_{i-1}} W(y_{i-1}, y_i) + \delta_{i-1}(y_{i-1}) \end{aligned}$$

# Viterbi Algorithm

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- Input:  $x_1, \dots, x_T$ ,  $W()$  and  $e()$
- Initialize:  $\delta_0(<s>) = 0$ , and  $-\infty$  for other labels
- For  $i=1$  to  $T$  do
  - For  $(y')$  in all possible tagset

$$\delta_i(y') = e(X, y') + \max_y W(y, y') + \delta_{i-1}(y)$$

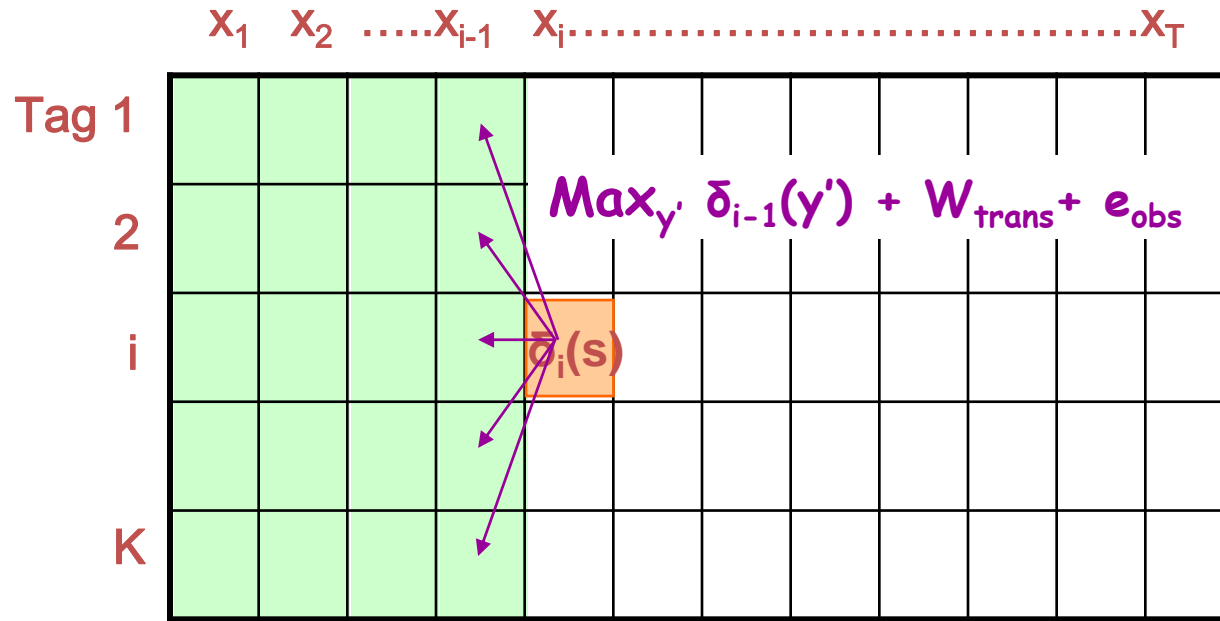
- Return

$$\max_{y'} W(y', </s>) + \delta_T(y')$$

returns only the optimal value

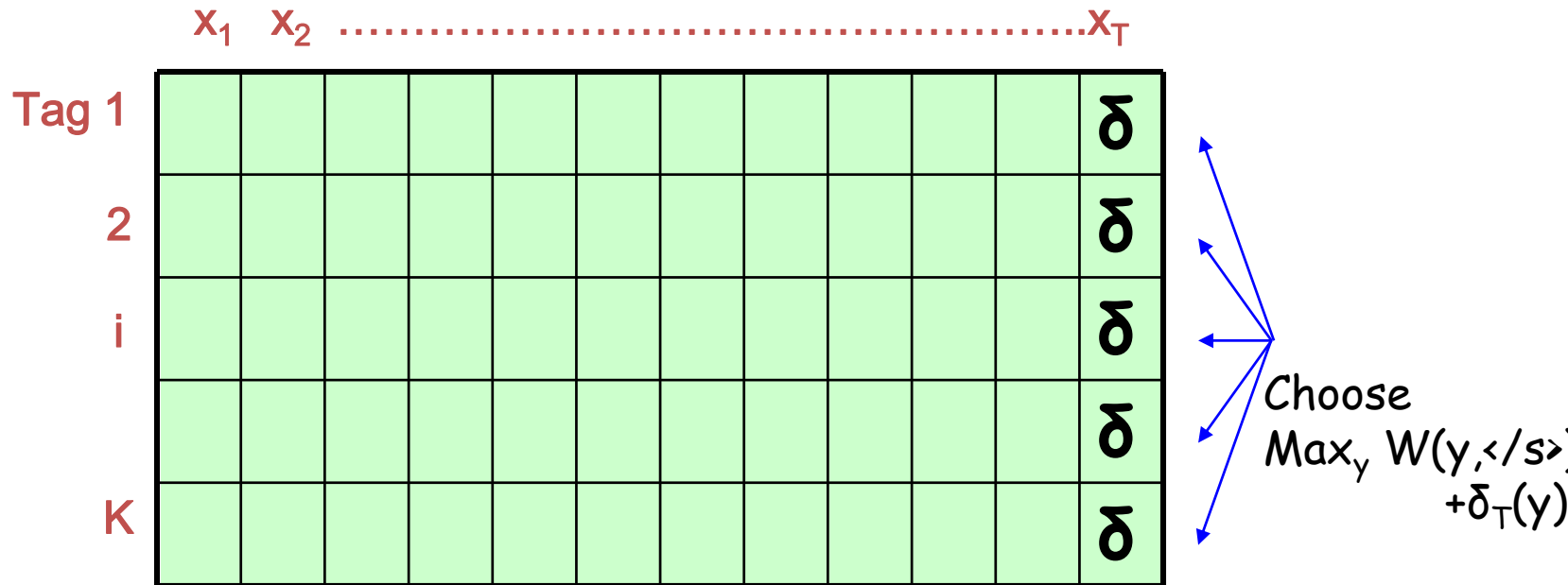
keep backpointers

# Viterbi Algorithm

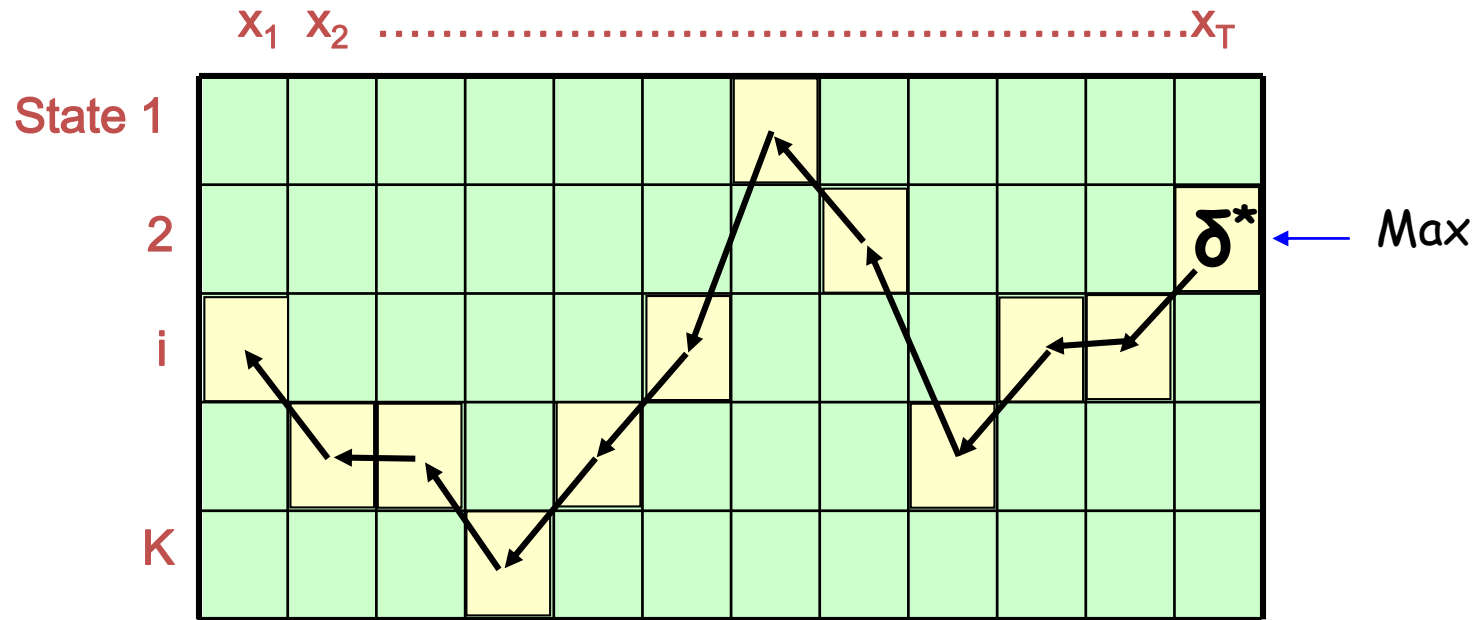


Remember:  $\delta_i(y)$  = score of most likely tag seq ending with  $y$  at time  $i$

# Terminating Viterbi



# Terminating Viterbi



How did we compute  $\delta^*$ ?

$$\text{Max}_{s'} \delta_{T-1}(y') + P_{\text{trans}} + P_{\text{obs}}$$

Now Backchain to Find Final Sequence

Time:  $O(|Y|^2T)$

Space:  $O(|Y|T)$

← Linear in length of sequence

# Training

- Find weights such that

$$Loss(\theta) = -\log P_{CRF}(Y | X; \theta)$$

is maximized

$$P(Y|X) = \frac{\prod_{i=1}^L \psi_i(y_{i-1}, y_i, X)}{\sum_Y \prod_{i=1}^L \psi_i(y'_{i-1}, y'_i, X)}$$

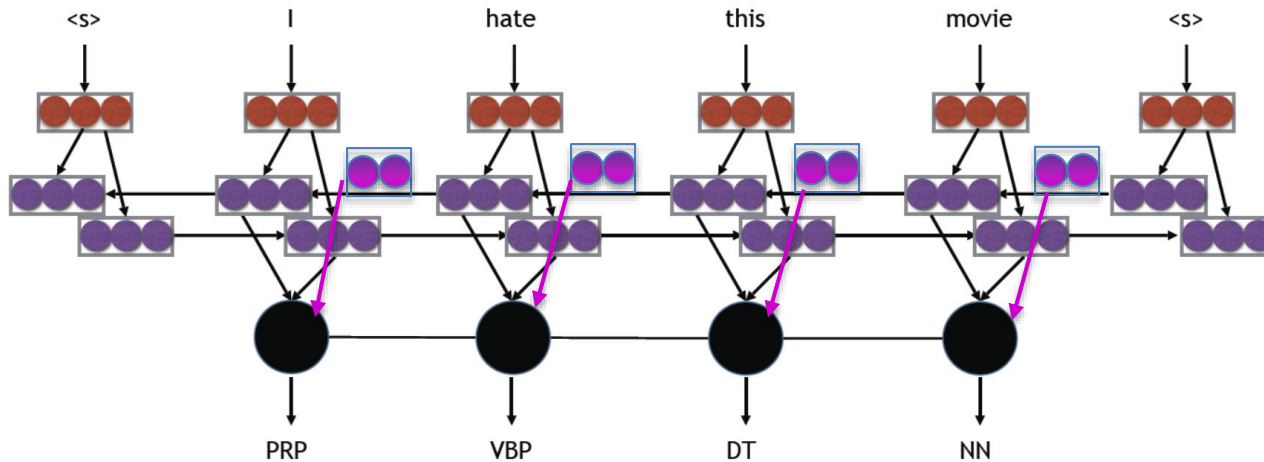
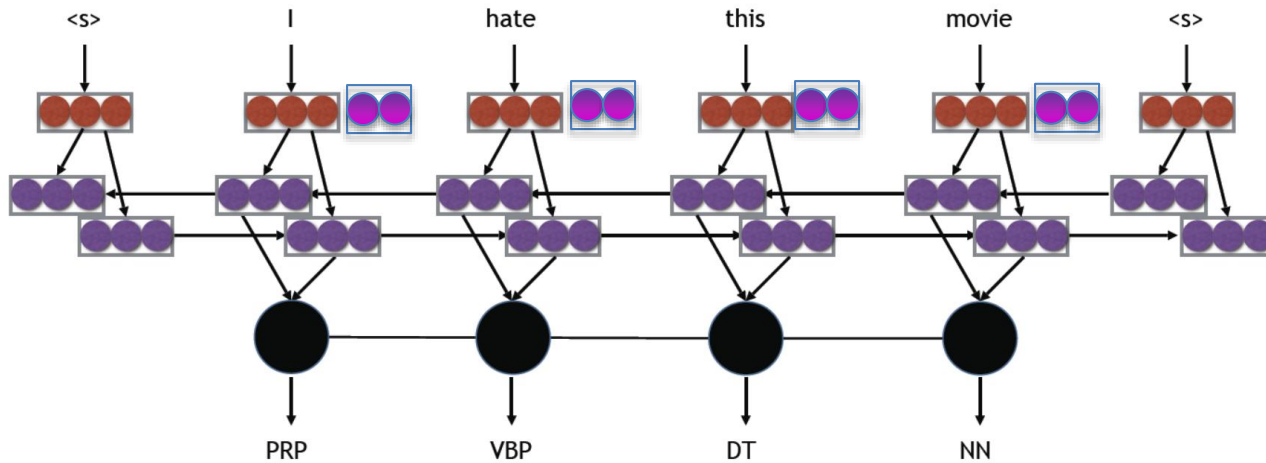
Log\_sum\_exp  
(additive terms)

How to compute partition function?

(backward step handled by autograd)



# BiLSTM-CRF w/ Features



# MSQU: Multi-Sentence Qn Understanding

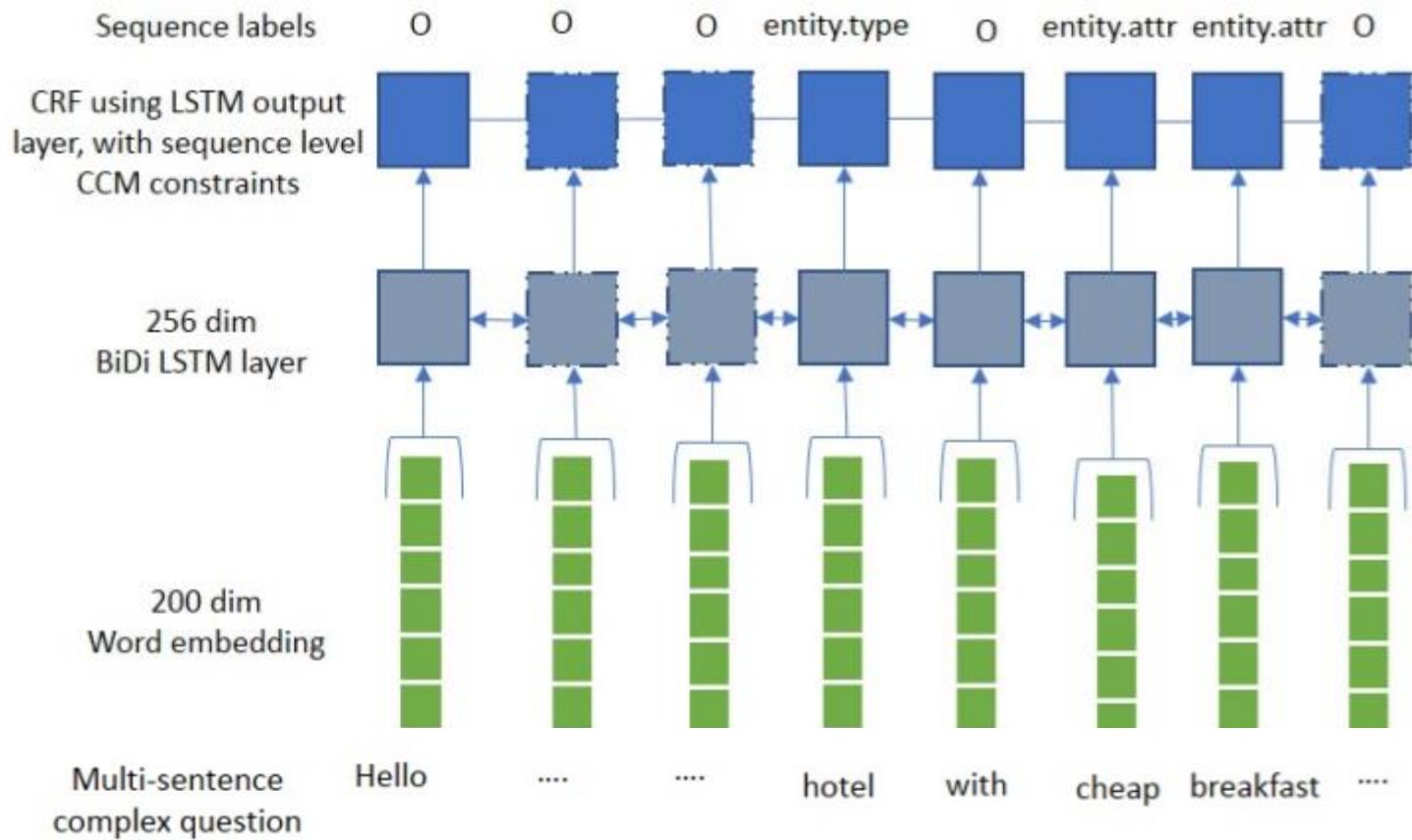
- *“I am taking 15 Scouts to New Zealand over Christmas and New Year. We are spending NYE in Auckland and are looking for suggestions of restaurants (maybe buffet style) which will be suitable for a large group? Ideally close to somewhere where we can watch the fireworks from. Any ideas would be welcome”*



~Open Question Understanding

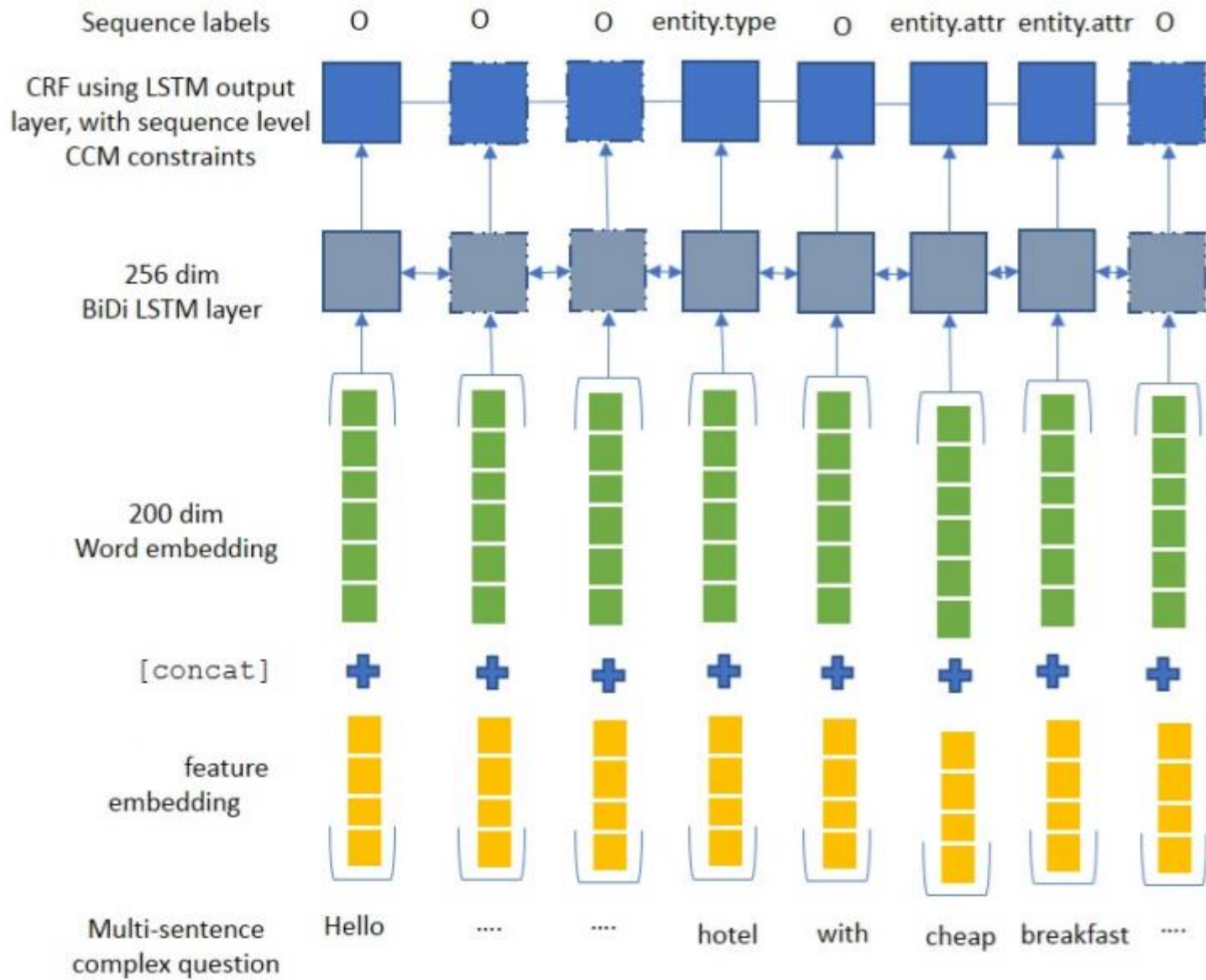
select x where x.type = “restaurant” and  
x.location IN “Auckland” and x.attribute = “buffet style” and  
x.attribute = “suitable for large group” and  
x.attribute PREF “somewhere we can watch fireworks from”

**Key Issue: Only 150 labeled questions!**



# Human Insight: Features!

- Token level features
  - Raw token, lexicalized features, POS Tag, NER Tags
- Hand designed features
  - Indicator features for candidates that are likely to be types based on targets of WH- POS words such as Which, Where etc
  - Indicator features for candidates that are likely to be attributes by checking if there is an edge in the dependency graph leading up to a candidate type.
  - Indicator features for adj-noun phrases
- Cluster ids of word2vec clustered words
- Global word counts in post



# Question Parsing Accuracy

[Contractor, Patra, Mausam, Singla JNLE'21]

Model	F1 (type)	F1 (attribute)	F1 (location)	F1 (macro-avg)
CRF (with Features)	51.4	45.3	55.7	50.8
BiLSTM CRF	53.3	47.6	52.1	51.0
BiLSTM CRF + Features	<b>58.4</b>	<b>48.1</b>	<b>62.0</b>	<b>56.2</b>

Neural + Features > Neural > Symbolic + Features

# Question Parsing Accuracy

[Contractor, Patra, Mausam, Singla JNLE'21]

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CRF	51.4	45.3	55.7	50.8
BiLSTM CRF	53.3	47.6	52.1	51.0
BERT	59.6	50.6	59.5	56.6
BERT + BiLSTM + CRF	<b>63.4</b>	<b>56.5</b>	<b>72.4</b>	<b>64.4</b>

BERT + CRF > BERT

# Summary

- BiLSTM+CRF
  - combines feature engineering of LSTMs
  - global reasoning of CRFs
- When are CRFs helpful?
  - Joint inference
  - Low data setting



# Deep Learning With Constraints

Yatin Nandwani

*Work done in collaboration with*

Abhishek Pathak

*Under the guidance of*

*Prof. Mausam and Prof. Parag Singla*

# Learning with Constraints:

## *Motivation*

→ Modern day AI == Deep Learning (DL) [**Learn from Data**]

# Learning with Constraints:

## *Motivation*

- Modern day AI == Deep Learning (DL) [**Learn from Data**]
- Can we inject symbolic knowledge in Deep Learning? E.g. Person
  - => Noun [**Learn from ~~Data~~ Knowledge**](credit: Vivek S Kumar)

# Learning with Constraints:

## *Motivation*

- Modern day AI == Deep Learning (DL) [Learn from Data]
- Can we inject symbolic knowledge in Deep Learning? E.g. Person  
=> Noun [Learn from ~~Data~~ Knowledge]
- **Constraints:** One of the ways of representing symbolic knowledge.

$$\mathbb{1}\{y_{PER.} = 1\} \implies \mathbb{1}\{y_{Noun.} = 1\}$$

# Learning with Constraints:

## *Motivation*

- **Task:**

Fine Grained Entity Typing

# Learning with Constraints:

## *Motivation*

**Input:**

Bag of Mentions

**Sample Mention:**  
*the United States”*

*“Barack Obama is the President of*

**Output:**

*president, leader,  
politician...*

# Learning with Constraints:

## Motivation

**Input:**

**Sample Mention:**  
*“Barack Obama is the President of the United States”*

**Output:**

*president, leader, politician...*

Bag of Mentions

*“Barack Obama is the President of*

Mention 1

Mention 2

Mention N

**Neural  
Network**

president



leader



politician



sportsman



# Learning with Constraints:

## *Motivation*

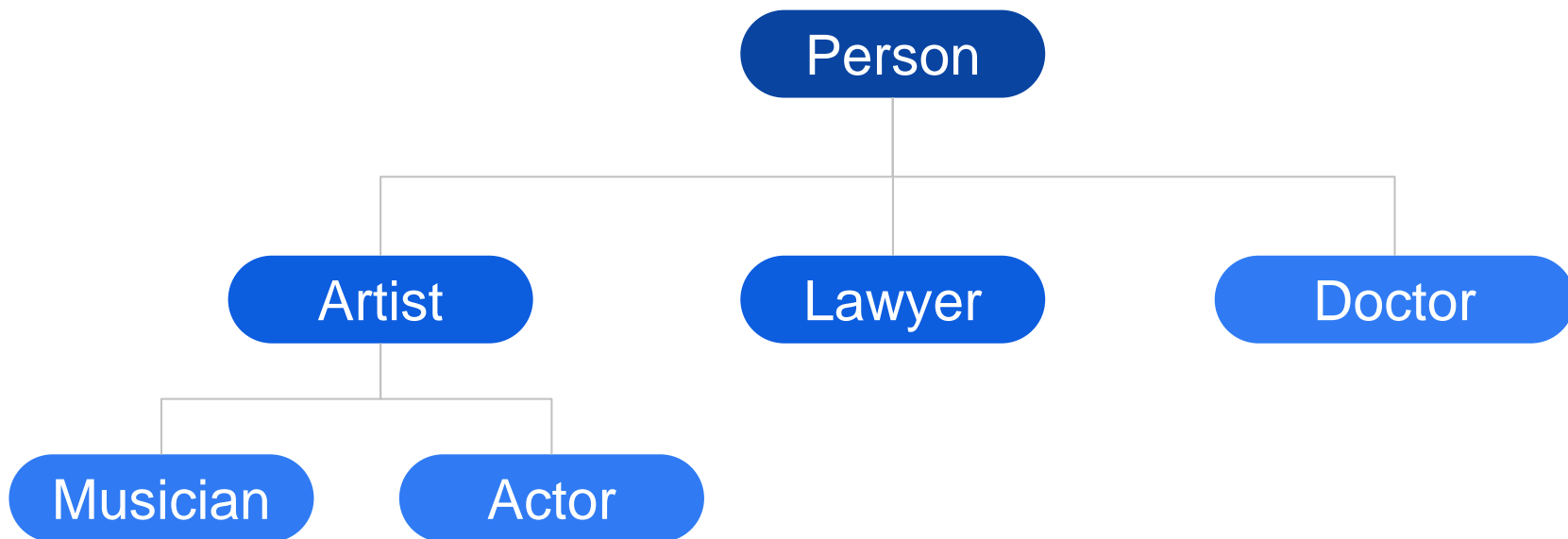
- **Constraints:** Hierarchy on Output label space



# Learning with Constraints:

## *Motivation*

- **Constraints:** Hierarchy on Output label space



# Learning with Constraints:

## *Motivation*

→ Using Soft Logic

$$\mathbb{1}\{y_{ARTIST} = 1\} \implies \mathbb{1}\{y_{PERSON} = 1\}$$

# Learning with Constraints:

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$$(\neg \mathbb{1} \{y_{ARTIST} = 1\}) \vee (\mathbb{1} \{y_{PERSON} = 1\})$$

# Learning with Constraints:

## *Motivation*

### → Using Soft Logic

$$\mathbb{1}\{y_{ARTIST} = 1\} \implies \mathbb{1}\{y_{PERSON} = 1\}$$

$$(\neg \mathbb{1}\{y_{ARTIST} = 1\}) \vee (\mathbb{1}\{y_{PERSON} = 1\})$$

$$(1 - p(y_{ARTIST})) + p(y_{PERSON})$$

# Learning with Constraints:

Re

→

Boolean Expression	T-norm: Choice 1	T-norm: Choice 2
$v$	$p(v = 1)$	
$\neg v$	$1 - p(v = 1)$	
$v_1 \vee v_2$	$\min(p(v_1 = 1) + p(v_2 = 1), 1)$	$\max(p(v_1 = 1), p(v_2 = 1))$
$v_1 \wedge v_2$	$\max(p(v_1 = 1) + p(v_2 = 1) - 1, 0)$	$\min(p(v_1 = 1), p(v_2 = 1))$

$$\mathbb{1} \{y_{ARTIST} = 1\} \implies \mathbb{1} \{y_{PERSON} = 1\}$$

$$(\neg \mathbb{1} \{y_{ARTIST} = 1\}) \vee (\mathbb{1} \{y_{PERSON} = 1\})$$

$$(1 - p(y_{ARTIST})) + p(y_{PERSON})$$

# Learning with Constraints:

## *Representation of Constraints*

$$1 - p(y_{ARTIST}) + p(y_{PERSON}) = 1$$

# Learning with Constraints:

## *Representation of Constraints*

$$1 - p(y_{ARTIST}) + p(y_{PERSON}) = 1$$

$$1 - p(y_{ARTIST}) + p(y_{PERSON}) \geq 1$$

# Learning with Constraints:

## *Representation of Constraints*

$$1 - p(y_{ARTIST}) + p(y_{PERSON}) = 1$$

$$1 - p(y_{ARTIST}) + p(y_{PERSON}) \geq 1$$

**Equivalently:**

$$p(y_{ARTIST}) - p(y_{PERSON}) \leq 0$$



# Learning with Constraints:

## *Representation of Constraints*

**Define:**

$$f_k^i = p(y_{ARTIST}) - p(y_{PERSON})$$

$k^{th}$  Constraint

$i^{th}$  Data point

**Inequality Constraint:**

$$f_k^i \leq 0$$

# Learning with Constraints:

## *Formulation*

### Unconstrained Problem

$$\min_w L(w)$$

$L(w)$  : Any standard loss function,  
say Cross Entropy

# Learning with Constraints: *Formulation*

## Unconstrained Problem

$$\min_w L(w) \quad L(w) : \text{Any standard loss function, say Cross Entropy}$$

## Constrained Problem

$$\min_w L(w) \quad \text{subject to} \quad f_k^i(w) \leq 0; \quad \forall 1 \leq i \leq m; \quad \forall 1 \leq k \leq K$$

# Learning with Constraints:

## *Formulation*

### Constrained Problem

$$\min_w L(w) \quad \text{subject to} \quad f_k^i(w) \leq 0; \quad \forall 1 \leq i \leq m; \quad \forall 1 \leq k \leq K$$

**Where:**

***m***: Size of training data

***K***: Number of Constraints

# Learning with Constraints: *Formulation*

## Constrained Problem

$\min_w L(w)$  subject to  $f_k^i(w) \leq 0; \forall 1 \leq i \leq m; \forall 1 \leq k \leq K$

## Lagrangian

$$\mathcal{L}(w, \Lambda) = L(w) + \sum_{i=1}^m \sum_{k=1}^K \lambda_k^i f_k^i(w)$$

# Learning with Constraints:

## *Formulation*

### Constrained Problem

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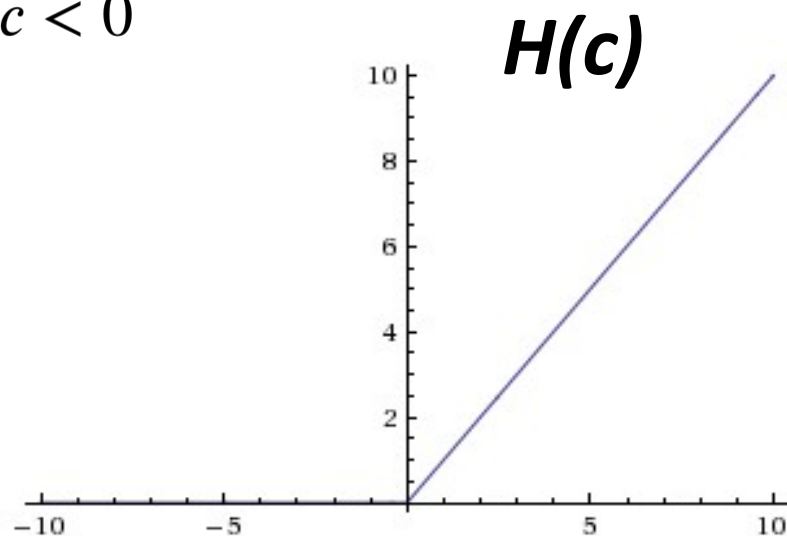
**Issue:**

***O(mK)*** #constraints

i.e. ***mK*** Lagrange Multipliers!

# Learning with Constraints: *Reduce # Constraints*

$$H(c) = c \text{ for } c \geq 0, \text{ and } 0 \text{ for } c < 0$$

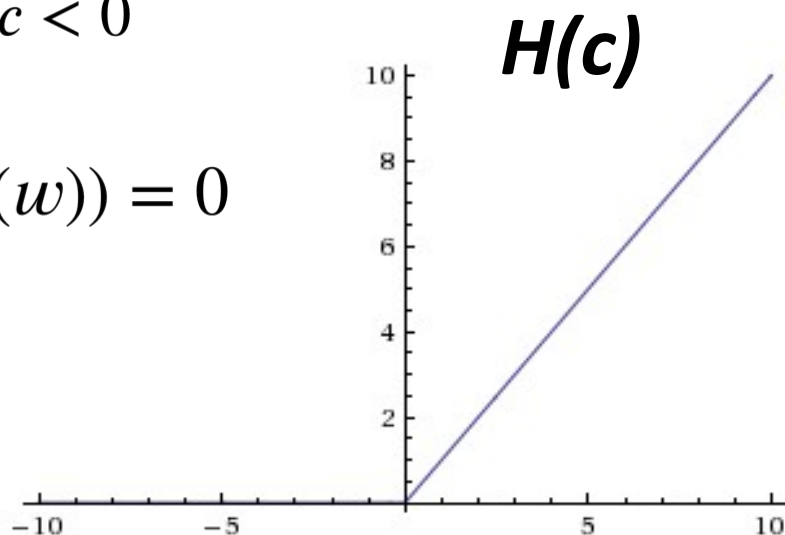


# Learning with Constraints: *Reduce # Constraints*

$$H(c) = c \text{ for } c \geq 0, \text{ and } 0 \text{ for } c < 0$$

$$f_k^i(w) \leq 0 \quad \equiv \quad H(f_k^i(w)) = 0$$

**Equivalent**





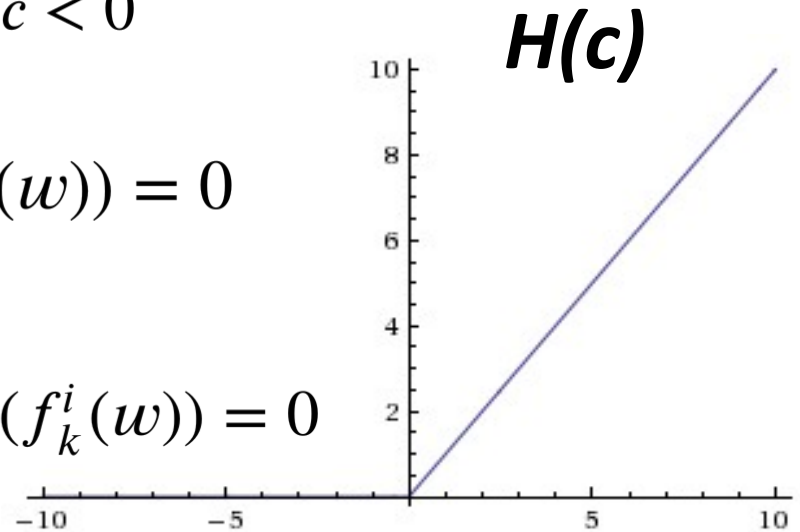
# Learning with Constraints: *Reduce # Constraints*

$$H(c) = c \text{ for } c \geq 0, \text{ and } 0 \text{ for } c < 0$$

$$f_k^i(w) \leq 0 \quad \equiv \quad H(f_k^i(w)) = 0$$

**Equivalent**

$$\forall i : H(f_k^i(w)) = 0 \quad \equiv \quad \sum_i H(f_k^i(w)) = 0$$



# Learning with Constraints: *Reduce # Constraints*

**Originally:**

$$\min_w L(w) \quad \text{subject to} \quad f_k^i(w) \leq 0; \quad \forall 1 \leq i \leq m; \quad \forall 1 \leq k \leq K$$

# Learning with Constraints: *Reduce # Constraints*

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**Now:**

Define:  $h_k(w) = \sum_i H(f_k^i(w))$

$$\min_w L(w) \quad \text{subject to} \quad h_k(w) = 0; \quad \forall 1 \leq k \leq K$$

# Learning with Constraints: *Reduce # Constraints*

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**Now:**

Define:  $h_k(w) = \sum_i H(f_k^i(w))$   **$O(K)$  #constraints**

$$\min_w L(w) \quad \text{subject to} \quad h_k(w) = 0; \quad \forall 1 \leq k \leq K$$

# Learning with Constraints: *Reduce # Constraints*

$$\min_w L(w) \quad \text{subject to} \quad h_k(w) = 0; \quad \forall 1 \leq k \leq K$$

## Lagrangian

$$\mathcal{L}(w; \Lambda) = L(w) + \sum_{k=1}^K \lambda_k h_k(w)$$

# Learning with Constraints:

## *Experiments: Typenet*

	MAP Scores			Constraint Violations		
Scenario	5% Data	10% Data	100% Data	5% Data	10% Data	100% Data
B	68.6			22,715		
B+H	68.71			22,928		
B+C						
B+S						

# Learning with Constraints:

## *Experiments: Typenet*

	MAP Scores			Constraint Violations		
Scenario	5% Data	10% Data	100% Data	5% Data	10% Data	100% Data
<b>B</b>	68.6			22,715		
<b>B+H</b>	68.71			22,928		
<b>B+C</b>	80.13			<b>25</b>		
<b>B+S</b>	<b>82.22</b>			41		

# Learning with Constraints:

## *Experiments: Typenet*

	MAP Scores			Constraint Violations		
Scenario	5% Data	10% Data	100% Data	5% Data	10% Data	100% Data
<b>B</b>	68.6	69.2	70.5	22,715	21,451	22,359
<b>B+H</b>	68.71	69.31	71.77	22,928	21,157	24,650
<b>B+C</b>	80.13	81.36	<b>82.80</b>	<b>25</b>	45	<b>12</b>
<b>B+S</b>	<b>82.22</b>	<b>83.81</b>		41	<b>26</b>	