

# Regular Expressions and Finite State Automata

---

Mausam

(Based on slides by Jurafsky & Martin,  
Julia Hirschberg)

# Regular Expressions and Text Searching

- Everybody does it
  - ◆ Emacs, vi, perl, grep, etc..
- Regular expressions are a compact textual representation of a set of strings representing a language.

<b>RE</b>	<b>Example Patterns Matched</b>
/woodchucks/	“interesting links to <u>woodchucks</u> and lemurs”
/a/	“M <u>a</u> ry Ann stopped by Mona’s”
/Claire_says,/	“ “Dagmar, my gift please,” <u>Claire says,</u> ”
/DOROTHY/	“SURRENDER <u>DOROTHY</u> ”
/!/	“You’ve left the burglar behind again <u>!</u> ” said Nori

# Regular Expressions

RE	Match	Example Patterns
/[wW]oodchuck/	Woodchuck or woodchuck	“ <u>W</u> oodchuck”
/[abc]/	‘a’, ‘b’, <i>or</i> ‘c’	“In uomini, in soldat <u>i</u> ”
/[1234567890]/	any digit	“plenty of <u>7</u> to 5”

# Regular Expressions

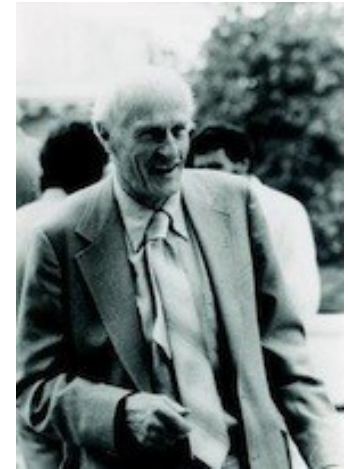
RE	Match	Example Patterns Matched
/ [ A-Z ] /	an upper case letter	“we should call it ‘ <u>D</u> renched Blossoms’ ”
/ [ a-z ] /	a lower case letter	“ <u>m</u> y beans were impatient to be hoed!”
/ [ 0-9 ] /	a single digit	“Chapter <u>1</u> : Down the Rabbit Hole”

# Regular Expressions

RE	Match (single characters)	Example Patterns Matched
[ ^A-Z ]	not an upper case letter	“Oyfn pripetchik”
[ ^Ss ]	neither ‘S’ nor ‘s’	“ <u>I</u> have no exquisite reason for’t”
[ ^\ . ]	not a period	“ <u>o</u> ur resident Djinn”
[ e^ ]	either ‘e’ or ‘^’	“look up <u>^</u> now”
a^b	the pattern ‘a^b’	“look up <u>a^b</u> now”

# Regular Expressions: ? \* + .

Pattern	Matches	
<code>colou?r</code>	Optional previous char	<u>color</u> <u>colour</u>
<code>oo*h!</code>	0 or more of previous char	<u>oh!</u> <u>ooh!</u> <u>oooh!</u> <u>ooooh!</u>
<code>o+h!</code>	1 or more of previous char	<u>oh!</u> <u>ooh!</u> <u>oooh!</u> <u>ooooh!</u>
<code>baa+</code>		<u>baa</u> <u>baaa</u> <u>baaaa</u> <u>baaaaa</u>
<code>beg.n</code>		<u>begin</u> <u>begun</u> <u>begun</u> <u>beg3n</u>



Stephen C Kleene

Kleene \*, Kleene -

# Regular Expressions: Anchors

^ \$

Pattern	Matches
<code>^[A-Z]</code>	<u>P</u> alo Alto
<code>^[^A-Za-z]</code>	<u>1</u> "Hello"
<code>\.\$</code>	The end <u>.</u>
<code>.\$</code>	The end <u>?</u> The end <u>!</u>



# Regular Expressions

RE	Expansion	Match	Examples
\d	[0-9]	any digit	Party_of_5
\D	[^0-9]	any non-digit	Blue_moon
\w	[a-zA-Z0-9_]	any alphanumeric/underscore	Daiyu
\W	[^\w]	a non-alphanumeric	!!!!
\s	[\r\t\n\f]	whitespace (space, tab)	
\S	[^\s]	Non-whitespace	in_Concord

# Regular Expressions

RE	Match	Example Patterns Matched
\*	an asterisk “*”	“K*_A*_P*_L*_A*_N”
\.	a period “.”	“Dr._Livingston, I presume”
\?	a question mark	“Why don’t they come and lend a hand_?”
\n	a newline	
\t	a tab	

# Example

- Find all the instances of the word “the” in a text.
  - ◆ `/the/`
  - ◆ `/[tT]he/`
  - ◆ `/\b[tT]he\b/`
  - ◆ `^[a-zA-Z][tT]he[a-zA-Z]`
  - ◆ `(^|^[a-zA-Z])[tT]he($|^[a-zA-Z])`

# Errors

- The process we just went through was based on **two fixing kinds of errors**
  - ◆ Matching strings that we should not have matched (**there, then, other**)
    - **False positives (Type I)**
  - ◆ Not matching things that we should have matched (The)
    - **False negatives (Type II)**

# Errors

- We'll be telling the same story for many tasks, all semester. Reducing the error rate for an application often involves two **antagonistic** efforts:
  - ◆ **Increasing accuracy, or precision**, (minimizing false positives)
  - ◆ **Increasing coverage, or recall**, (minimizing false negatives).

# Precision & Recall

	Predicted		
Actual		“P”	“N”
	P	TP	FN
	N	FP	TN

$$\text{Precision} = \text{TP}/(\text{TP}+\text{FP})$$

$$\text{Recall} = \text{TP}/(\text{TP}+\text{FN})$$

$$\text{F-measure} = 2pr/(p+r)$$

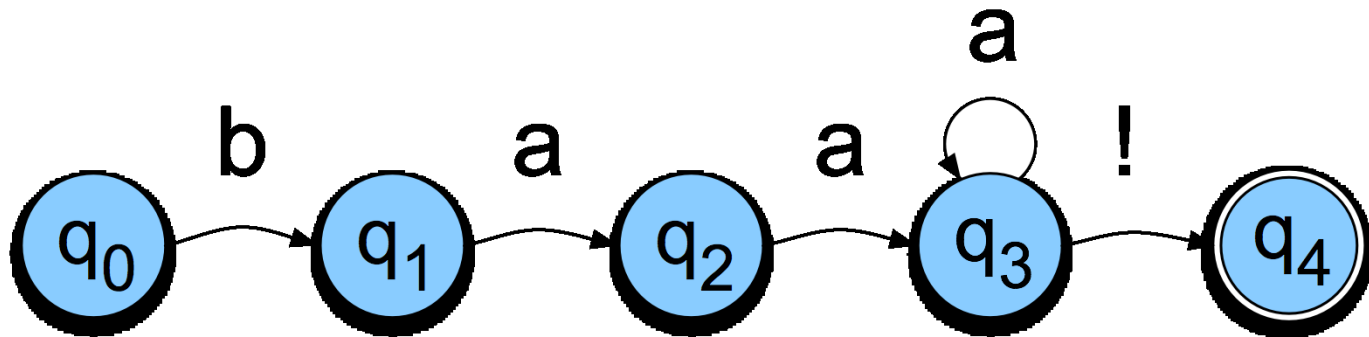
$$F_{\beta} = (1 + \beta^2) \cdot \frac{\text{precision} \cdot \text{recall}}{(\beta^2 \cdot \text{precision}) + \text{recall}}$$

# Finite State Automata

- Regular expressions can be viewed as a textual way of specifying the structure of finite-state automata.

# FSAs as Graphs

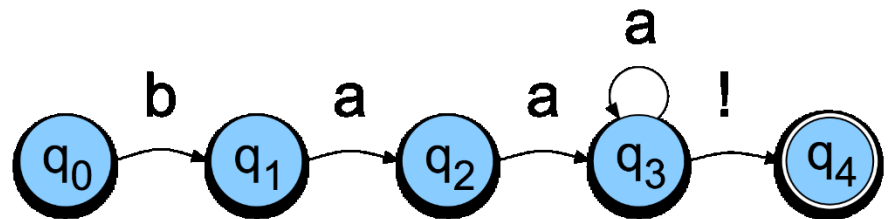
- Let's start with the sheep language
  - ♦ `/baa+!/`





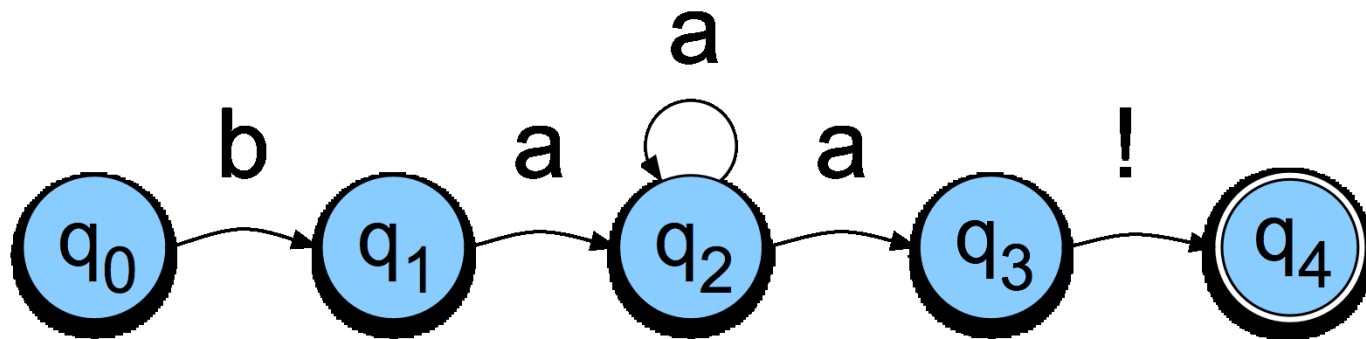
# Sheep FSA

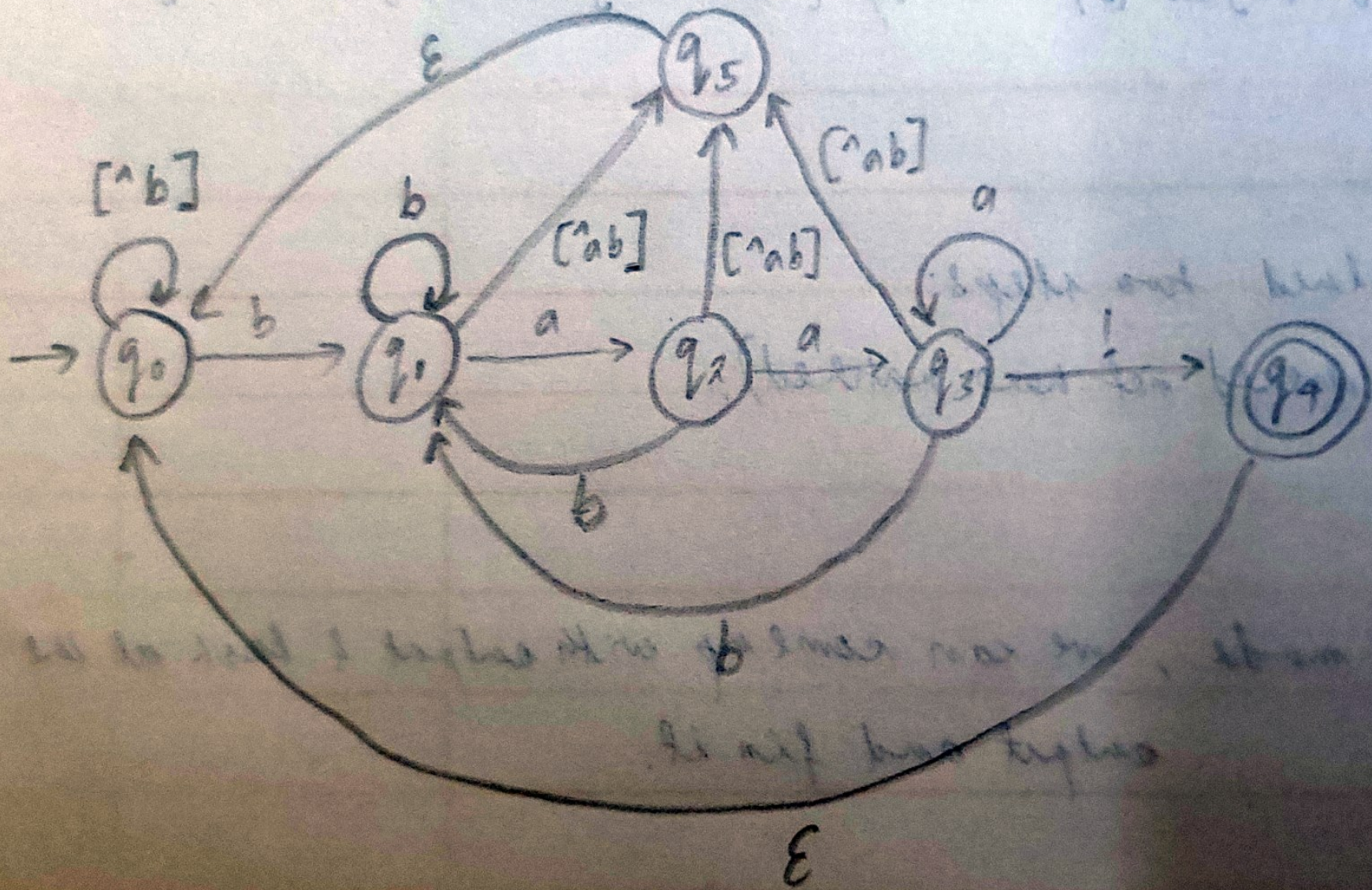
- We can say the following things about this machine
  - ◆ It has 5 states
  - ◆ **b**, **a**, and **!** are in its alphabet
  - ◆  $q_0$  is the start state
  - ◆  $q_4$  is an accept state
  - ◆ It has 5 transitions



# But Note

- There are other machines that correspond to this same language







# Finite State Automata (FSAs)

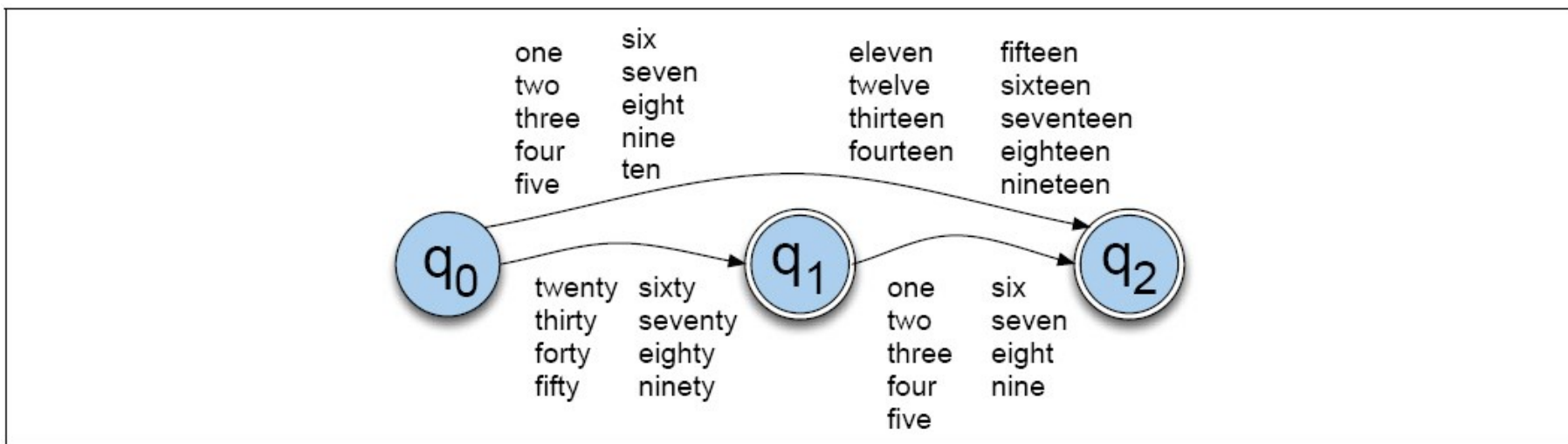
A **finite-state automaton**  $M = \langle Q, \Sigma, q_0, F, \delta \rangle$  consists of:

- A finite **set of states**  $Q = \{q_0, q_1, \dots, q_n\}$
- A finite **alphabet**  $\Sigma$  of input symbols (e.g.  $\Sigma = \{a, b, c, \dots\}$ )
- A designated **start state**  $q_0 \in Q$
- A set of **final states**  $F \subseteq Q$
- A **transition function**  $\delta$ :
  - The transition function for a **deterministic (D)FSA**:  $Q \times \Sigma \rightarrow Q$   
$$\delta(q, w) = q' \quad \text{for } q, q' \in Q, w \in \Sigma$$

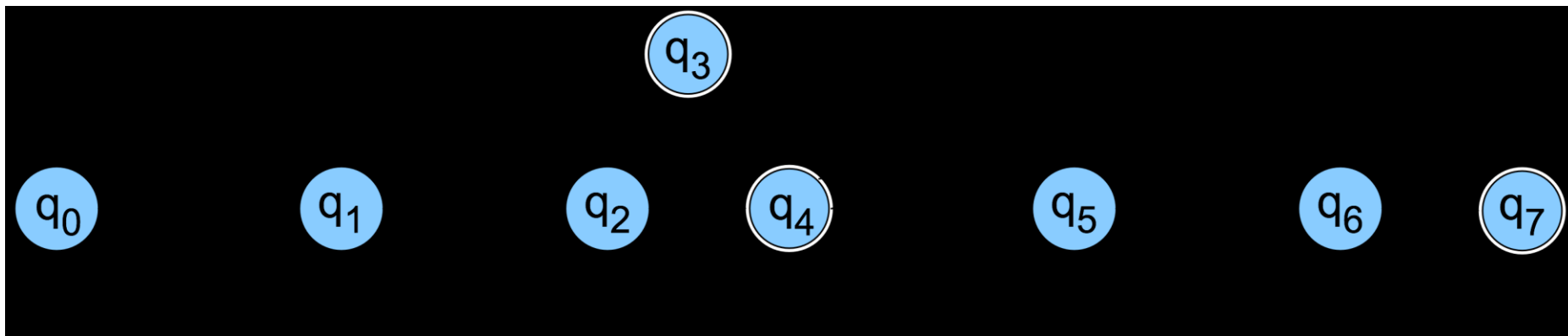
If the current state is  $q$  and the current input is  $w$ , go to  $q'$
  - The transition function for a **nondeterministic (N)FSA**:  $Q \times \Sigma \rightarrow 2^Q$   
$$\delta(q, w) = Q' \quad \text{for } q \in Q, Q' \subseteq Q, w \in \Sigma$$

If the current state is  $q$  and the current input is  $w$ , go to any  $q' \in Q'$

# Dollars and Cents



# Dollars and Cents

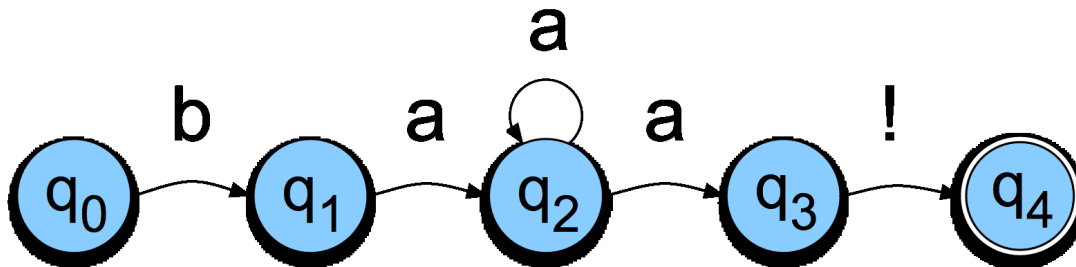


# Yet Another View

- The guts of FSAs can ultimately be represented as tables

If you're in state 1 and you're looking at an a, go to state 2

	b	a	!	e
0	1			
1		2		
2		2,3		
3			4	
4				



# Recognition

- Recognition is the process of determining if a string should be accepted by a machine
- Or... it's the process of determining if a string is in the language we're defining with the machine
- Or... it's the process of determining if a regular expression matches a string
- Those all amount the same thing in the end



# Recognition

- Simply a process of starting in the start state
- Examining the current input
- Consulting the table
- Going to a new state and updating the input pointer.
- Until you run out of input.

# D-Recognize

**function** D-RECOGNIZE(*tape, machine*) **returns** accept or reject

*index* ← Beginning of tape

*current-state* ← Initial state of machine

**loop**

**if** End of input has been reached **then**

**if** *current-state* is an accept state **then**

**return** accept

**else**

**return** reject

**elsif** *transition-table*[*current-state*,*tape*[*index*]] is empty **then**

**return** reject

**else**

*current-state* ← *transition-table*[*current-state*,*tape*[*index*]]

*index* ← *index* + 1

**end**

# Key Points

- Deterministic means that at each point in processing there is always one unique thing to do (no choices).
- D-recognize is a simple table-driven interpreter
- The algorithm is universal for all unambiguous regular languages.
  - ◆ To change the machine, you simply change the table.

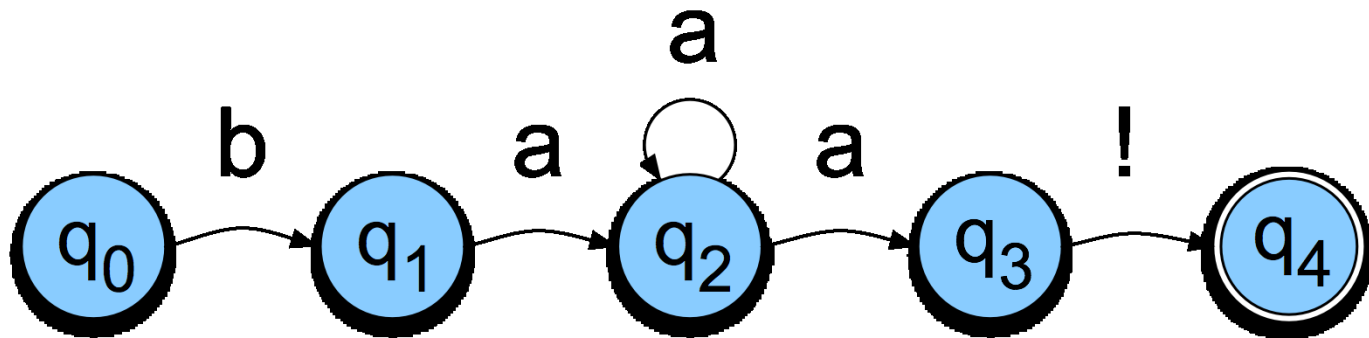
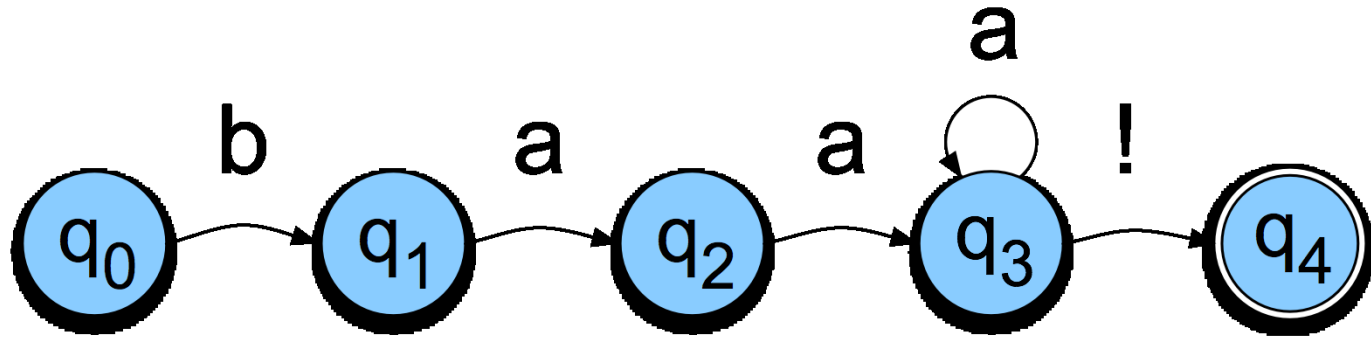
# Generative Formalisms

- *Formal Languages* consist of words whose letters are taken from an alphabet and are well-formed according to a specific set of rules
- Finite-state automata define formal languages (without having to enumerate all the strings in the language)
- The term *Generative* is based on the view that you can run the machine as a generator to get strings from the language.

# Generative Formalisms

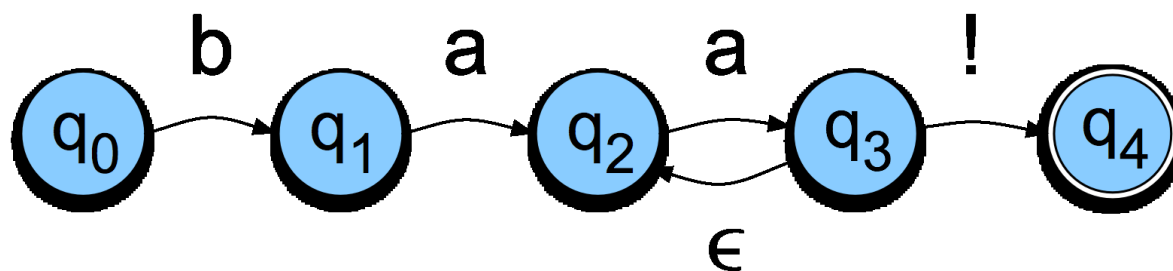
- FSAs can be viewed from two perspectives:
  - ◆ Acceptors that can tell you if a string is in the language
  - ◆ Generators to produce *all and only* the strings in the language

# Non-Determinism



# Non-Determinism cont.

- Yet another technique
  - ◆ Epsilon transitions
  - ◆ Key point: these transitions do not examine or advance the tape during recognition



# Equivalence

- Non-deterministic machines can be converted to deterministic ones with a fairly simple construction
- That means that they have the same power; non-deterministic machines are not more powerful than deterministic ones in terms of the languages they can accept

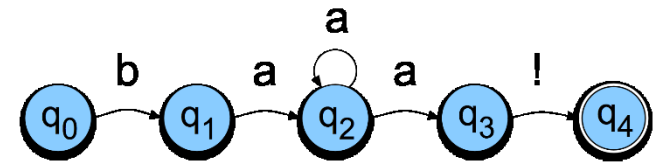
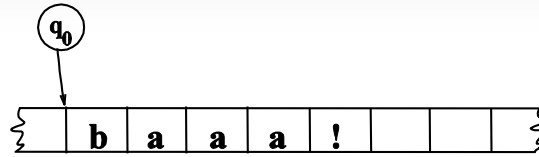


# ND Recognition

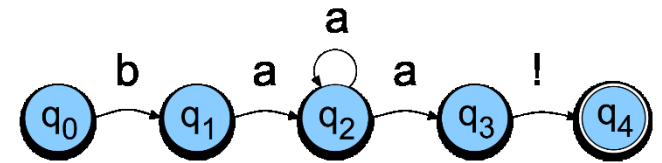
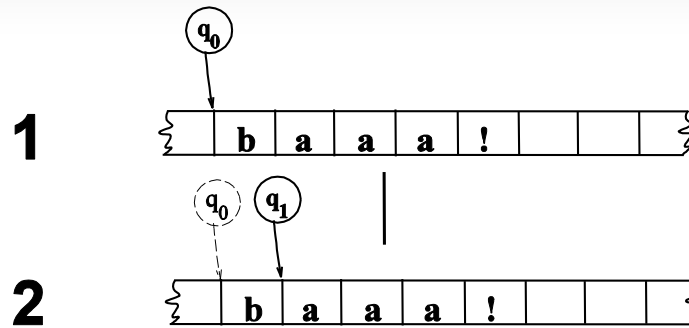
- Two basic approaches (used in all major implementations of regular expressions, see Friedl 2006)
  1. Either take a ND machine and convert it to a D machine and then do recognition with that.
  2. Or explicitly manage the process of recognition as a state-space search (leaving the machine as is).

# Example

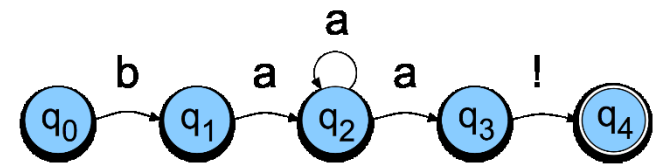
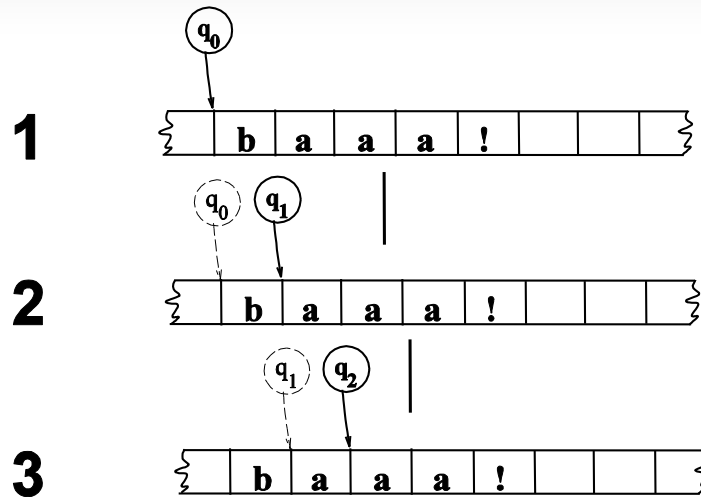
1



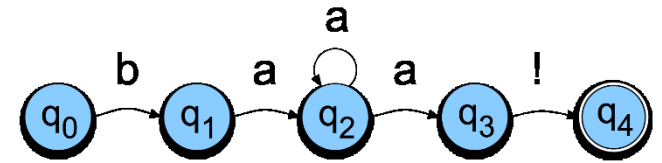
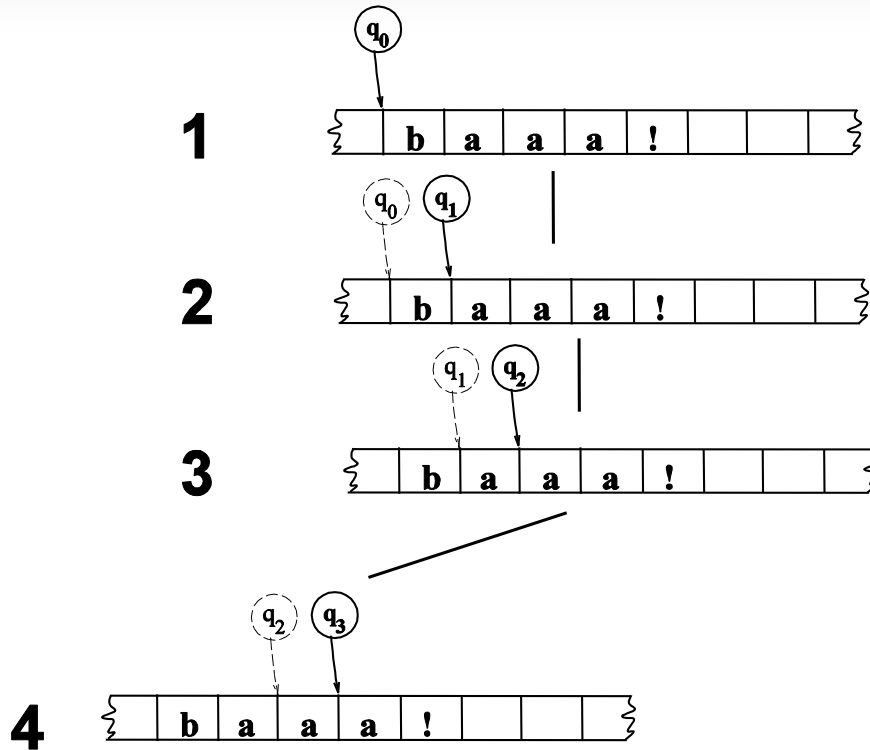
# Example



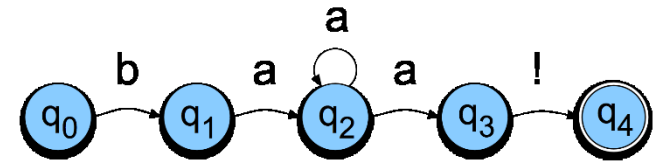
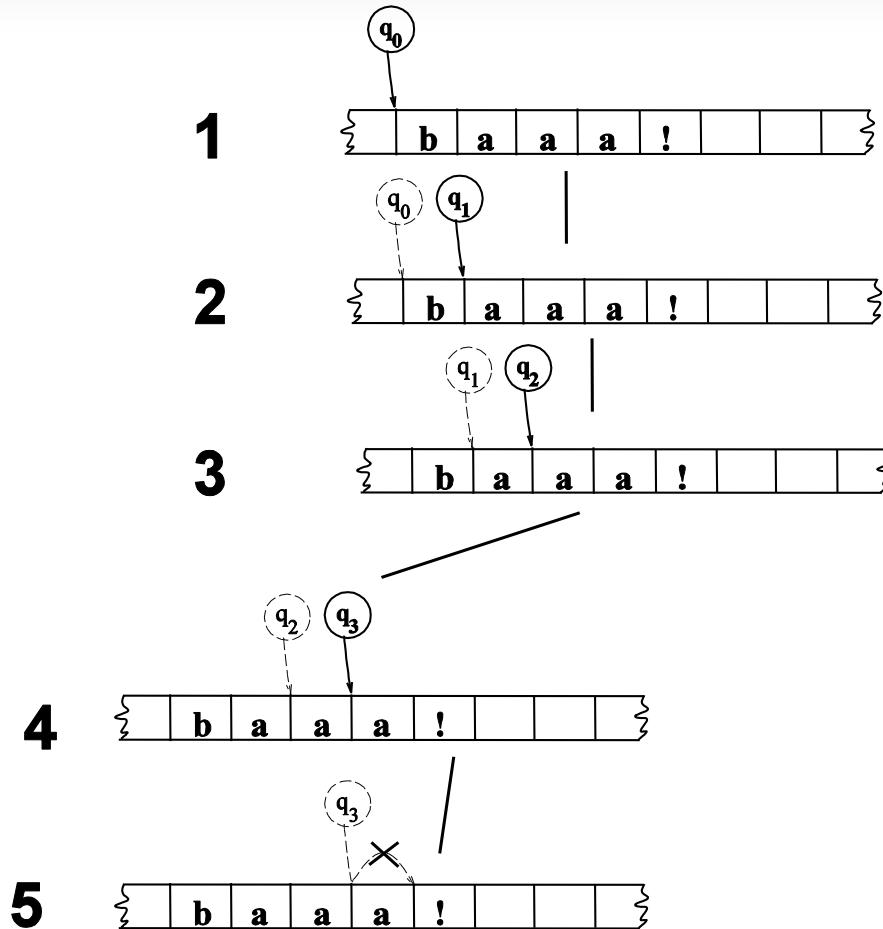
# Example



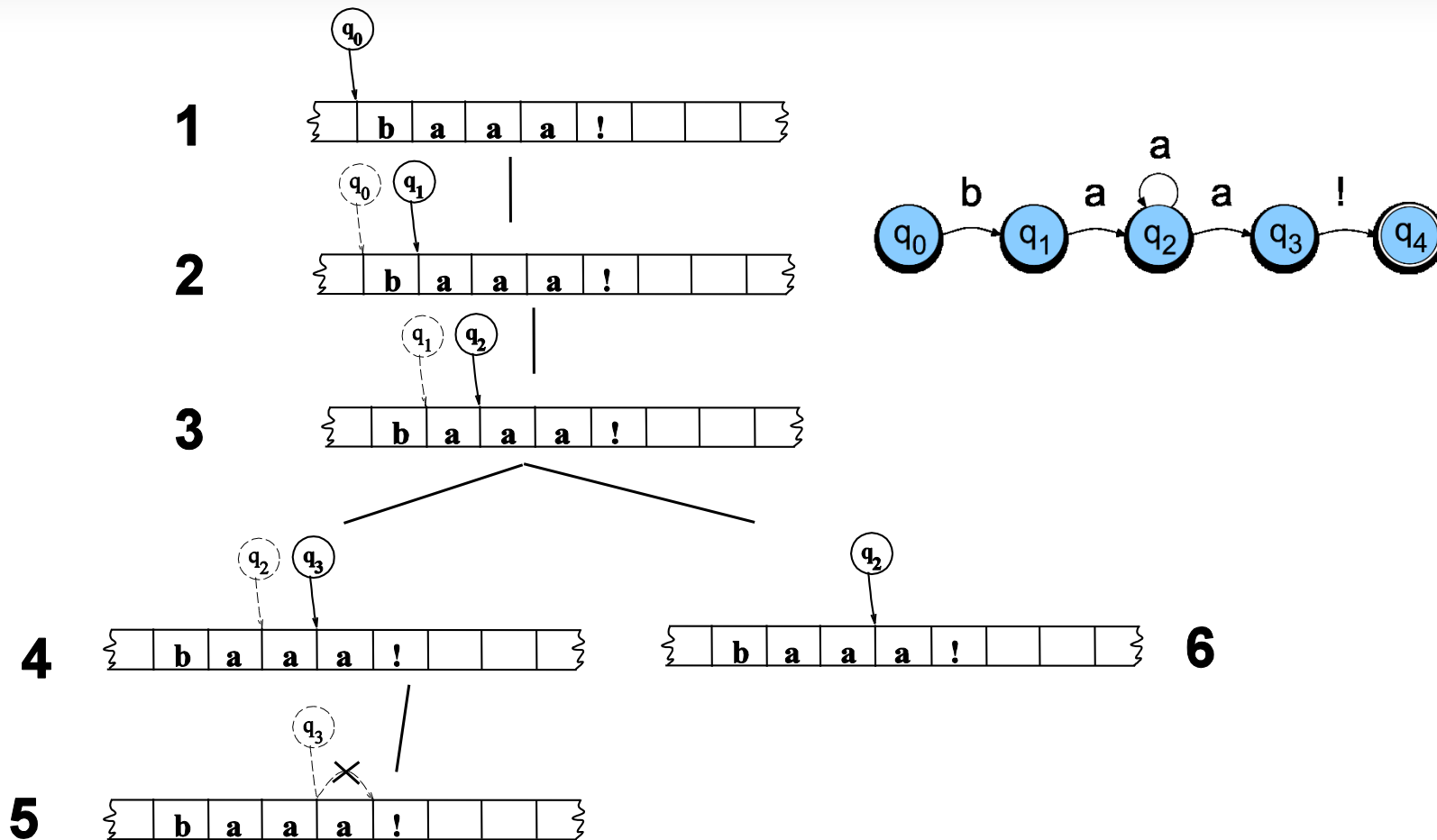
# Example



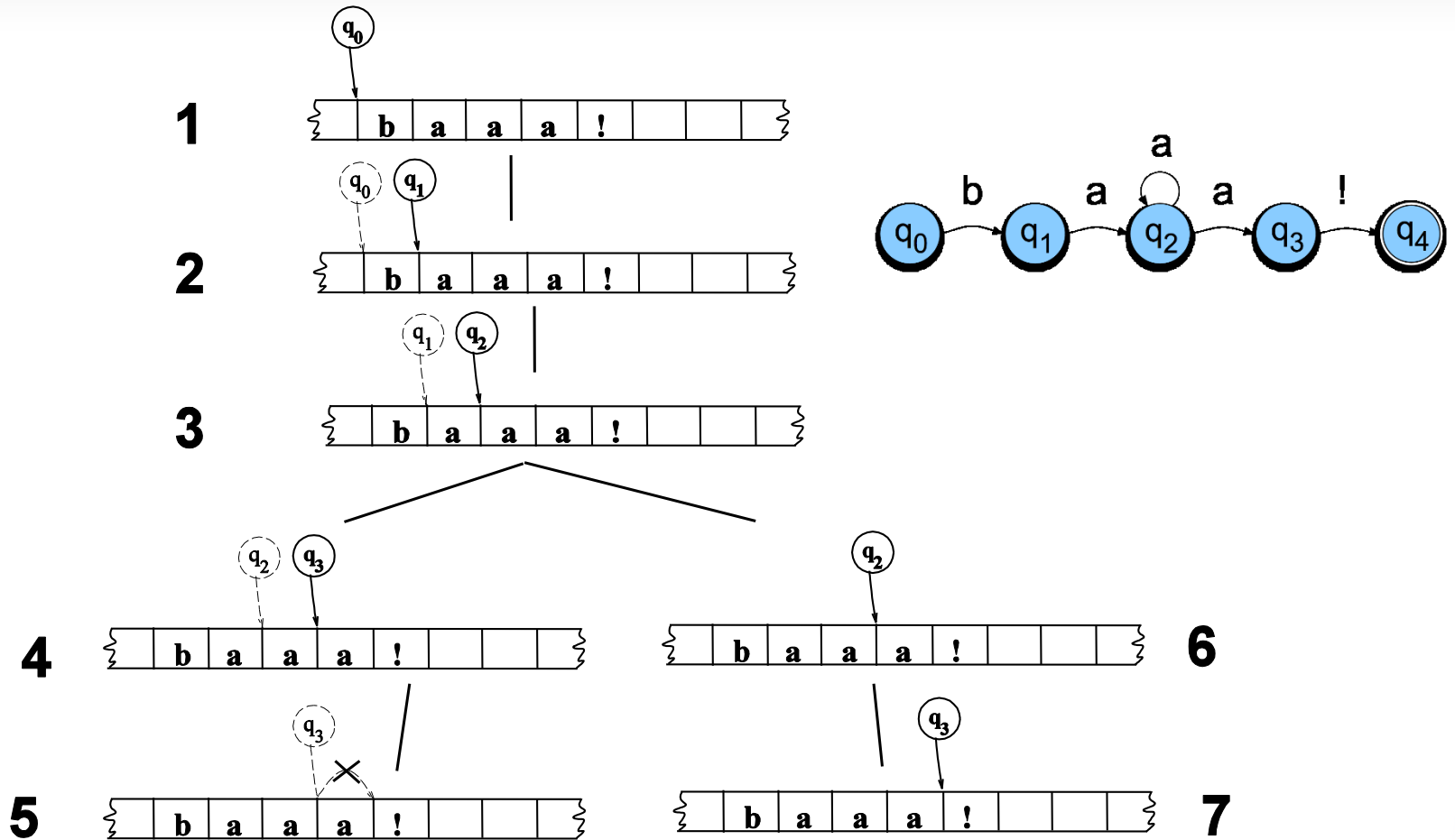
# Example



# Example

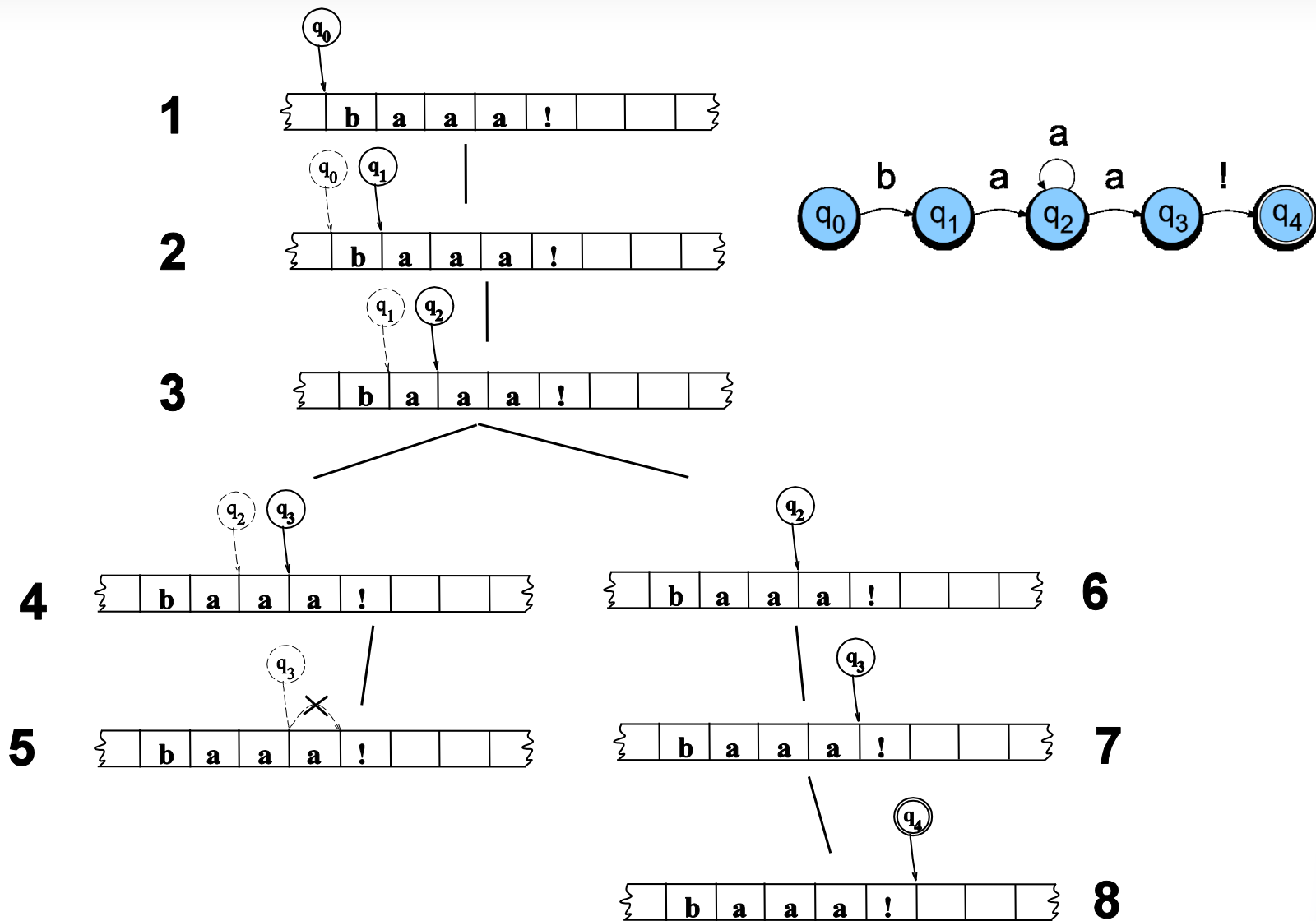


# Example





# Example



# Key Points

- States in the search space are **pairings of tape positions and states** in the machine.
- By keeping track of **as yet unexplored states**, a recognizer can systematically explore all the paths through the machine given an input.

# Uses of Regexes

- Observing simple subcomponents
  - ◆ Dollars and cents
  - ◆ Date, Time
  - ◆ Chemical compounds
  - ◆ Mathematical formulas
  - ◆ Word search in crossword puzzles
  - ◆ Noun compounds, Lexico-POS patterns
- Use regexes in low-data setting
- Use regexes as features in ML

# Summing Up

- Regular expressions and FSAs can represent subsets of natural language as well as regular languages
  - ◆ Both representations may be difficult for humans to use for any real subset of a language
  - ◆ But quick, powerful and easy to use for small problems
- Finite state transducers and rules are common ways to incorporate linguistic ideas in NLP for small applications
- Particularly useful for no data setting