# CS105L: Discrete Structures I semester, 2005-06 

Tutorial Sheet 7: Graph Theory: Paths and Cycles<br>Instructor: Amitabha Bagchi

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1. (Diestel: Proposition 1.3.1) Every graph $G$ contains a path of length $\delta(G)$ and a cycle of length at least $\delta(G)+1$, provided $\delta(G)$, the minimum degree of the graph, is at least 2 .
2. (Diestel: Proposition 1.3.2) Every graph $G$ containing a cycle satisfies $g(G) \leq 2 \cdot \operatorname{diam}(G)+1$, where $g(G)$ is the girth of the graph i.e. the length of the smallest cycle in the graph, and $\operatorname{diam}(G)$ is the diameter of the graph.
3. (Diestel: Chap 1, Prob 3) Let $G$ be a graph containing a cycle $C$, and assume that $G$ contains a path of length at least $k$ between some two vertices of $C$. Show that $G$ contains a cycle of length at least $\sqrt{k}$. Is this the best possible?
